# **CC Shadow Volumes**

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Figure 1: These images demonstrate the benefits of CC shadow volumes on a scene with 96K polygons. Standard shadow volumes are shown in the left image and CC shadow volumes in the middle. Shadow volumes are shown in transparent yellow. The right image shows the shadows generated by CC shadow volumes at interactive rates. CC shadow volumes generate up to 7 times less fill than standard shadow volumes in this scene.

# Abstract

We present a technique that uses culling and clamping (CC) for accelerating the performance of stencil-based shadow volume computation. Our algorithm reduces the fill requirements and rasterization cost of shadow volumes by reducing unnecessary rendering. A culling step removes shadow volumes that are themselves in shadow or do not contribute to the final image. Our novel clamping algorithms restrict shadow volumes to those regions actually containing shadow receivers. In this way, we avoid rasterizing shadow volumes over large regions of empty space. We utilize temporal coherence between successive frames to speed up culling and clamping computations. We obtain substantial reduction in fill requirements and shadow rendering time in dynamic environments composed of up to a 100K triangles.

# 1 Introduction

Shadows are important in computer graphics because they add realism to a scene and can aid in understanding spatial relationships between objects. Shadows have been an active area of research in computer graphics for more than two decades. Advances in graphics hardware have made it possible to accurately render shadows from point light sources in interactive applications including games and walkthroughs.

One popular technique for shadow generation is *shadow volumes* [Crow 1977]. A shadow volume is the region of space behind a shadow caster containing points that lie in shadow. The shadow volume technique computes shadow boundaries implicitly, which makes them attractive for computing shadows on complex geome-

try. Moreover, the asymptotic complexity of shadow generation is linear in the number of shadow caster polygons.

Shadow volumes can be implemented using the stencil buffer on current graphics systems. The algorithm proceeds in three stages. First, the scene is rendered with only ambient lighting. Second, the shadow volumes are rendered to the stencil buffer which sets the stencil in shadowed regions. Finally, the scene is rendered again with full lighting using the stencil test to prevent overwriting the shadows.

A major drawback of the algorithm is that the rasterization of shadow volumes can be expensive. Since shadow volumes extend away from shadow casters toward infinity, they sometimes cover much of the screen, leading to high bandwidth and fill consumption. Often large portions of the rendered shadow volumes make no contribution to the final image. The three main sources of unnecessary shadow volume rendering are: large regions of empty space, shadow casters completely enclosed in other shadow volumes, and shadow generation on parts of the scene not visible to the viewer.

**Main Results:** We present methods for accelerating the performance of stencil buffer-based shadow volume computation. Our algorithms target scenarios where shadow volume rasterization is the major bottleneck. We lower the rasterization overhead in shadow volume computation by using two techniques:

**Shadow Volume Culling**: Using a variation of the shadow culling algorithm presented in Govindaraju et al. [2003], we eliminate the shadow casters that are themselves completely in shadow. We also eliminate the shadow casters whose shadows are not visible to the eye. Shadow volume culling is shown in Fig. 2(b).

Shadow Volume Clamping: By clamping each shadow volume to the regions that contain potential shadow receivers we avoid the cost of rasterizing shadow volumes over large regions of empty space. To compute the occupied regions of a shadow volume we use two techniques. The first technique employs bounding volumes to identify intervals along the shadow volume that contain objects. (Fig. 2(c)). We accelerate the computations by utilizing temporal coherence and performing incremental computations between successive frames. Our second technique divides a shadow volume into discrete regions and utilizes the graphics hardware to test for objects within these regions (Fig. 2(d)).

The culling and clamping (CC) algorithms often work well together. Culling eliminates completely shadowed objects, creating empty space in the shadow volumes. The size of the shadow volumes is reduced by the clamping algorithms, leading to lower rasterization costs.

We have tested our algorithms on a PC with an NVIDIA GeForce 5950FX graphics card. In a dynamic environment composed of 100K triangles, we have observed up to a 7 times reduction in fill and a 4 times speed-up in shadow volume rendering time by using CC shadow volumes over standard shadow volumes.

**Organization:** This paper is organized as follows: Section 2 reviews previous research in the area of interactive shadow generation. Section 3 provides the details of shadow volume culling and clamping. We describe their implementation in Section 4 and highlight their performance. We analyze our techniques in Section 5, discuss some of their limitations, and compare them with other methods.

# 2 Related Work

In this section, we give a brief overview of previous work on fast generation of hard shadows. We mainly focus on two popular techniques: shadow volumes and shadow maps.

### 2.1 Shadow Volumes

Shadow volumes were introduced by Crow [1977]. Bergeron [1985] generalized shadow volumes for non-manifold objects and non-planar polygons. BSP trees have been used to accelerate shadow volume computation [Chin and Feiner 1989; Chrysanthou and Slater 1995; Batagelo and Junior 1999], but they do not work well with dynamic lights or many moving objects.

One of the first hardware implementations of shadow volumes was demonstrated in Pixel-Planes 4 [Fuchs et al. 1985]. Heidmann [1991] implemented Crow's algorithm on graphics hardware using the stencil buffer. This approach, known as the z-pass method, can produce incorrect results when the viewport cuts through a shadow volume. Diefenbach [1996] presented capping methods, but these were not completely robust. To overcome the robustness problems many researchers have proposed z-fail testing for shadow volume computation [Carmack 2000; Everitt and Kilgard 2002]. Lengyel [2002] described a hybrid algorithm that uses faster z-pass rendering when the viewport is not shadowed and z-fail rendering when the viewport is shadowed. McGuire et al. [2003] further improved the performance of Lengyel's algorithm by using culling and depth bounds clipping to reduce the fill consumptions as well as number of triangles rendered. Brabec and Seidel [2003] described an algorithm for fast shadow volume computation using the graphics hardware for silhouette edge computation.

### 2.2 Shadow Maps

Shadow maps were introduced by Williams [1978]. They can be implemented in standard hardware [Segal et al. 1992]. Shadow maps are prone to aliasing due to their limited resolution. Several techniques have been proposed to minimize the impact of aliasing. These include image-precision techniques like percentage closer filtering [Reeves et al. 1987], adaptive shadow maps [Fernando et al.



Figure 3: Standard shadow volumes (left) vs. CC shadow volumes (right).

2001] and perspective shadow maps [Stamminger and Drettakis 2002]. Hybrid algorithms combine some benefits of object-space techniques like shadow volumes or shadow polygons with shadow maps [Brotman and Badler 1984; McCool 2000; Govindaraju et al. 2003; Sen et al. 2003]

# 3 Shadow Volume Acceleration

In this section, we present our algorithms used to accelerate shadow volumes. We represent the scene as a hierarchical scene graph. Each object in the scene is represented as a leaf node in the hierarchy. We further decompose spatially large objects into smaller sub-objects using a k-D tree to provide better localization. The sub-objects can largely be treated as independent objects except when rendering shadow volumes as explained later in Section 3.6.

## 3.1 Shadow Volume Culling

Each object in the scene can be a potential shadow caster as well as a potential shadow receiver. The purpose of shadow volume culling is to eliminate those shadow casters that are themselves in shadow or that cast shadows not contributing to the final image [Govindaraju et al. 2003]. The computation proceeds in two steps:

*1. Compute potential shadow receivers (PSR): PSR* consists of the set of objects potentially visible from the viewpoint of the eye.

2. *Compute potential shadow casters (PSC):* PSC consists of objects visible from the viewpoint of the light (see Fig. 2(b)).

We use occlusion queries and stencil tests for computing *PSC*. From the viewpoint of the light, we render all objects that could possibly cast a shadow, creating a representation of the visible surface in the depth buffer. Next, with depth buffer writes disabled, we render the bounding box of each object using an occlusion query. The occlusion query indicates whether any pixels make it through the pipeline. If all pixels fail the depth test then the object is completely occluded, i.e. completely in shadow. Objects with visible bounding boxes are added to the *PSC*. A similar algorithm can be used to compute *PSR*, except that the scene is rendered from the viewpoint of the eye. If a scene has little occlusion, we use only view-frustum culling to compute *PSC* and *PSR*.

*PSC* may contain objects that cast shadows on areas that are not visible to the eye. Step 2 can be modified slightly to remove these shadow casters. After rendering the occlusion representation, we render *PSR*, setting the stencil when the depth test fails. This identifies the shadowed regions of *PSR*. When performing occlu-



Figure 2: Shadow Volume Acceleration: (a) Every object in the scene is a potential shadow caster as well as a shadow receiver. (b) Shadow Volume Culling: The shadow casters visible to the light are  $PSC = \{O_1, ..., O_5\}$  and shadow receivers visible to the eye are  $PSR = \{O_1, O_2, O_3, O_5\}$ . (c) Continuous Shadow Clamping: Shadow volumes  $SV_i$  are clamped by using AABBs around the shadow receivers to compute clamped volumes  $CV_i$ . (d) Discrete Shadow Clamping: Testing for object containment in regions defined by slicing planes refines  $CV_5$  to a smaller  $\overline{CV}_5$ . Culling and clamping reduce the original shadow volumes to only  $CV_1 \dots CV_4$  and  $\overline{CV}_5$ , reducing fill requirements considerably.

sion queries, we also enable the stencil test so only shadow casters covering shadowed regions are included in *PSC*.

### 3.2 Shadow Volume Clamping

Each shadow volume extends to infinity, thus its projection can cover a large number of pixels in the stencil buffer. To reduce fill consumption we compute *clamped volumes* that more tightly enclose the objects in *PSR* (see Fig. 2(d)).

We use two different clamping techniques that are in some ways complimentary. Each technique uses a different method for determining where interactions occur between shadow receivers and a shadow volume. The continuous algorithm clamps precisely to the bounds of the shadow receivers, but can overestimate the size of a shadow volume when only a small part of the receiver lies in shadow. The discrete algorithm clamps only to truly occupied regions, but the bounds on the region are only as accurate as the region discretization. Both algorithms can be used together. Poorly clamped volumes resulting from continuous clamping can be further refined using discrete clamping (see Fig. 2).

#### 3.3 Continuous Shadow Clamping

Continuous shadow clamping proceeds in two steps (Fig. 4). First, we use overlap tests in the light view to identify the shadow receivers that lie in each shadow volume. Then we compute the occupied intervals along a shadow volume by merging the extents of the shadow receivers it contains. These computations are performed entirely on the CPU.

**Overlap Tests:** We calculate overlaps using the axis-aligned bounding boxes (AABBs) of the objects' projection on the light's image plane. We also compute the depth interval  $(z_{min}, z_{max})$  of each object in light-space. An object S is considered to lie within the shadow volume of an object T when the AABBs of S and T overlap and when the  $z_{min}$  of S is greater than the  $z_{min}$  of T.

**Occupied Intervals Computation:** Computation of occupied intervals can be performed efficiently by processing all the shadow casters simultaneously. Each shadow caster stores a list of the intervals occupied by the receivers within its shadow volume. The lists are initialized with the depth intervals of the shadow casters themselves to account for self-shadowing. Then we process the shadow receivers according to their  $z_{min}$  value, from smallest to largest, updating the occupied intervals of the shadow volumes in which each receiver lies. Since the shadow receivers are processed in order, only the last occupied interval in each list needs to be updated. There are three possible ways to update the occupied interval:

**1**. The occupied interval completely contains the receiver. Nothing is done in this case.

**2**. The occupied interval partially contains the receiver. The interval is extended to include the receiver.

**3**. The object lies completely outside the occupied interval. In this case the depth interval of the receiver is added to the occupied interval list.

Whenever a new occupied interval is created in case 3, two sets of caps and an extra set of edges must be drawn. If the size in screen-space of the gap between successive intervals is small, the cost of rendering the new shadow volume interval may exceed any savings in rasterization cost. A simple heuristic can be used for determining whether or not to create a new interval. Let V be the vertex processing cost of the new interval and R be the rasterization cost of the gap. If V > R, then a new interval is not created. Instead, the receiver depth interval is merged as in case 2.



Figure 4: **Continuous Clamping**: Bounding box overlap tests on the light's image plane are used to determine potential shadow receivers. Depth intervals of receivers are merged to determine shadow volume intervals.



Figure 5: **Discrete Clamping**: A single shadow caster is tested against an empty region (left). In the next slice (right), the region is occupied so a shadow volume is rendered for this region.

*V* and *R* can be computed with the following equation:

$$V = (2C+2S)v,$$
  
$$R = Ar$$

where *C* and *S* are the number of vertices in the shadow volume cap and silhouette respectively, *v* is cost per vertex, *A* is an estimate of the area of the gap in pixels, and *r* is the rasterization cost per pixel. The values of *v* and *r* can be determined empirically by rendering a "typical" set of shadow volumes at different resolutions. Rendering at a low resolution, e.g.  $10 \times 10$ , gives an estimate of *v*. Rendering at high resolution and subtracting *v* gives an estimate of *r*. Though this heuristic assumes an overly simplified model of graphics processing, it gives acceptable results.

**Temporal Coherence:** We accelerate the overlap tests by performing incremental computations. We employ a variation of the sweepand-prune algorithm [Cohen et al. 1995] used to perform bounding box overlap tests in large environments composed of multiple moving objects. We project the intervals of the AABBs along the Xand Y axis in the light's image plane and sort the projected values along each axis. When the objects or the light move we update the AABBs and re-sort the list using an insertion sort with local interchanges. The list of depth intervals is maintained similarly. We compute the overlapping AABBs from the sorted lists.

#### 3.4 Discrete Shadow Clamping

The continuous shadow clamping algorithm computes clamped volumes  $CV_i$  for each shadow caster based on the AABBs of shadow receivers. In many cases, AABBs can generate tight fitting clamped volumes (e.g.  $CV_1, CV_2$  in Fig. 2(c)). Since the entire extents of the shadow receivers are included in the shadow volume, the clamped volumes may fit poorly (e.g.  $CV_5$  in Fig. 2(c)). Discrete shadow clamping divides a shadow volume into discrete regions and uses the GPU for testing which regions contain shadow receivers. Discrete clamping can be used by itself or to refine poorly clamped volumes produced by continuous clamping.

We partition the scene into slices by using a set of similarly oriented slicing planes (Fig. 5). The slices partition each shadow volume into disjoint regions. We then use occlusion queries to determine if shadow receivers lie within these regions. A convenient choice for slicing planes are those which face towards the light source and pass through the viewpoint, splitting the image plane into strips of equal width. The discrete shadow volume regions created by these slicing planes cover an approximately equal area on the image plane, regardless of how far away the shadow volume is from the viewpoint. An additional benefit is that the caps between regions need not be drawn. Since they lie on planes that pass through the eye, the caps do not affect any pixels. Note that this choice of planes is most useful if the light source lies outside the view frustum. This corresponds to situations where the empty space problem is most common.



Figure 6: *CC shadow volumes in a 96K polygon scene composed of multiple robots.* 

The discrete clamping computations are performed in the light's view. Each slice is rendered in back-to-front order using a pair of clipping planes. We check each shadow caster against the slice to determine if there are objects in this region of its shadow volume. We project the shadow caster to the slicing plane below the slice. With the depth test set to *GREATER*, we use an occlusion query to determine if objects lie in front of the projected shadow caster.

Projecting the shadow caster into a plane does not change its shape in the light view, only the depth of the pixels rasterized. The projection is accomplished with a simple transformation matrix. A plane **p** is represented in homogeneous 4D coordinates as  $\mathbf{p} = (a \ b \ c \ d)$  with vector components corresponding to the coefficients of the plane equation:

$$ax + by + cz + d = 0$$

The 4 × 4 matrix **M** that projects onto the plane **p** through a center of projection  $\mathbf{c} = (c_x c_y c_z 1)$  is given by:

$$\mathbf{M} = \mathbf{c} \otimes \mathbf{p} - (\mathbf{p} \cdot \mathbf{c})\mathbf{I}$$

where  $\otimes$  denotes outer product and **I** is the identity matrix. **M** should be negated if the center of projection is behind the plane. Though this has no effect on the final 3D coordinates of the projected points, it does ensure that the fourth coordinate is positive, which is necessary to prevent the point from being clipped by the graphics hardware. If a portion of an object is farther away from a slicing plane than the light, then it will not be projected correctly. To handle this problem, the edges of the object's shadow volume should be extruded to infinity from the last plane onto which the object can be correctly projected.

#### 3.5 Conservative Discrete Shadow Clamping

The use of image-precision occlusion queries in discrete clamping may lead to sampling errors due to limited screen resolution and z-buffer precision. The errors can cause occupied regions to be incorrectly classified as empty leading to small areas of missing shadows. A recent paper [Govindaraju 2004] describes a technique for performing robust collision detection on graphics hardware. This technique "fattens" the geometric primitives sufficiently to avoid sampling errors. Discrete clamping is a collision detection problem between shadow casters and the objects within the slices. We can adapt the conservative collision technique to perform reliable clamping. First, the bounding representations of the shadow volumes are constructed and fattened. Using these representations, we can then perform collision detection with the fattened objects enclosed in the slices. The method would be slower but would eliminate the image-precision artifacts.



Figure 7: CC Shadow Volumes (CCSV) vs. Standard Shadow Volumes (SV): These graphs show the reduction in fill and shadow volume rendering time obtained with CCSVs in two test scenes. Also shown is the fill that actually results in stencil writes (CCSV-SW and SV-SW), clamping time, and the time to render shadow volumes with an empty depth bounds range (CCSV-DB and SV-DB).

#### 3.6 Rendering Clamped Volumes

Both continuous and discrete clamped shadow volumes are rendered in a similar manner. In the continuous case, silhouette edges of a shadow caster are extruded to form quads that extend across the covered intervals or regions. Caps are drawn at interval boundaries. In the discrete case, the quads are formed by projecting the silhouette edges onto the slicing planes. No caps need to be drawn because they lie in the slicing planes which pass through the eye and have zero area in screen-space.

Two shadow casters may have edges in common if they are subobjects of the same parent object. To minimize the size of the shadow volume sides arising from shared edges, the list of occupied intervals or regions for the triangles on either side of a shared edge are merged. Portions occupied on both sides are not drawn.

### 3.7 Omnidirectional Light Sources

The culling and clamping algorithms use planar projections, which implies that they can only be used within a restricted frustum. For omnidirectional light sources, CC shadow volumes can be used for a portion of the space around the light and standard shadow volumes can be used for the rest. This works especially well for lights that are located near the edge of the viewport or close to a wall. In these cases, the large shadow volumes which would benefit most from culling and clamping lie predominantly in one direction.

#### 4 Implementation and Performance

We have implemented our system on a PC with a NVIDIA GeForce FX 5950 Ultra graphics card and dual 2.8GHz Xeon processors, although only one processor was utilized for our computations. The system uses the OpenGL API. We use the *vertex array range* extension for accelerating shadow volume rendering by storing the vertex information in video memory on the graphics card. To perform occlusion queries, we use the *GL\_NV\_occlusion\_query* extension.

Both the CPU and the GPU are used for computation. The computations are organized so as to maximize parallelism. Occlusion queries for culling and clamping require the CPU to wait for the GPU, so they are performed first. Then using data precomputed in the previous frame, the CPU rapidly issues the commands for the ambient pass, shadow volume rendering, and the lit pass. While the GPU to processes the commands, the CPU constructs the shadow volumes for the next frame. The CPU computations usually finish before the GPU, so they have no affect on the frame rate.

We tested the performance of our system on two different scenes:

**1. Corridor Scene:** The corridor shown in Fig. 1 is part of a model consisting of 96K triangles. Most of the primitives are contained in the complex trusses overhead which cast shadows on the floor and walls below. This scene demonstrates the savings achieved by shadow volume clamping. Most of the shadow volumes traverse empty space. Since there is very little occlusion in the scene, we perform only view-frustum culling to compute *PSC* and *PSR*.

**2. Robot Scene:** This part of the scene is a large room with a crowd of moving robots (Fig. 6) which creates a high degree of occlusion. When the light is placed low in the scene, the shadow

culling algorithm removes many shadow casters.

Fig. 7 shows the fill and shadow volume rendering times for the paths shown in the video. The test scenes were rendered at  $1280 \times 1024$  resolution. Clamping and culling are performed at the same resolution. The fill we measured is the total number of pixels touched when rendering the shadow volumes with the depth test disabled. We also measured the number of stencil writes (CCSV-SW and SV-SW). For z-pass shadow volumes, this is equivalent to the number of fragments that pass the depth test. For both paths there are portions where z-fail shadow volumes are faster than zpass shadow volumes, and vice versa. Z-pass was used for path 1 and z-fail for path 2. The average frame rates were similar with either setting. Discrete and continuous clamping give comparable results for these paths, though discrete clamping is takes twice as long for path 2 because more occlusion queries are used. Continuous clamping performs best when the light direction is aligned well with the geometry in the scene. In general, discrete clamping tends to result in greater fill savings and reduced shadow volume rendering time.

With CC shadow volumes we observed up to 7 times reductions in fill and a 4 times speed-up in shadow volume rendering time. For the paths shown in Fig. 7, we see an average of 2–3 times reduction in fill and 2.5 times speed-up in shadow volume rendering time. Table 1 shows the breakdown of the average timings.

### 5 Analysis

The cost of shadow volume rendering can be divided into two parts. The vertex processing cost includes the time to compute the vertices of the shadow volumes on the CPU and the time to transmit, transform, and set up the geometric primitives on the graphics hardware. This cost is independent of screen resolution. The rasterization cost is higher when anti-aliasing is enabled and increases proportionally with screen size. Our algorithm is targeted for scenes in which rasterization cost is the major bottleneck. Shadow volume culling reduces both the vertex processing and rasterization cost by eliminating the redundant shadow volumes altogether. Shadow clamping splits the shadow volumes to significantly reduce rasterization cost in empty space while increasing the vertex processing cost. The graphs in Fig. 7 show the existence of a strong empirical relationship between the area of the shadow volumes and the shadow volume rendering time, though the exact relationship can be hardware dependent.

In continuous clamping, the overlap tests are relatively inexpensive. Although there are potentially  $n^2$  interactions between shadow casters and shadow receivers, by utilizing temporal coherence the expected running time is reduced to O(n + k), where k is the actual number of overlapping bounding boxes. In typical scenes, k is usually fairly small. The main cost is incurred in merging depth

Average Timings (ms)					
	Scene 1		Scene 2		
	SV	CCSV	SV	CCSV*	CCSV
Ambient + Lit	6.6	6.6	7.4	7.4	7.4
SV Rendering	49.4	20.0	59.7	32.8	24.7
Clamping	-	2.9	-	-	4.6
Culling	-	-	-	6.9	6.9
Frames per sec.	18.6	38.1	15.4	23.3	27.3

Table 1: Timing for standard shadow volumes (SV), CC shadow volumes (CCSV), and CC shadow volumes without clamping (CCSV\*). Note that most CPU computations are performed while the GPU renders the scene and the shadow volumes, so they do not affect the frame rate.

intervals.

For the discrete clamping, vertex processing and clamping costs increase linearly with the number of slices. The overall savings introduced by adding more slices are large at first, but then begin to diminish. At some point the cost of additional slicing planes dominates the savings. In our experiments 8 - 20 slices seemed to work well.

The extra rendering used for performing culling and discrete clamping is fairly inexpensive for several reasons.

1. Whenever possible, we use tight bounding volumes instead of the objects themselves to reduce rendering overhead.

**2**. There are no pixel writes when performing occlusion queries, so this rasterization is less expensive than that of shadow volumes.

**3**. There is less overdraw. The depth complexity in light view is usually much lower than that of the shadow volumes when looking at them through the side.

Thus the extra rendering to reduce the size and complexity of large shadow volumes often leads to significant savings.

Occlusion queries are currently a bottleneck in our system. We have observed a maximum of only 1.2M queries per second at any resolution, though the graphics hardware can render the objects at a much higher rate. We expect the overhead associated with occlusion queries will be reduced considerably in the future. Since the current performance of occlusion queries is slow we are forced to use fewer of them. We have to use a coarser object subdivision which leads to less fill savings.

### 5.1 Limitations

CC shadow volumes are appropriate only for those situations where rasterization is a bottleneck. In addition, there must be some degree of *unnecessary* shadow volume rendering. Consider the complex self-shadowing of branches in a tree. Shadow volumes in such a scene may be fill-bound, but since there are few large occluders to create occlusion and there are few large regions of empty space, CC shadow volumes would provide very little performance gain. Clamping would probably work well, however, to eliminate the empty space in the shadow volumes between the branches and the ground. In general, culling and clamping work best on complex models, which either have a high degree of occlusion or large empty spaces.

Tight bounding volumes for the objects are important. If the bounds are too loose much of the potential savings may be lost. Long, thin objects with a large aspect ratio can be especially problematic for the continuous shadow clamping algorithm because AABBs often provide a poor fit.

Occlusion queries used in culling may lead to artifacts. The visibility computations are performed at image-precision. The sampling on the image plane may miss small holes or small occluders, leading to incorrect shadows. Triangles that are nearly parallel to the view can also be problematic because they are covered by few samples. These sampling problems are reduced by using bounding boxes around the objects and by ensuring that the light's view is fit tightly to the visible objects in the scene in order to maximize the sampling resolution.

Another drawback of CC shadow volumes is that they require more CPU time to construct. Methods that off-load shadow volume construction to the GPU [Brabec and Seidel 2003] are difficult to adapt for use with CC shadow volumes. Though shadow volume construction on the CPU does not adversely affect frame-rate in our current implementation, it less time remains for other computations.

#### 5.2 Comparison with other Methods

BSP-tree based shadow volumes [Chin and Feiner 1989; Chrysanthou and Slater 1995; Batagelo and Junior 1999] can render shadows efficiently in static scenes or scenes with few moving objects. However, when the light source moves or many objects move, large portions of the BSP-tree need to be re-built, which is usually an expensive process. Our algorithms can easily handle dynamic scenes with a moving light source. The only limitation is that continuous clamping algorithm requires coherent motion. The discrete clamping algorithm is completely insensitive to motion.

McGuire et al. [McGuire et al. 2003] recently demonstrated an effective algorithm for accelerating shadow volumes. Their method uses a combination of the OpenGL scissor test and depth bounds tests to reduce shadow volume fill. The scissor region is set to the intersection of the viewport with the screen projection of the light's region of influence. In the types of scenes for which our algorithm was designed, the scissor region would usually contain the entire viewport because the whole scene is within the light's region of influence. Thus the only fill savings come from the depth bounds test. Fig. 7 shows the time to render the shadow volumes with a depth bounds range set to (0,0). This range effectively rejects every fragment early from the pipeline. The timings indicate that even with the depth bounds test the rasterization cost is still significant. In fact, even if no pixels were to pass the depth bounds test, these results indicate that on the same hardware, CC shadow volumes would be faster for these scenes. For scenes with little occlusion or without large, mostly empty shadow volumes, our algorithm would perform poorly because the overhead would dominate the potential savings.

# 6 Conclusion and Future Work

In this paper, we have presented algorithms for shadow culling and shadow clamping to accelerate the performance of shadow volumes. These include visibility computations for shadow culling and continuous and discrete shadow clamping. These algorithm can be efficiently implemented by utilizing temporal coherence between successive frames. We have demonstrated the performance of these algorithms on two relatively complex environments, reducing fill requirements by up to 7 times.

There are several avenues for future work. Our main focus in this paper has been to reduce rasterization costs. We would like to explore methods to reduce the vertex processing cost of shadow volumes which remains fairly high. Adaptive approaches using slice coverage information from one frame might be used to compute a better set of slicing planes for the next, i.e. use temporal coherence for discrete shadow clamping. We could also improve the continuous clamping by computing better depth bounds with more sophisticated overlap tests. Finally we would like to extend these ideas to improve the performance of soft shadow generation algorithms.

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