

Comp 790-058 Lecture 10: Autonomous Driving: Control, Traffic, Predictions

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Administrative

- ✦ Homework 2 due:
 - ⑩ 11:59 PM October 30th
- ✦ Homework 3:
 - ⑩ Not today! But this week.
- ✦ Project Updates:
 - ⑩ Remember to work consistently on projects
 - ⑩ It WILL sneak up on you
- ✦ AutonoVi Updates:
 - ⑩ Git setup
 - ⑩ If you need access, please see me after class



Structure

★ Recap

- ⑩ Perception

- ⑩ Localization

- ⑩ State / Kinematics / Dynamics

- ⑩ Planning

★ Control

★ Traffic-Sim

★ Prediction



Autonomous Driving

- ★ **Autonomous vehicle**: a motor vehicle that uses artificial intelligence, sensors and global positioning system coordinates to drive itself without the active intervention of a human operator
- ★ Focus of enormous investment [\$1b+ in 2015]



Tesla



Waymo



Nutonomy



Autonomous Driving: Levels of Autonomy

- ★ 0: Standard Car
- ★ 1: Assist in some part of driving
 - ⑩ Cruise control
- ★ 2: Perform some part of driving
 - ⑩ Adaptive CC + lane keeping
- ★ 3: Self-driving under ideal conditions
 - ⑩ Human must remain fully aware
- ★ 4: Self-driving under near-ideal conditions
 - ⑩ Human need not remain constantly aware
- ★ 5: Outperforms human in all circumstances



Autonomous Driving: Main Components

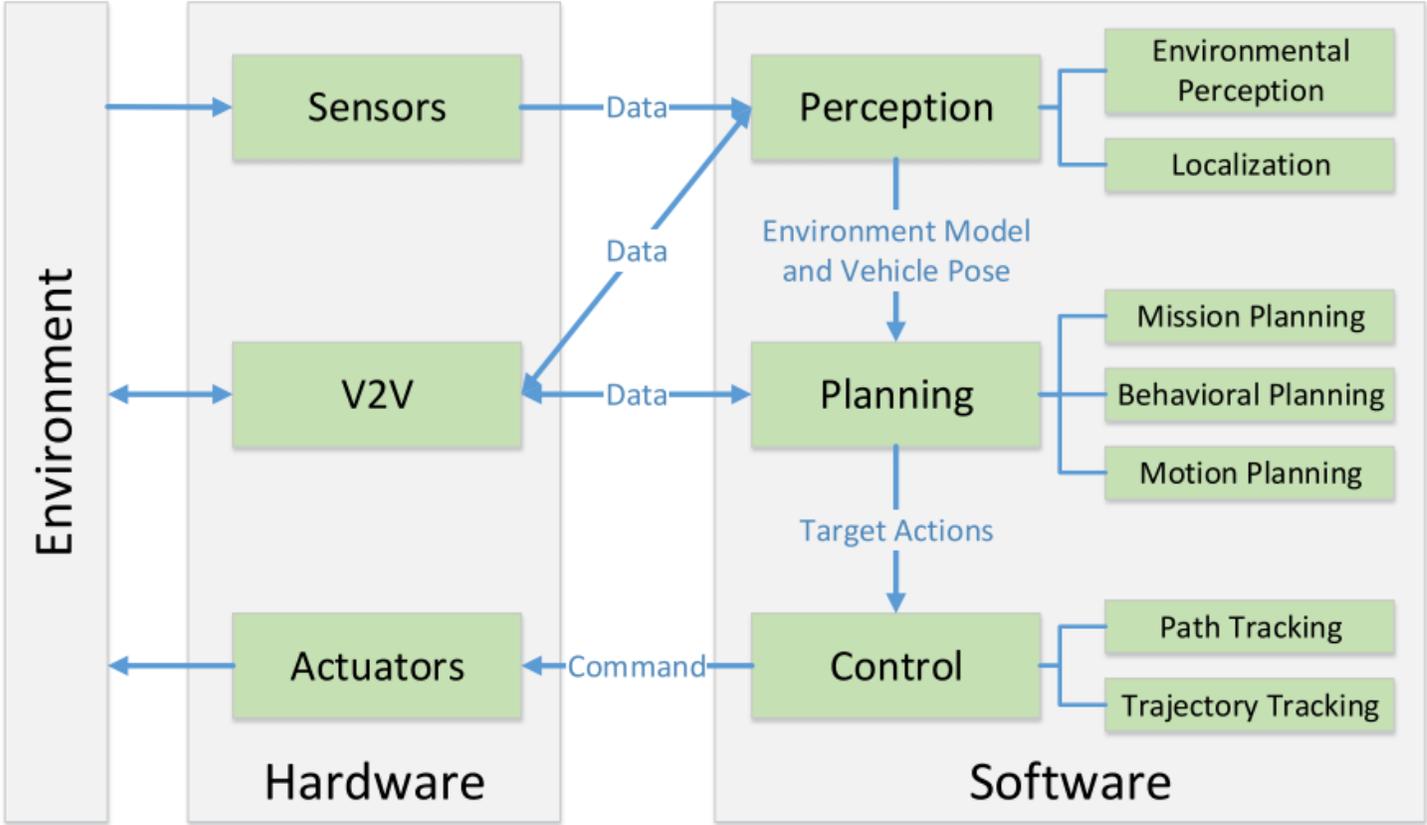


Figure 2. A typical autonomous vehicle system overview, highlighting core competencies.



Structure

★ Recap

⑩ **Perception**

⑩ Localization

⑩ State / Kinematics / Dynamics

⑩ Planning

★ Control

★ Traffic-Sim

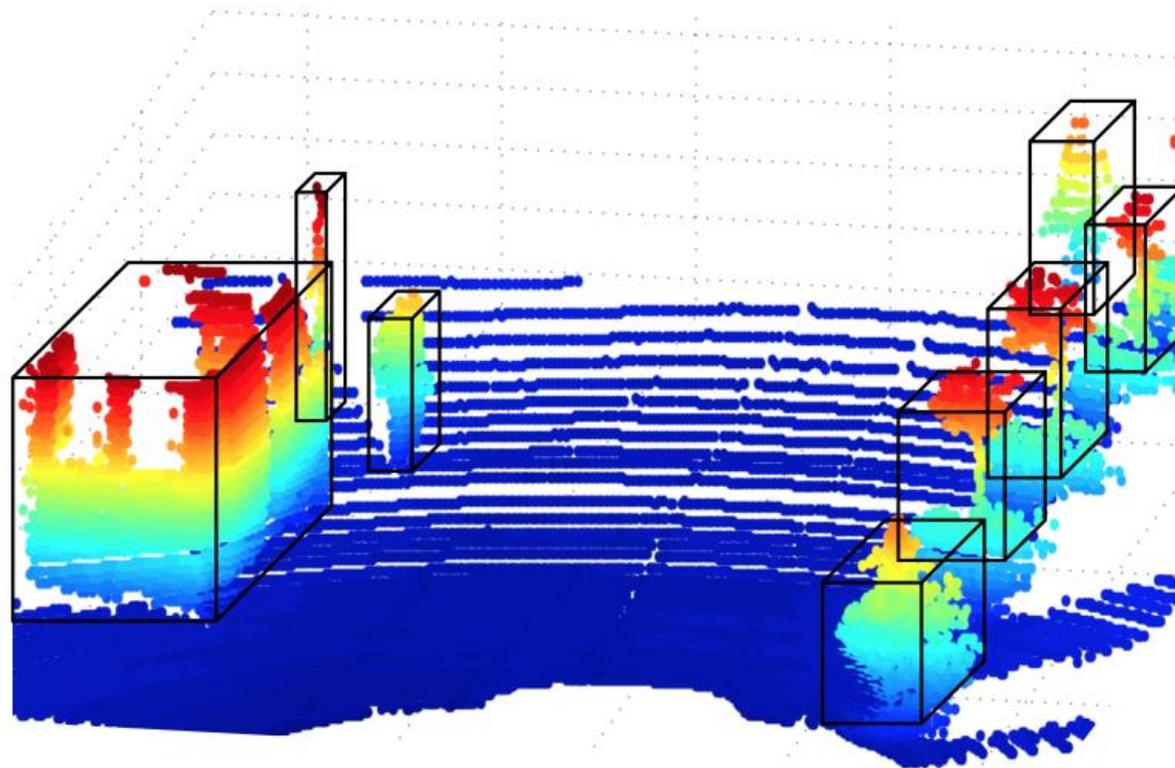
★ Prediction



Autonomous Driving: Perception using LIDAR

★ Light Detection and Ranging

- ⑩ Illuminate target using pulsed laser lights, and measure reflected pulses using a sensor



Autonomous Driving: Perception using LIDAR

★ LIDAR in practice

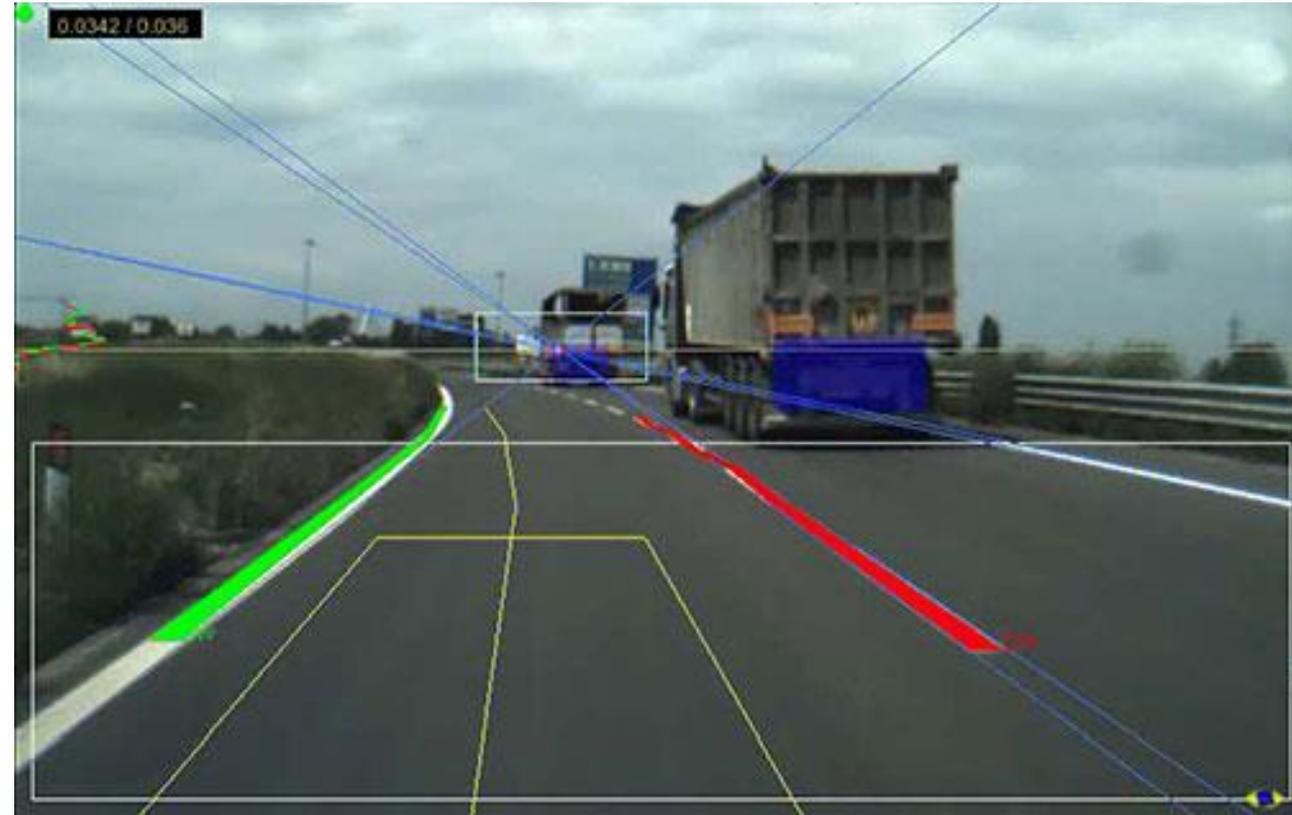
⑩ Velodyne 64HD lidar

★ https://www.youtube.com/watch?v=nXlqv_k4P8Q



Autonomous Driving: Perception using Cameras

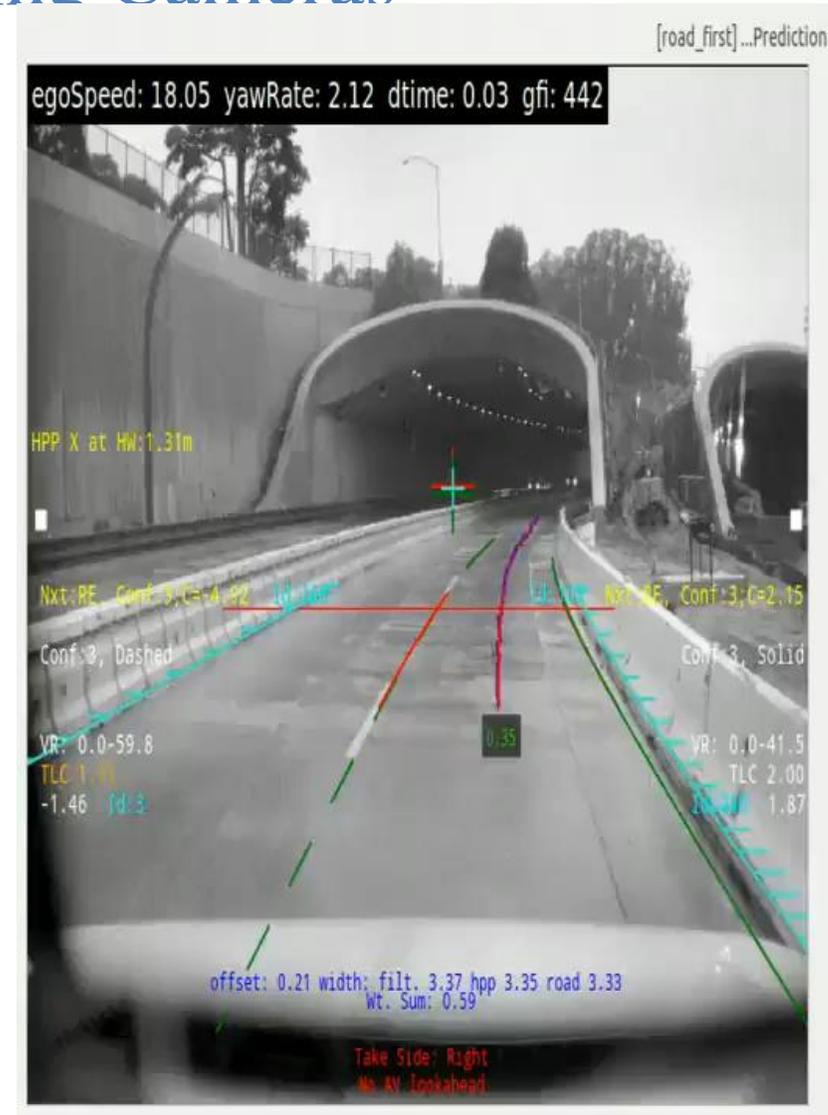
- ★ Camera based vision
 - ⑩ Road detection
 - ★ Lane marking detection
 - ★ Road surface detection
 - ⑩ On-road object detection



Autonomous Driving: Perception using Cameras

★ Sensing Challenges

- ⑩ Sensor Uncertainty
- ⑩ Sensor Configuration
- ⑩ Weather / Environment



Structure

★ Recap

- ⑩ Perception

- ⑩ **Localization**

- ⑩ State / Kinematics / Dynamics

- ⑩ Planning

★ Control

★ Traffic-Sim

★ Prediction



Autonomous Driving: Vehicle Localization

- ✦ Determining the pose of the ego vehicle and measuring its own motion
- ✦ Fusing data
 - ⑩ Satellite-based navigation system
 - ⑩ Inertial navigation system
- ✦ Map aided localization
 - ⑩ SLAM



Structure

★ Recap

⑩ Perception

⑩ Localization

⑩ **State / Kinematics / Dynamics**

⑩ Planning

★ Control

★ Traffic-Sim

★ Prediction



Autonomous Driving: State Space

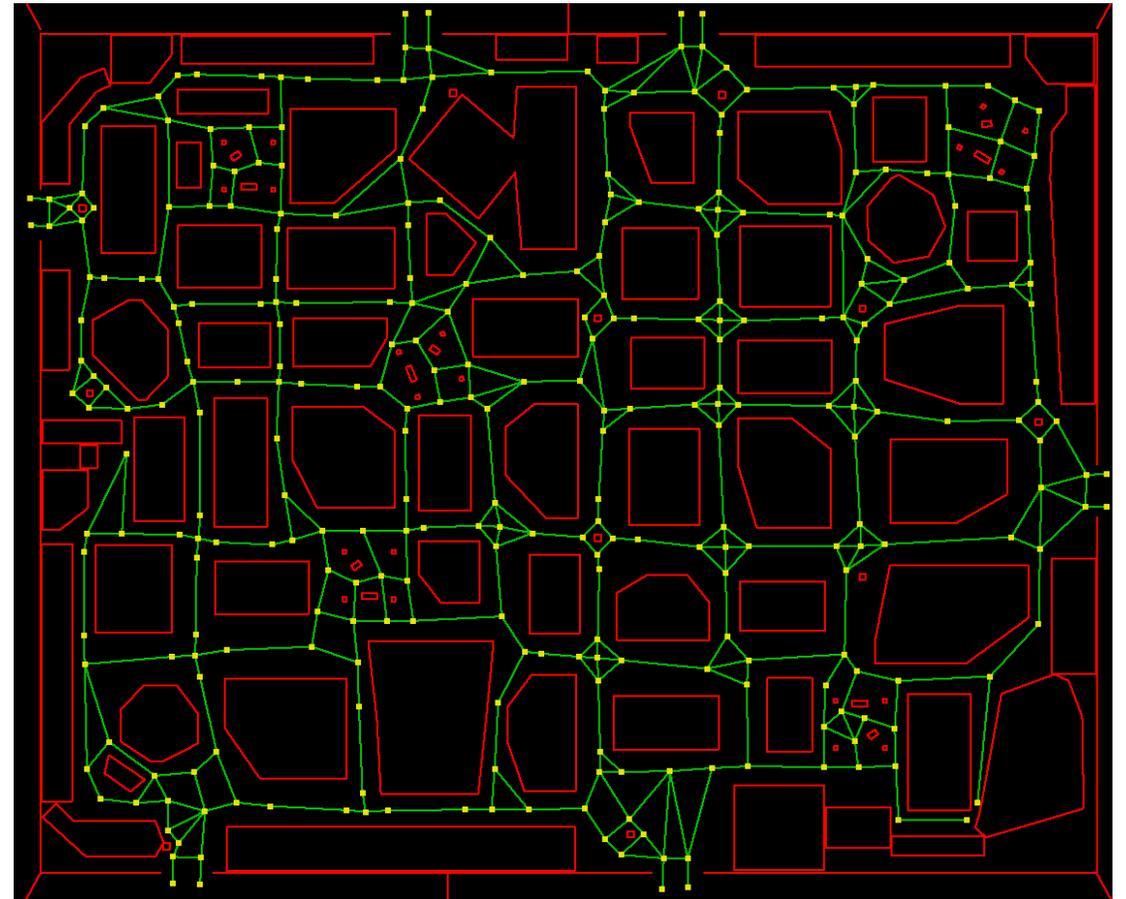
- ★ “The set of attribute values describing the condition of an autonomous vehicle at an instance in time and at a particular place during its motion is termed the ‘state’ of the vehicle at that moment”
- ★ Typically a vector with position, orientation, linear velocity, angular velocity
- ★ **State Space**: set of all states the vehicle could occupy



Autonomous Driving: State Space

★ Recall Pedestrian Planning:

- ⑩ Roadmap is essential a graph of potential agent states



Autonomous Driving: State Space

★ Examples:

⑩ 2D space with blinker booleans

★ $(\vec{p}, \theta, \vec{v}, \omega, bl_l, bl_r)$

⑩ State contains everything we need to describe the robot's current configuration!

⑩ Neglect some state variables when planning



Structure

- ★ Recap
- ★ State, Kinematics, and Dynamics Models
 - ⑩ State Space
 - ⑩ **Kinematic constraint models of the vehicle**
 - ⑩ Dynamic constraint models of the vehicle
- ★ Planning
- ★ AutonoVi-Sim



Autonomous Driving: Holonomicity

- ★ Cars are “non-holonomic” robots
 - ⑩ Typically 5 values describing physical
 - ★ (2 Cartesian coordinates, orientation, linear speed, angular speed)
 - ⑩ 2 “kinematic” constraints
 - ★ Can only move forward or backward, tangent to body direction
 - ★ Can only steer in bounded radius



Kinematic Constraints

★ Kinematics of Motion

- ⑩ “the branch of mechanics that deals with pure motion, without reference to the masses or forces involved in it”
- ⑩ Equations describing conversion between control and motion
- ⑩ Control: inputs to the system
 - ★ In vehicle: steering and throttle
 - ★ Also referred to as “Action” in literature



Autonomous Driving: Holonomicity

- ★ kinematic and dynamic constraints can be considered “rules” governing the state evolution function
- ★ For state $s_t \in S$, control input $u_t \in U$, time $t \in T$:
 - ⑩ $F(s_t, u_t, \Delta t) \rightarrow s_{t+1}$
- ★ Ex:
 - ⑩ A car cannot turn in place. No amount of steering will accomplish this
 - ⑩ A Roomba can turn in place



Kinematic Constraints

★ Kinematic models of a car

⑩ Single-track Bicycle (or simple car model)

★ 3-DOF configuration: (x, y, θ)

★ 2-DOF control: steering (ϕ) , speed (v)

★ Full state: $(x, y, \theta, v, \phi, L)$

⑩ Equations of motion:

$$\dot{p}_x = v * \cos(\theta) \quad \dot{p}_y = v * \sin(\theta)$$

$$\dot{\theta} = \frac{\tan(\phi)}{L}$$

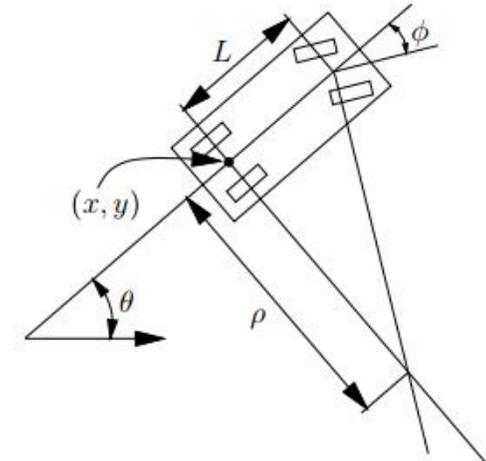
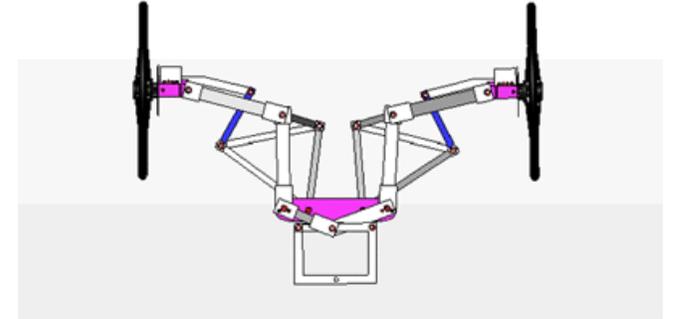


Figure 13.1: The simple car has three degrees of freedom, but the velocity space at any configuration is only two-dimensional.



Kinematic Constraints

- ★ Single-track bicycle example
 - ⑩ [github link to my project]

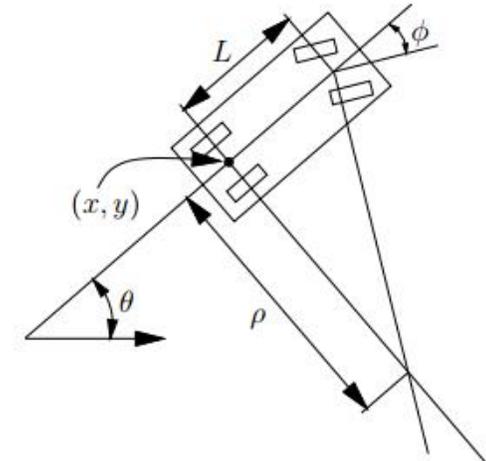
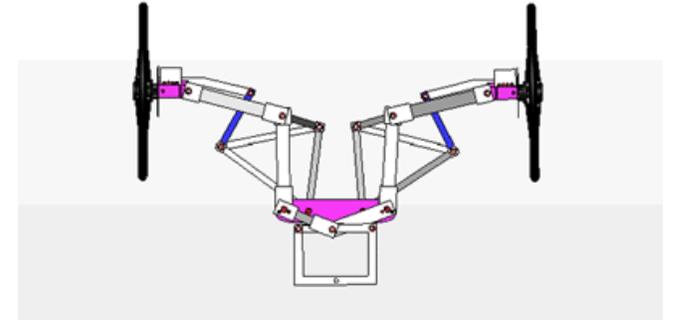


Figure 13.1: The simple car has three degrees of freedom, but the velocity space at any configuration is only two-dimensional.



Structure

- ★ Recap
- ★ State, Kinematics, and Dynamics Models
 - ⑩ State Space
 - ⑩ Kinematic constraint models of the vehicle
 - ⑩ **Dynamic constraint models of the vehicle**
- ★ Planning
- ★ AutoNoVi-Sim



Dynamic Constraints

- ★ “the branch of mechanics concerned with the motion of bodies under the action of forces.”
- ★ Tires subject to lateral and longitudinal force during steering / accelerating
 - ⑩ If lateral force exceeds friction force
 - ★ Fishtailing
 - ⑩ If longitudinal force exceeds friction force
 - ★ Peel out / skid



Dynamic Constraints

- ✦ No longer directly control acceleration and steering
 - ⑩ Apply engine force
 - ⑩ Apply steering force
- ✦ Diminishing returns on each force at limits of control



Dynamic Constraints

★ Dynamic Bicycle model with linear tires

- ⑩ No load transfer between tires
- ⑩ Larger state space including tire stiffness

- ★ F_x longitudinal force
- ★ F_y lateral force
- ★ m mass
- ★ I_z yaw moment of inertia

$$\begin{aligned}
 F_{xf} \cos \delta - F_{yf} \sin \delta + F_{xr} &= m(\dot{v}_x - v_y \dot{\psi}) \\
 F_{xf} \sin \delta + F_{yf} \cos \delta + F_{yr} &= m(\dot{v}_y + v_x \dot{\psi}) \\
 (F_{xf} \sin \delta + F_{yf} \cos \delta)b - F_{yr}c &= I_z \ddot{\psi} \\
 F_y &= C_\alpha \alpha
 \end{aligned}$$

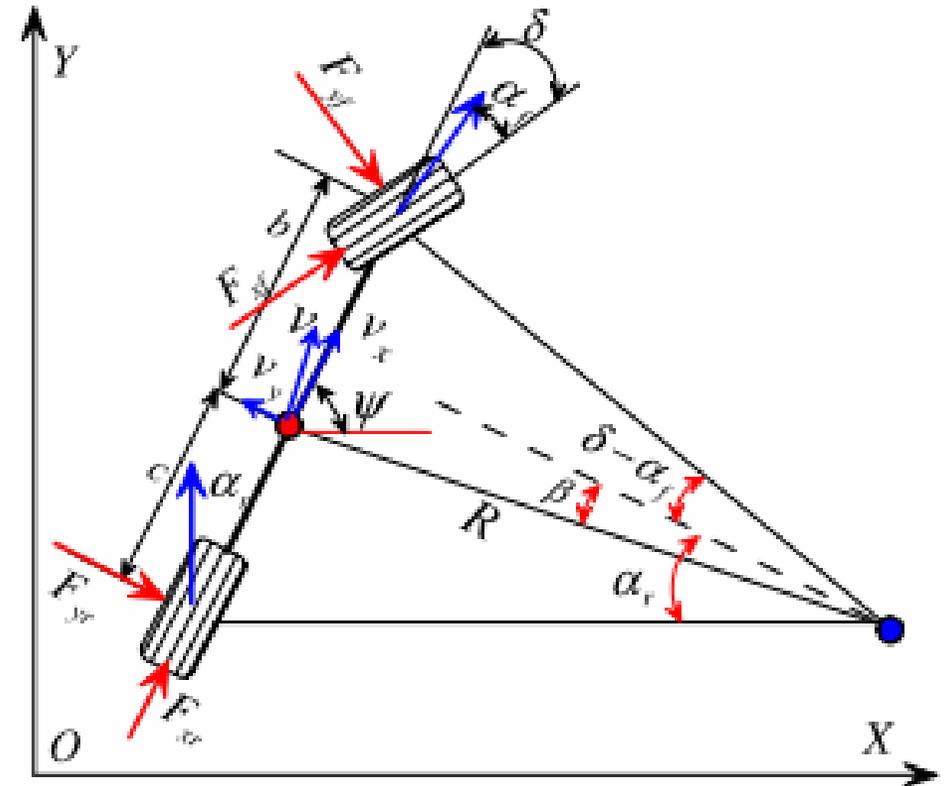
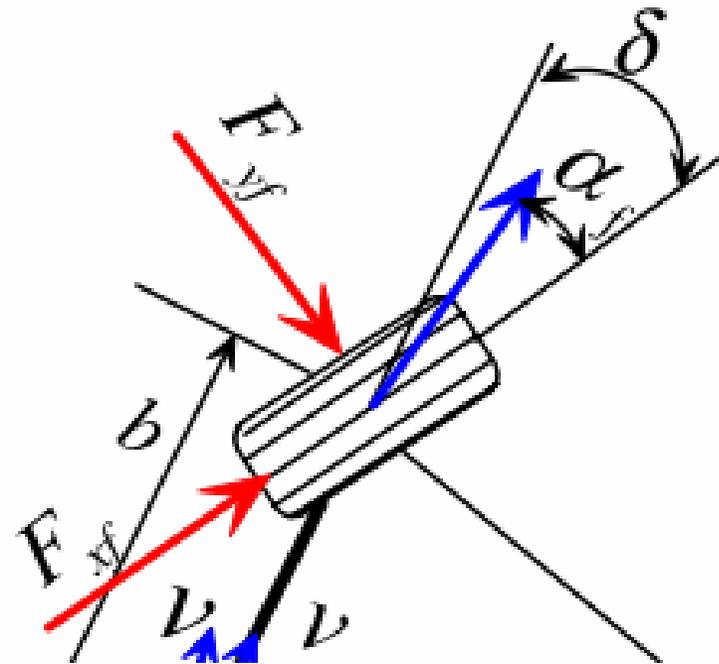


Fig. 1. Bicycle model of vehicle



Dynamic Constraints

- ★ Dynamic Bicycle model with linear tires
 - ⑩ F_y lateral force on tire
 - ⑩ F_x longitudinal force on tire
 - ⑩ α_f “slip angle” of tire
 - ⑩ δ steering angle



Dynamic Constraints

★ Models increase in complexity as needed for performance tuning

⑩ Aerodynamic drag force $F_{wind} = (C_w A_w v_t^2 g) / 16$

⑩ Maximum engine torque $\frac{F_{max}}{m} = 1 + \frac{3}{1 + e^{(\frac{v_t - 12}{4})}}$

★ Each layer of dynamics:

⑩ Increases accuracy of model

⑩ Increases computational complexity



Structure

★ Recap

⑩ Perception

⑩ Localization

⑩ State / Kinematics / Dynamics

⑩ **Planning**

★ Control

★ Traffic-Sim

★ Prediction



Autonomous Driving: Main Components

✦ Planning

- ⑩ Making purposeful decisions in order to achieve the robot's higher order goals

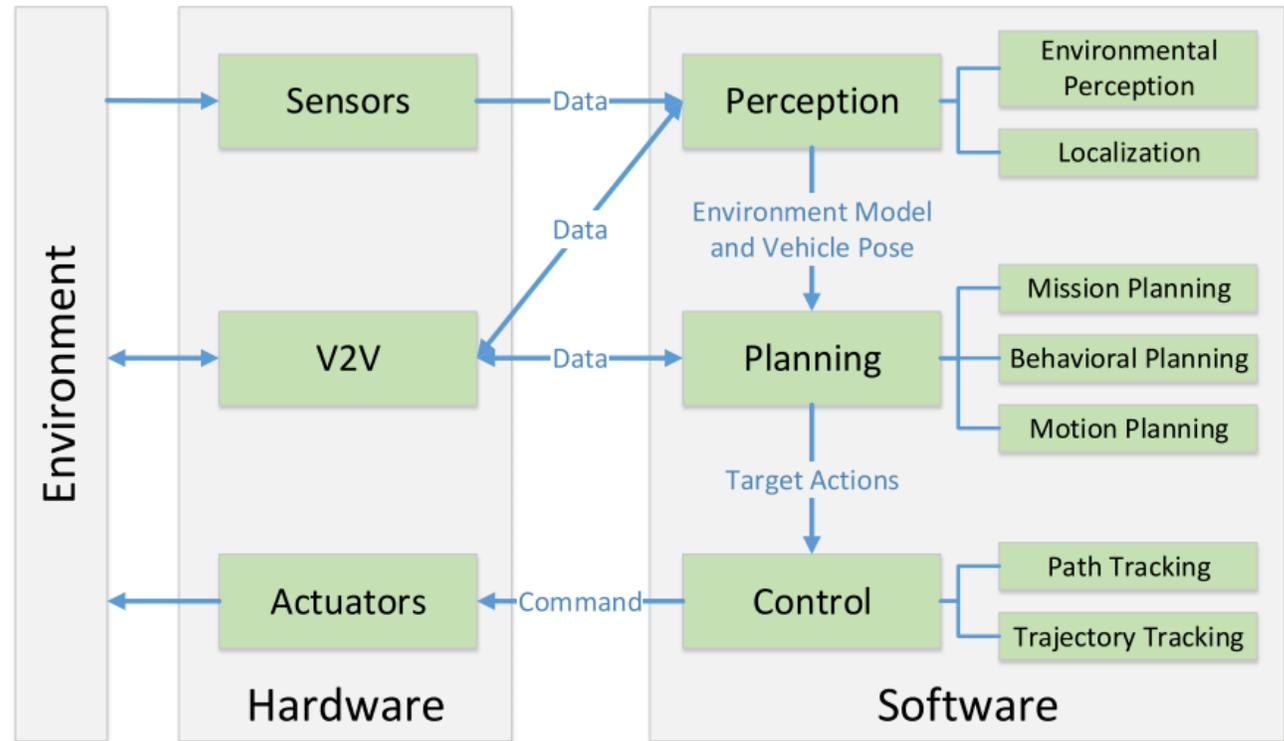


Figure 2. A typical autonomous vehicle system overview, highlighting core competencies.



Main Idea

- ★ **Motion Planning**: term used in robotics for the process of breaking down a desired movement task into discrete **motions** that satisfy movement constraints and possibly optimize some aspect of the movement



Autonomous Driving: Planning

★ Compare to Pedestrian Techniques:

- ⑩ Route Planning: road selection (global)
- ⑩ Path Planning: preferred lanes (global)
- ⑩ Maneuver-search: high level maneuvers (local)
- ⑩ Trajectory planning: Lowest level of planning (local)

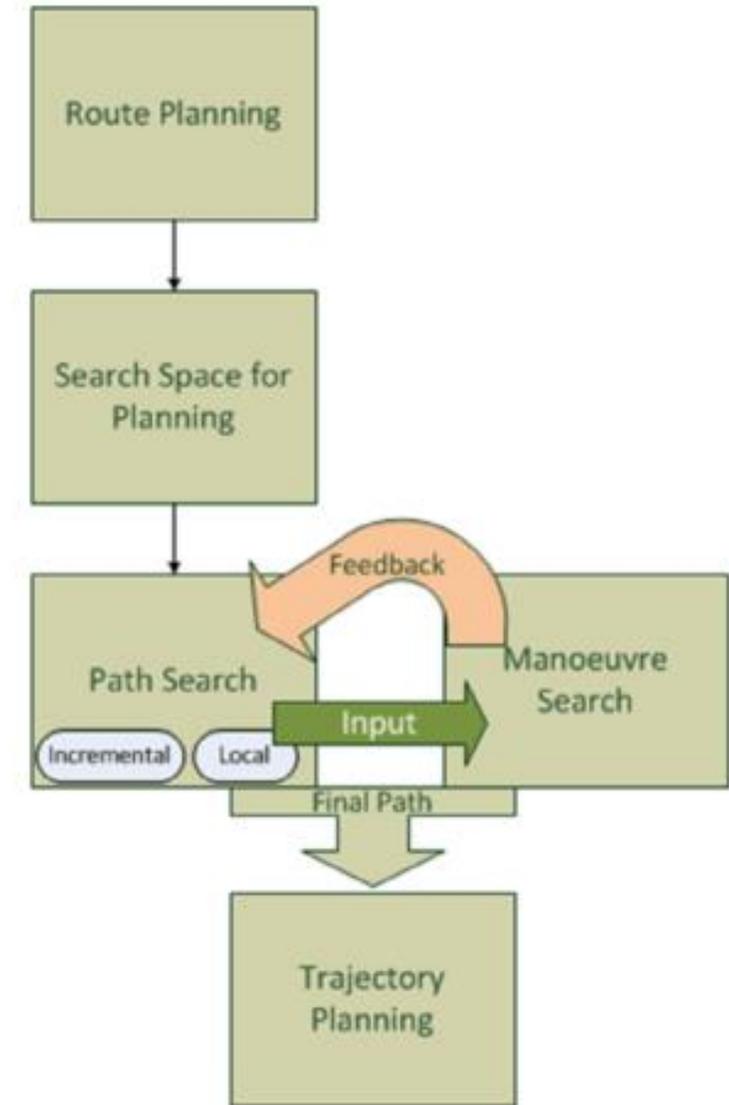


Fig. 2. A flow chart of planning modules.



Mission Planner (Route Planning)

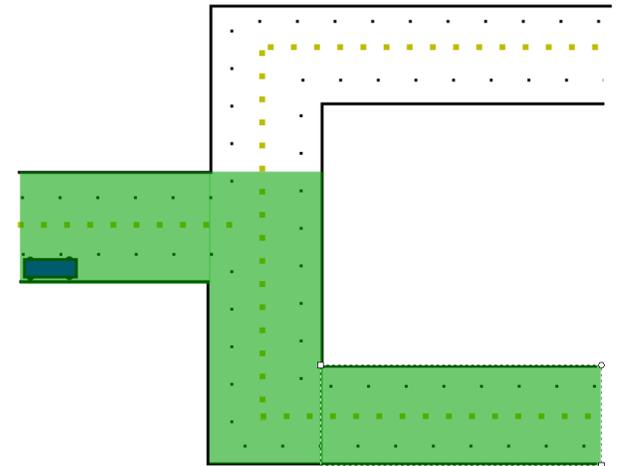
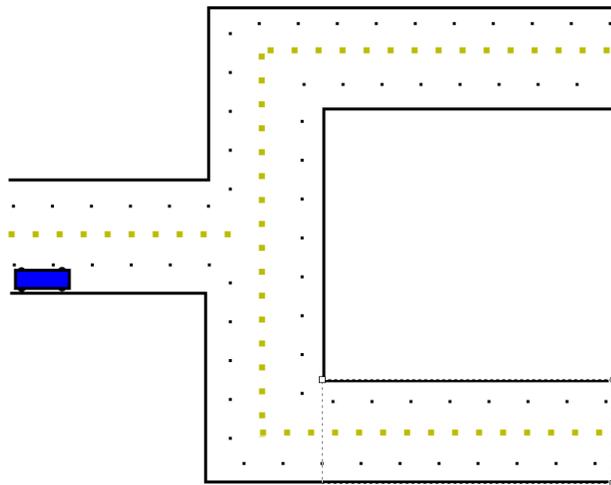
- ★ Pendleton: “considers high level objectives, such as assignment of pickup/dropoff tasks and which roads should be taken to achieve the task”
- ★ Typical approaches:

- ⑩ RNG (Road-network Graph)

- ★ A*

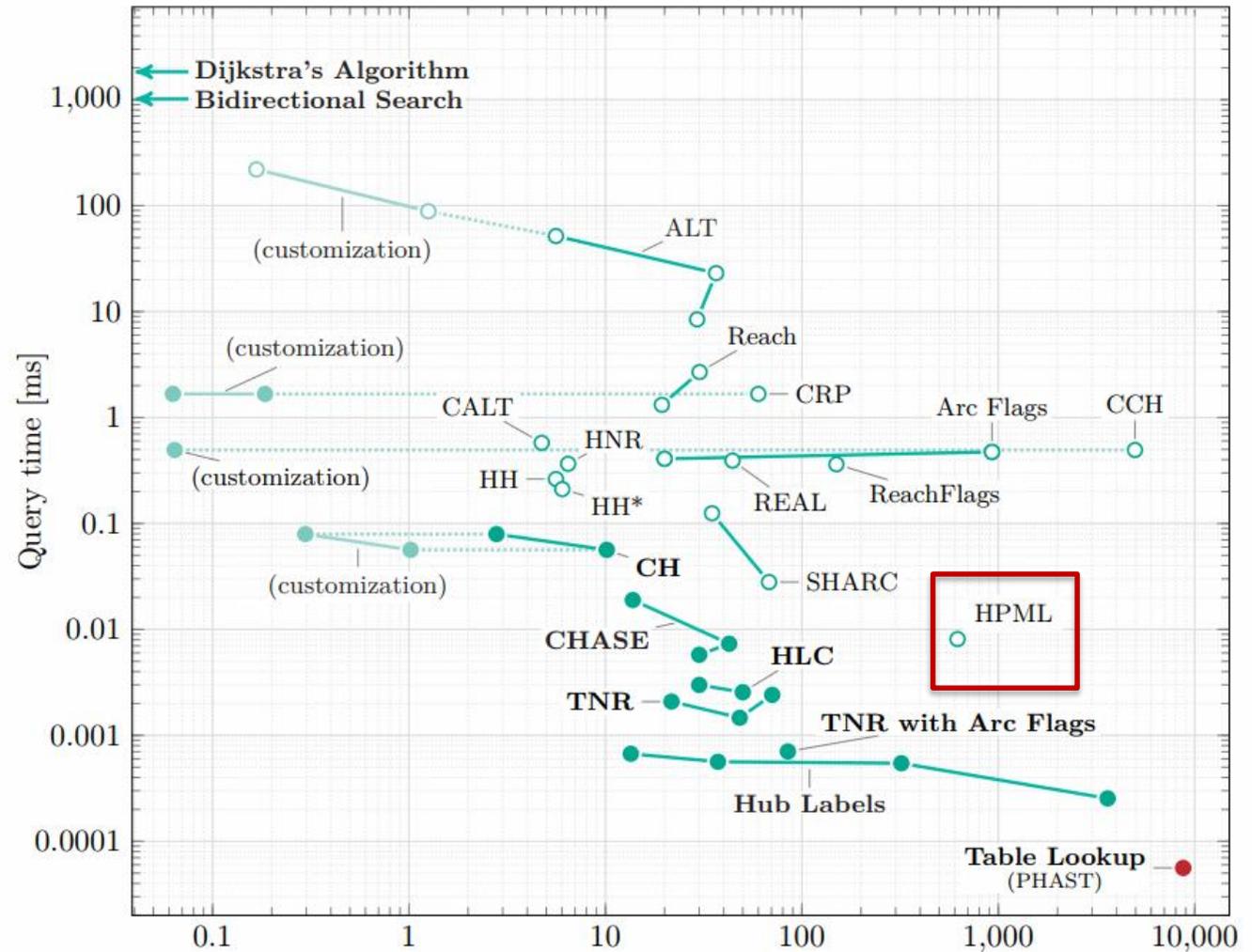
- ★ Dijkstras

- ⑩ Scale poorly!



Mission Planner (Route Planning)

- ★ Massive-scale algorithms needed for routing
- ★ 18 million vertices, 42.5 million edges
 - ⑩ Partial Western Europe dataset



Behavior Planner

★ Finite State Machines

- ⑩ Set of “states” and transition functions between them
- ⑩ Separate from configuration state

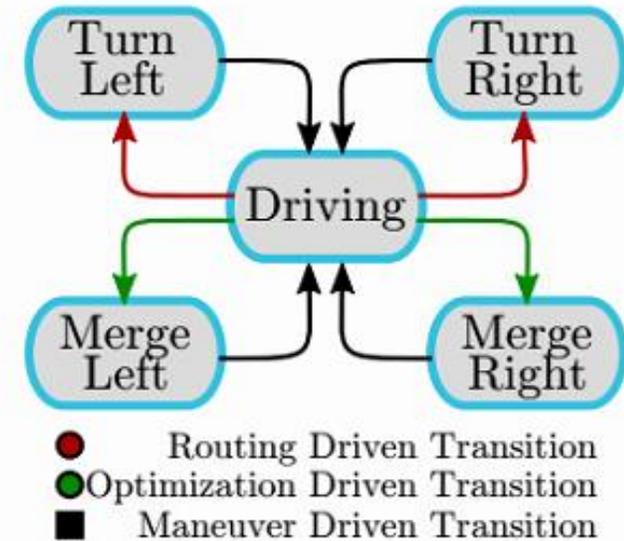
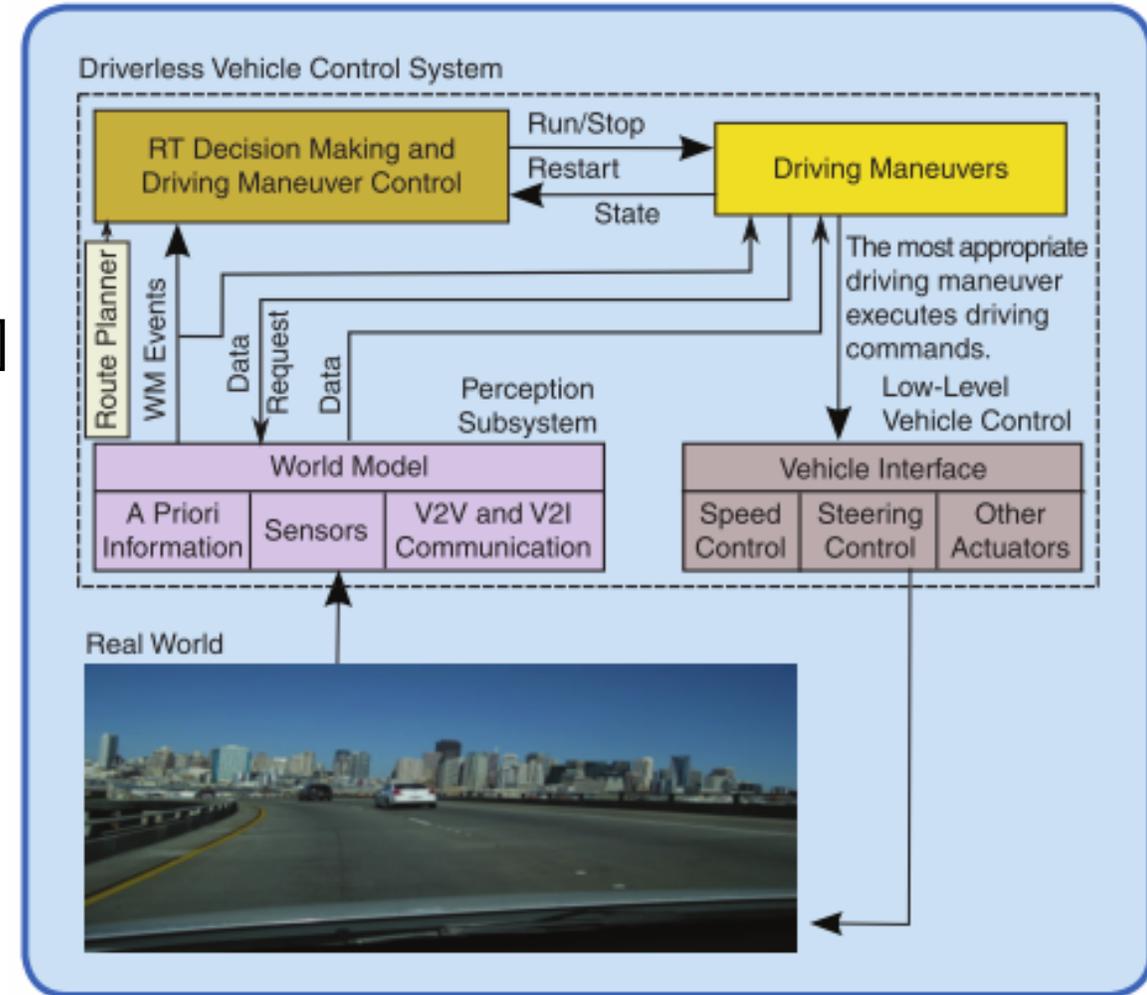
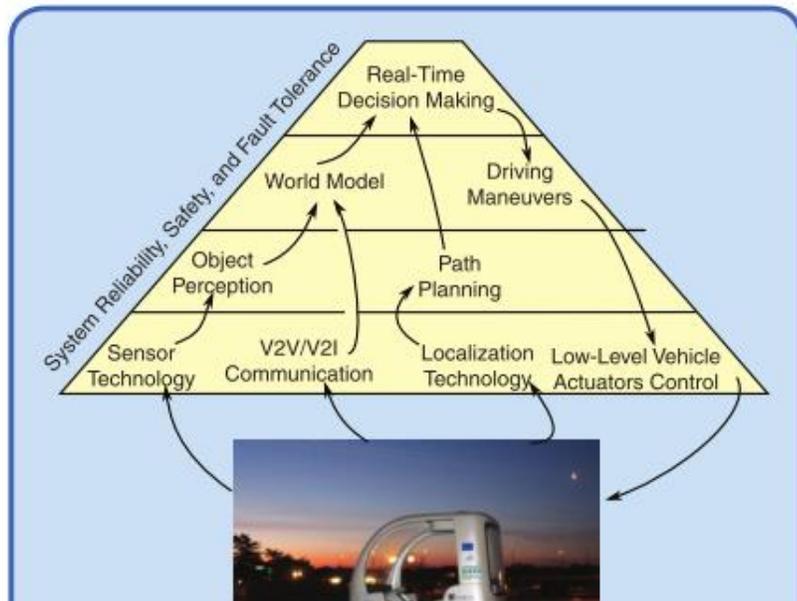


Fig. 2. **Finite State Machine:** We highlight different behavior states that are determined by the routing and optimization algorithms. When executing turns, the routing algorithm transitions the behavior state to a turning state. When the optimization-based maneuver algorithm plans a lane change, the behavior state is transitioned to merging.



Behavior Planner

- ◆ FSMs limited in some cases
 - ⑩ What to do in unseen situations?
- ◆ Real-time decision making [Furda et al 2011]



Motion Planner

★ Generally two stages:

- ⑩ Path planner - Computes the geometric representation of the path to be followed. I.e. the curve, spline, track, line, etc. we are following
- ⑩ Trajectory Planner / Path tracker - Computes the specific physical targets for following the path. I.e. velocity, acceleration, heading, steering, etc.



Motion Planner

★ Basic overview

- ⑩ **Complete planning** - continuous plan in configuration space
 - ★ Exponential in dimensions of c-space (curse of dimensionality)
 - ★ "Complete"
- ⑩ Combinatorial Planning - discrete planning over an exact decomposition of the configuration space
- ⑩ Sample-Based planning:



Motion Planner

★ Basic overview

⑩ Complete planning

⑩ **Combinatorial Planning** - discrete planning over an exact decomposition of the configuration space

★ Exponential in dimensions of c-space discretization (curse of dimensionality)

★ "resolution complete"

⑩ Sample-Based planning



Motion Planner

- ★ Basic overview

- ⑩ Complete planning

- ⑩ Combinatorial Planning

- ⑩ **Sample-Based planning** - Sample in space to find controls / positions which are collision free and linked

- ★ Probabilistically complete

- ⑩ Some “probabilistically optimal”

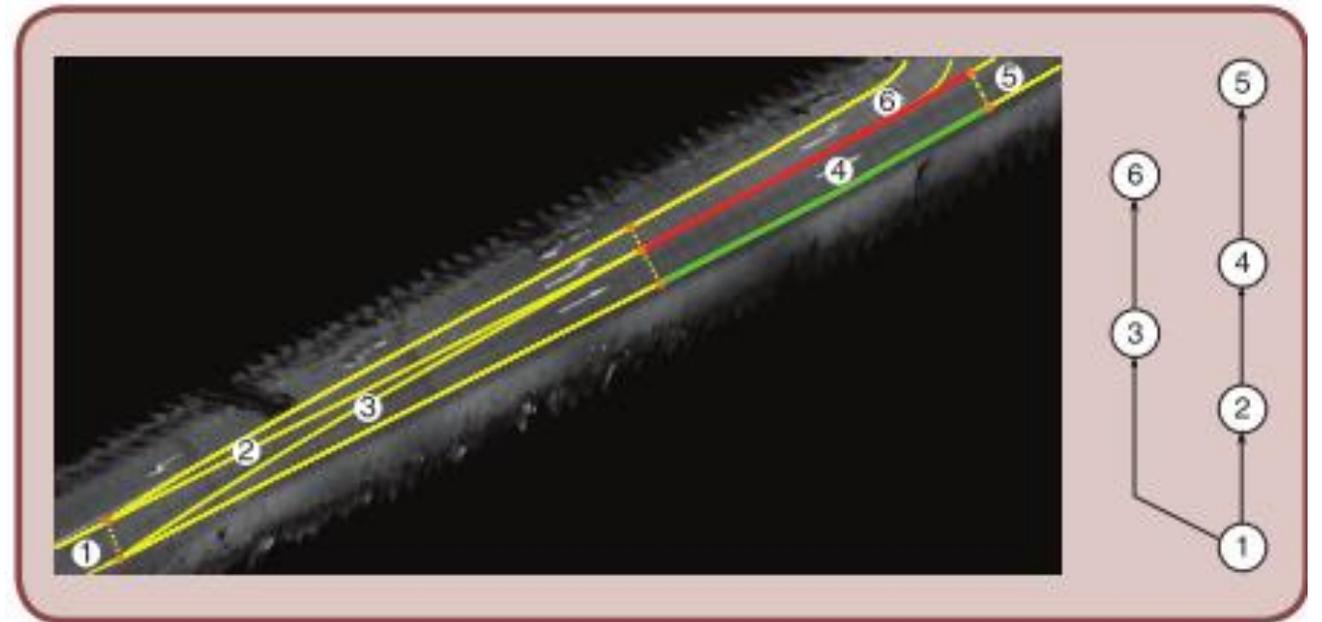
- ★ NOT exponential in configuration space



Motion Planner: Combinatorial Planners

★ Driving Corridors:

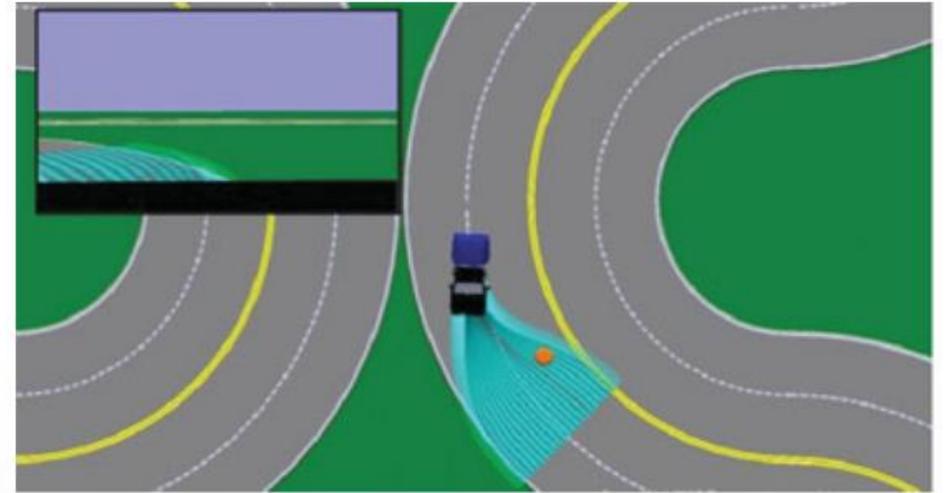
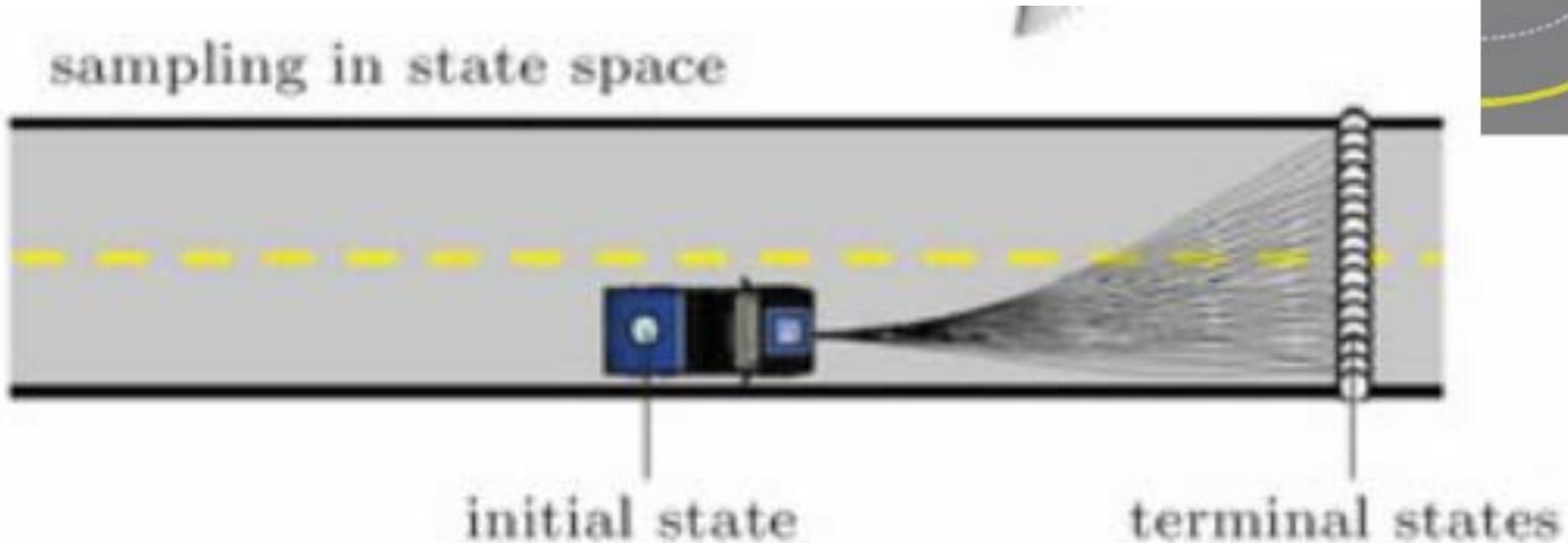
- ⑩ Decompose lanes into polygonal lanelets
- ⑩ Represent obstacles as polygonal bounding boxes or overlapping discs
- ⑩ Adjust lanelets to obstacle constraints



Motion Planner: Combinatorial Planners

★ Darpa Urban Challenge:

⑩ BOSS: kinodynamic reachable set



Maneuver Planner: Sample-based Planners

- ★ Sample-based Planning specifically for cars:
 - ⑩ Dynamics computation
 - ⑩ Inevitable collision states
 - ⑩ “Space-time planning approaches”
- ★ Pendleton: “Incorporating differential constraints into state-sampling planners is still a challenging matter, and requires a steering function to draw an optimal path between two given states which obeys control constraints (if such a path exists), as well as efficient querying methods to tell whether a sampled state is reachable from a potential parent state”



Maneuver Planner: Sample-based Planners

★ RRT:

⑩ Given at-least one initial configuration in free-space and a goal configuration

- ★ Sample a point p in configuration space, determine if it is collision free
- ★ If so, find nearest node n to the point, move some δ towards the point
- ★ If n to $n + \delta$ is CLEAR, connect to the tree



Maneuver Planner: Sample-based Planners

★ State-lattice planners

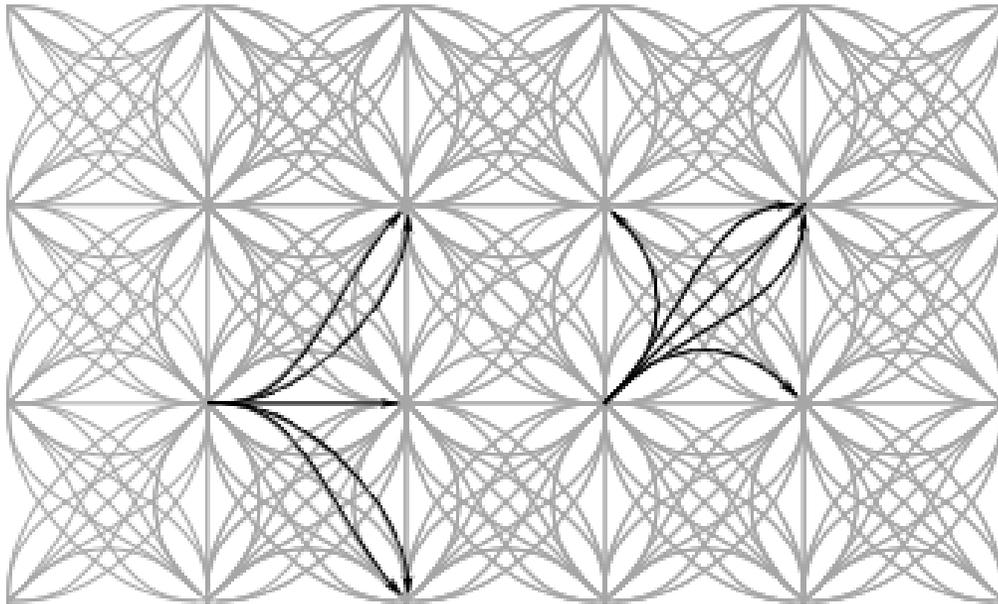
- ⑩ Generate set of potential future states through solving boundary-value problem
- ⑩ Generate connected “lattice” of potential future states expanding in time and space



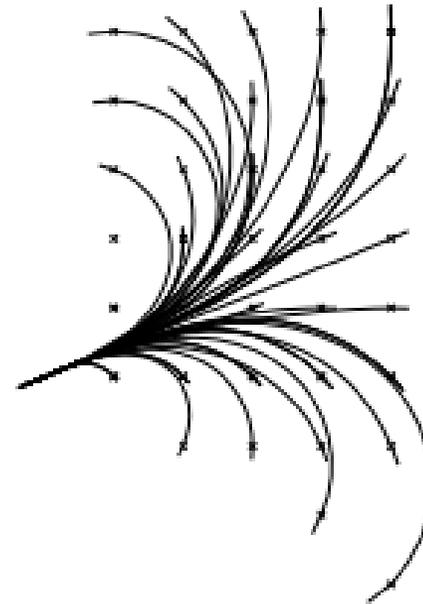
Maneuver Planner: Sample-based Planners

★ State-lattice planners

⑩ Ex: Configurations in space



(a)



(b)

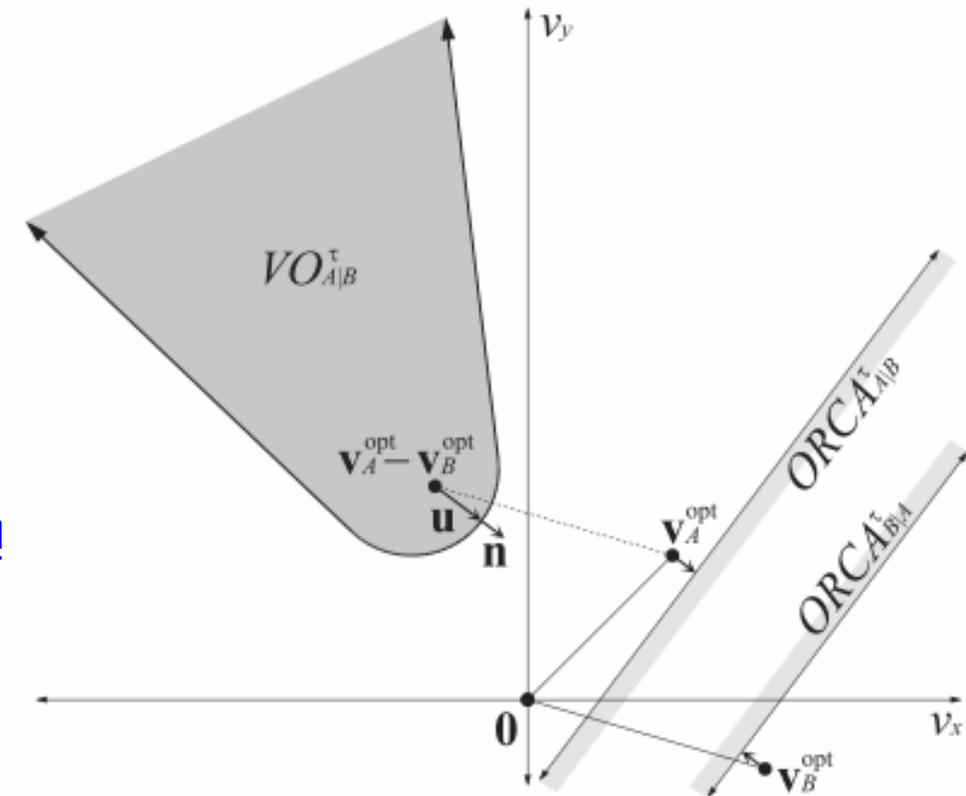


Maneuver Planner: Obstacle Representation

★ RVOs: Reciprocal-velocity Obstacles

⑩ Constructs mutually exclusive velocity set choices for multiple robots

⑩ <https://youtu.be/1Fn3Mz6f5xA?t=1n24s>



Structure

- ★ Recap
- ★ Control
 - ⑩ **Core concepts**
 - ⑩ PID
 - ⑩ MPC
- ★ Traffic-Sim
- ★ Prediction



Autonomous Driving: Main Components

✦ Control

- ⑩ Executing the planned maneuvers accounting for error / uncertainty
- ⑩ Commands sent to actuators

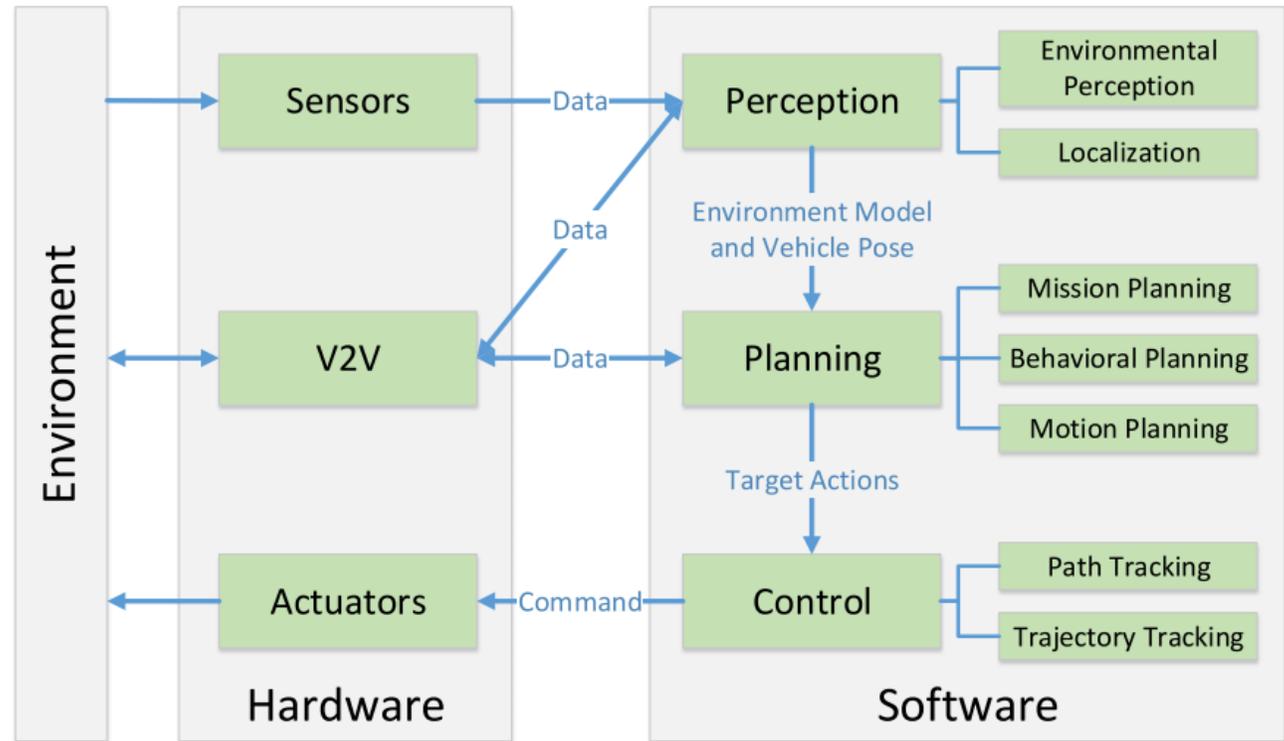


Figure 2. A typical autonomous vehicle system overview, highlighting core competencies.



Control: Core Concepts

- ★ **Automatic control** in engineering and technology is a wide generic term covering the application of mechanisms to the operation and regulation of processes without continuous direct human intervention
 - ⑩ Open-loop control: Control input delivered independent of measurements
 - ⑩ Closed-loop control: Control input determined by system outputs



Control: Core Concepts

★ Open-loop control examples

⑩ Timers:

- ★ Electronic timing switches
- ★ Clothes Dryer

⑩ Simple throttle (non-electronic)

- ★ Motorbikes, go-karts
- ★ Stove-top gas

⑩ Sinks / simple valves

- ★ Hot water / cold water



Control: Core Concepts

★ Closed-loop control examples

⑩ Thermostat:

- ★ Engages air-conditioning depending on temperature

⑩ Oven:

- ★ Heating element controlled by temperature

⑩ Cruise-control:

- ★ Throttle controlled by current speed / acceleration

⑩ Used EXTENSIVELY in plant control (i.e. chemical, energy)



Control: Core Concepts

- ✦ Process Variable (PV): The system output we wish to control
- ✦ Set Point (SP): Target value of the process Variable
- ✦ Control Output (CO): Output of the controller (input to the system)
- ✦ Error (E): Difference between SP and PV

<https://www.dataforth.com/introduction-to-pid-control.aspx>



Control: Core Concepts

- ◆ Example: Water Plant Thermal Control
 - ⑩ Water kept at constant temperature by gas heater
 - ⑩ If level rises, gas reduced to stabilize
- ◆ PV: Temperature of water
- ◆ SP: Desired Temperature
- ◆ CO: Level of gas applied to burner

<https://www.dataforth.com/introduction-to-pid-control.aspx>

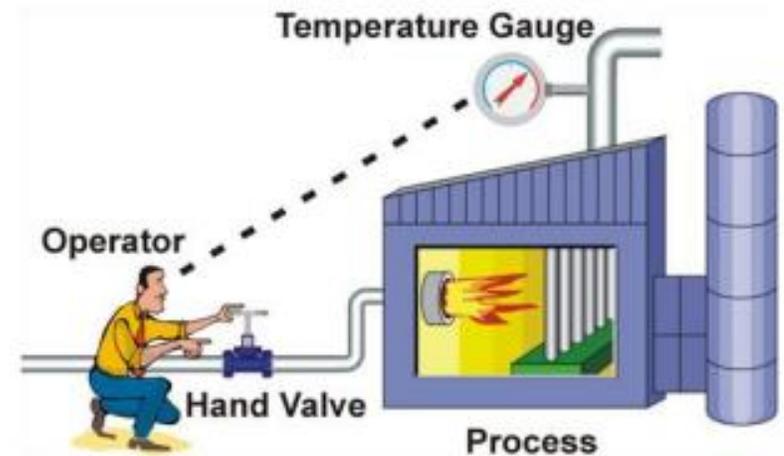


Figure 1
An Operator Performing Manual Control



Control: Core Concepts

◆ Can we replace the manual control with automatic controller?

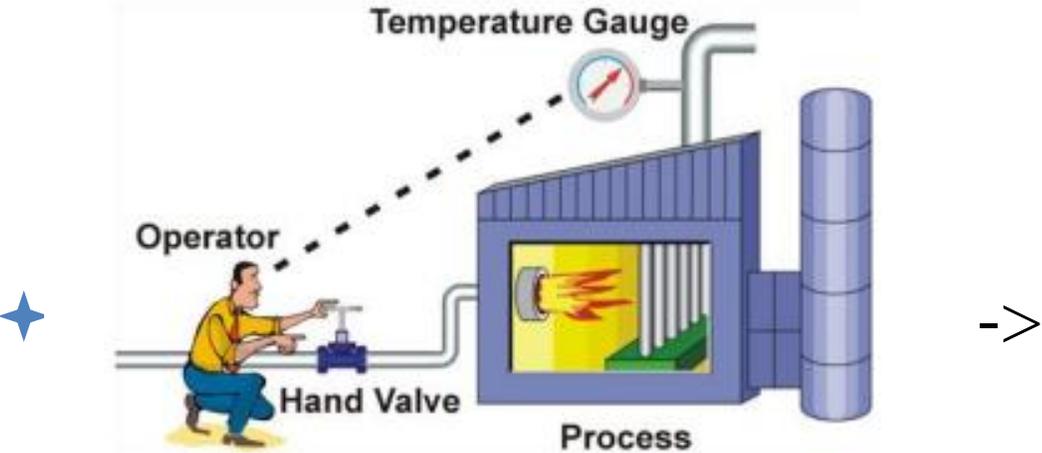


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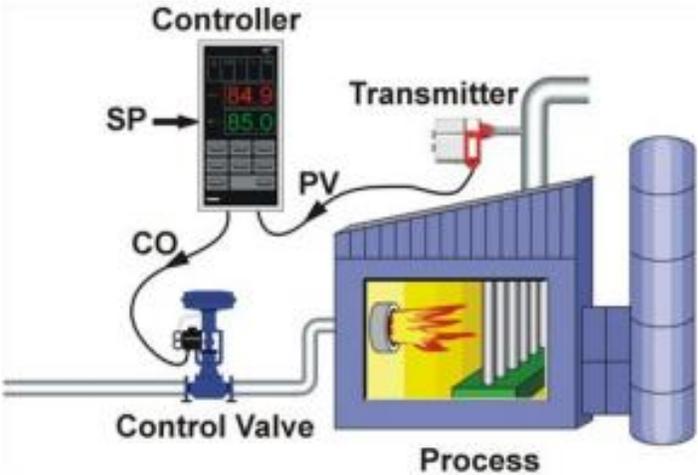


Figure 2
A PID Controller Performing Automatic Control

◆ Of course, we can!



Structure

- ★ Recap
- ★ Control
 - ⑩ Core concepts
 - ⑩ **PID**
 - ⑩ MPC
 - ⑩ Path Tracking
- ★ Traffic-Sim
- ★ Prediction



Control: PID

- ★ **Proportional-Integral-Derivative** Controller: control loop feedback mechanism widely used in industrial control systems and a variety of other applications requiring continuously modulated control.
 - ⑩ Continuously calculates E, applies correction based on proportional, integral, and derivative terms (denoted P, I, and D respectively)
 - ⑩ Proportion (P): Current error, E (typically $SP - PV$)
 - ⑩ Integral (I): integral of E (sum of errors over time)
 - ⑩ Derivative (D): derivative of E (typically finite difference)



Control: PID

- ★ **Proportional-Integral-Derivative** Controller: control loop feedback mechanism widely used in industrial control systems and a variety of other applications requiring continuously modulated control.

$$u(t) = K_p e(t) + K_i \int_0^t e(\tau) d\tau + K_d \frac{de(t)}{dt}$$



Control: PID

- ✦ Proportion: Output controlled by error and Controller Gain (K_p)
- ✦ Control output proportional to error
 - ⑩ Choice of error function, but typically $SP - PV$
- ✦ High gain: can cause oscillation
- ✦ Low gain: fails to correct to Set Point

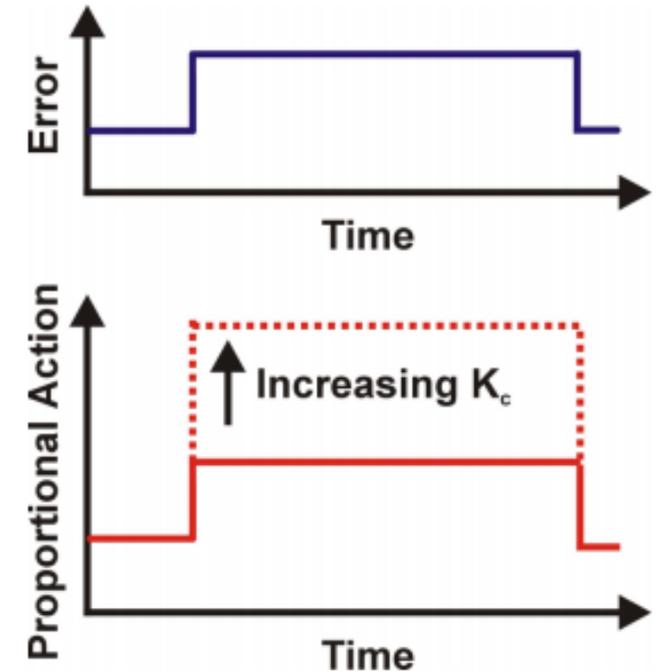


Figure 3
Proportional Control Action



Control: PID

- ★ Proportion-only controller: Output controlled by error and Controller Gain (K_p)
- ★ Control output proportional to error
 - ⑩ Choice of error function, but typically $SP - PV$
- ★ Add bias point for steady output at 0 error

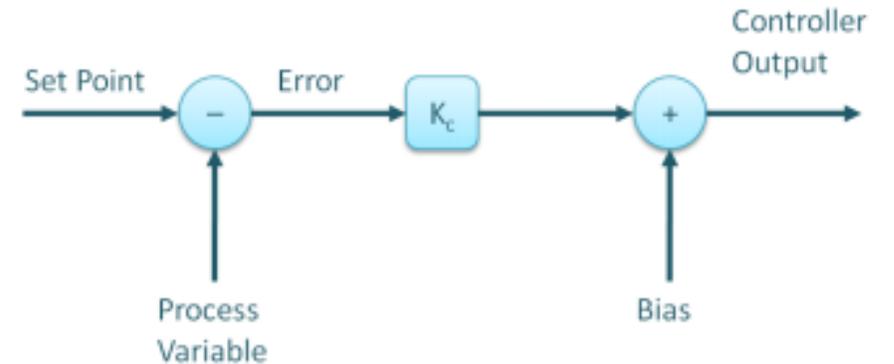


Figure 4
A Proportional-Only Controller Algorithm



Control: PID

- ◆ P-only controller

 - ⑩ Bias controls steady output

- ◆ <https://sites.google.com/site/fpgaandco/pid>

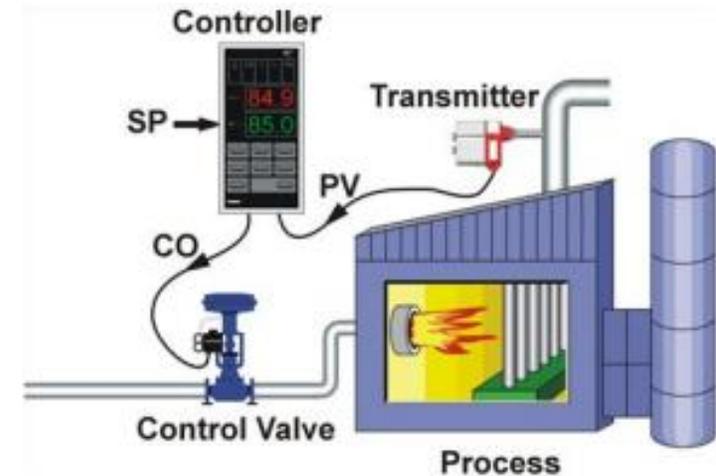


Figure 2
A PID Controller Performing Automatic Control



Control: PID

- ✦ Integral Control: Output term controlled by integral of error and Integral Gain (K_i)
- ✦ Corrects “steady-state” error
- ✦ Requires a “time” factor for integration (T_i)
- ✦ Longer time = less integral action

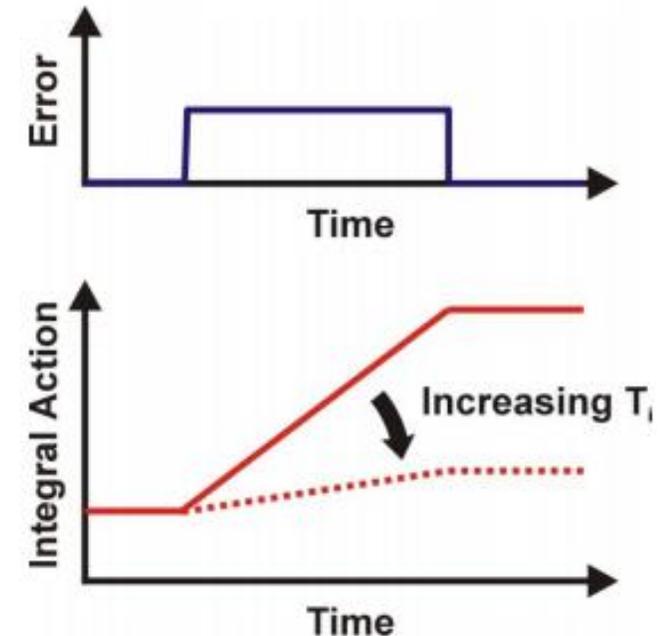


Figure 7
Integral Control Action



Control: PID

- ✦ PI Controller: Proportion and integral terms
- ✦ Corrects steady-state error, converges rather than oscillates

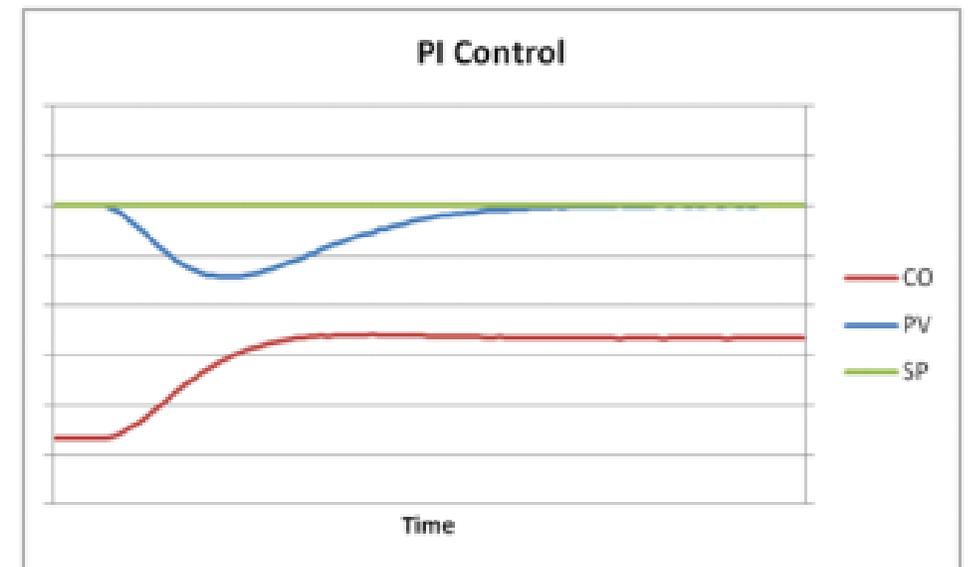


Figure 9
A PI Controller's Response to a Disturbance



Control: PID

- ◆ Derivative: Output term controlled by derivative of error and Derivative Gain (K_d)
- ◆ Assists in rapid response to disturbance
- ◆ Requires time parameter to operate

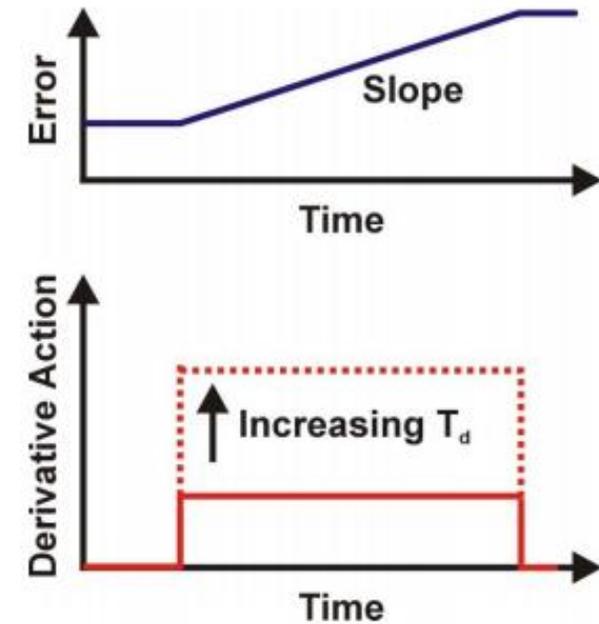


Figure 10
Derivative Control Action



Control: PID

- ★ PID Controller: Proportion, Integral, Derivative terms
- ★ Complete closed-loop controller
 - ⑩ Used in AutoVi and countless applications

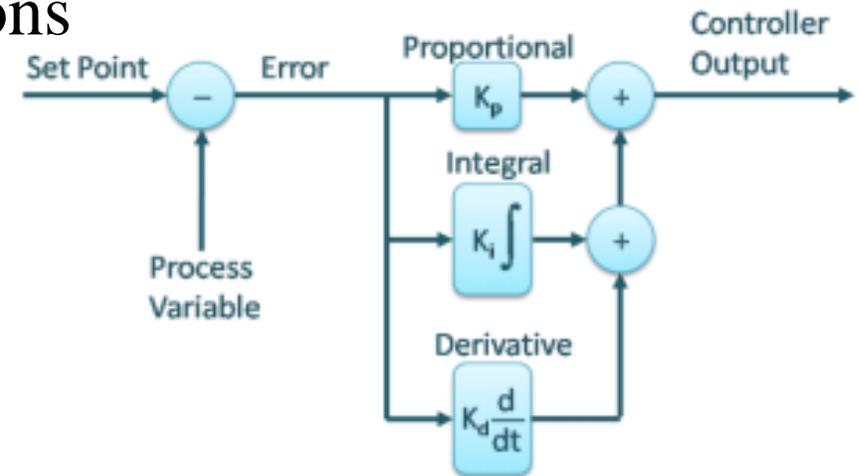


Figure 12
The Parallel PID Controller Algorithm



Control: PID Tuning

★ Rules of thumb for tuning a PID controller:

★ https://upload.wikimedia.org/wikipedia/commons/3/33/PID_Compensation_Animated.gif

Effects of increasing a parameter independently^{[20][21]}

Parameter	Rise time	Overshoot	Settling time	Steady-state error	Stability
K_p	Decrease	Increase	Small change	Decrease	Degrade
K_i	Decrease	Increase	Increase	Eliminate	Degrade
K_d	Minor change	Decrease	Decrease	No effect in theory	Improve if K_d small



Control: PID Tuning

★ Ziegler–Nichols Tuning

⑩ Tune K_p until the control loop begins to oscillate

★ Called Ultimate control point (K_u)

⑩ K_u and oscillation period T_u used to tune parameters as follows

Ziegler–Nichols method

Control Type	K_p	K_i	K_d
<i>P</i>	$0.50K_u$	—	—
<i>PI</i>	$0.45K_u$	$0.54K_u/T_u$	—
<i>PID</i>	$0.60K_u$	$1.2K_u/T_u$	$3K_uT_u/40$



Control: PID Examples

★ More examples of PID:

- ⑩ Cruise-control

- ⑩ Quad-rotor Autopilot

- ⑩ Mobile robot control

 - ★ PID for steering + PID for speed

- ⑩ Spaceships

- ⑩ ...

- ⑩ ...

- ⑩ Innumerable examples of PID control



Control: PID Examples

★ PID for QuadRotor

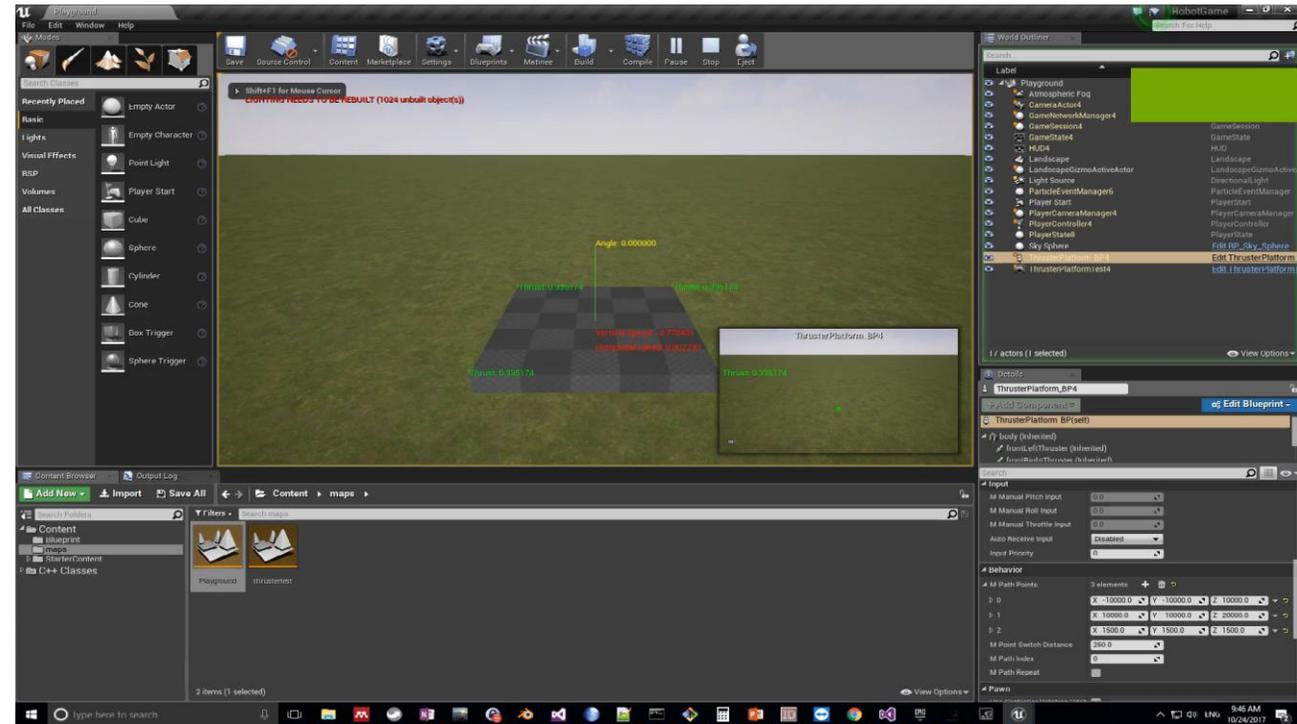
⑩ Pure pursuit

⑩ Target speed specified

⑩ 2 layer PID

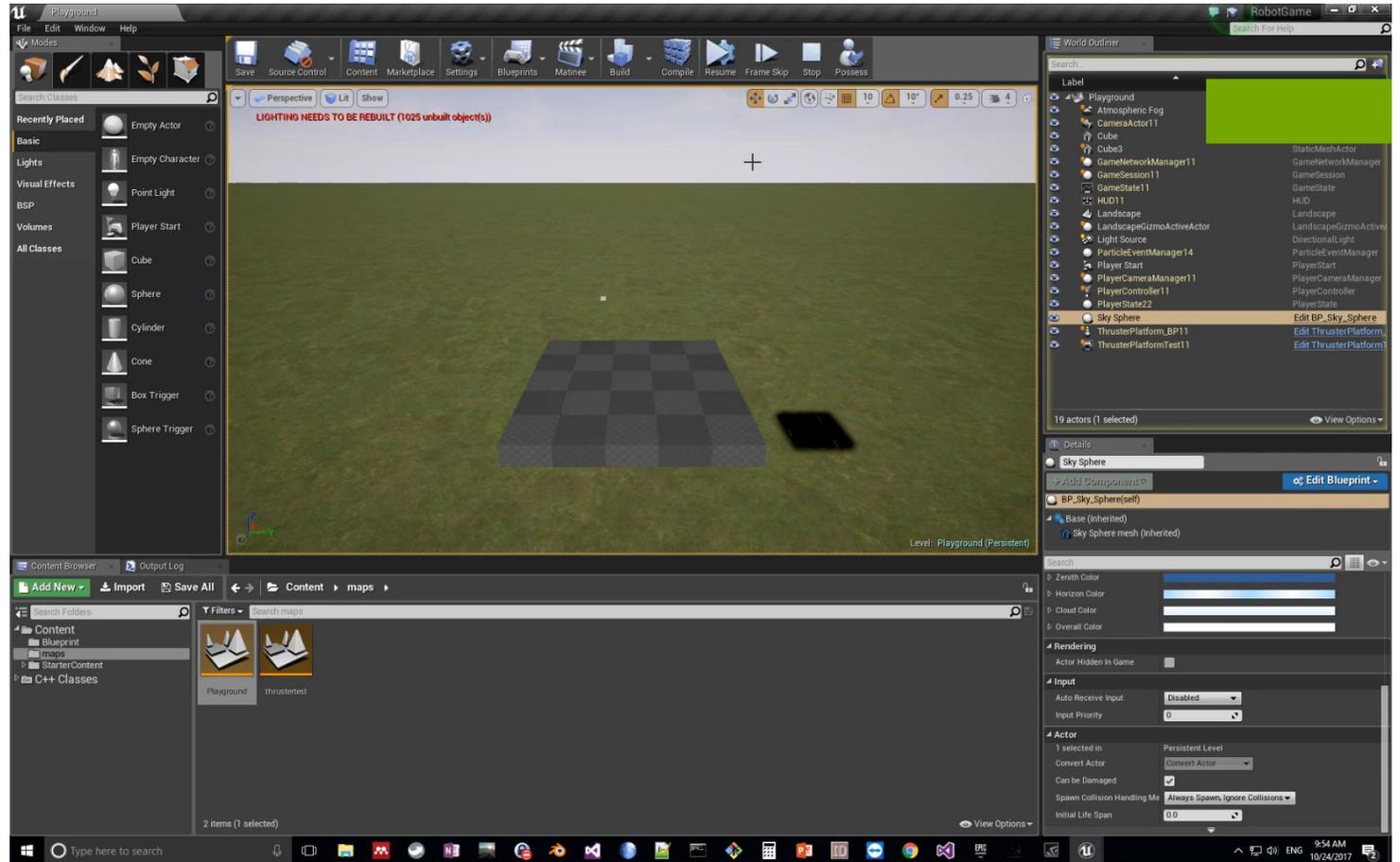
★ 1. Mix rotors for vertical speed

★ 2. Mix rotors for horizontal speed



Control: PID Examples

- ★ PID for QuadRotor
- ⑩ Robust to perturbation



Structure

- ★ Recap
- ★ Control
 - ⑩ Core concepts
 - ⑩ PID
 - ⑩ **MPC**
 - ⑩ Path Tracing
- ★ Traffic-Sim
- ★ Prediction



Control: MPC

- ★ **Model-Predictive** Controller: control loop relying on an underlying system model to generate feed-forward control
 - ⑩ Augment feedback control system to generate predicted future values and predicted control outputs
 - ⑩ Non-linear systems typically linearized over small timescales of MPC
 - ⑩ <https://www.youtube.com/watch?v=oMUtYZOgsng>
 - ★ Very good introduction
 - ⑩ <https://www.youtube.com/watch?v=DFqOf5wbQtc>
 - ★ Lecture series is helpful for MPC



Control: MPC

- ★ MPC is very useful when process model is available
 - ⑩ Reduces overshoot substantially
 - ⑩ Using cached table of input responses, optimization can be done quickly
- ★ MPC uses in automotive context:
 - ⑩ Traction control [Borelli 2006]
 - ⑩ Braking control [Falcone 2007]
 - ⑩ Steering [Falcone 2007]
 - ⑩ Lane-keeping [Liu 2015]



Structure

- ★ Recap
- ★ Control
 - ⑩ Core concepts
 - ⑩ PID
 - ⑩ MPC
 - ⑩ **Path Tracking**
- ★ Traffic-Sim
- ★ Prediction



Control: Path tracking with controllers

- ★ Given a path computed by the motion planner, we use controls to follow or “achieve” the path
- ★ Many methods for path tracking:
 - ⑩ Pure-pursuit
 - ⑩ AutonoVi (Arcs)
 - ⑩ Kinematic Bicycle
 - ⑩ Model-Predictive Control



Control: Path tracking with controllers

★ Pure-pursuit

⑩ Given a geometric path, track a point ahead of the vehicle according to a fixed lookahead (can be a function of speed)

⑩ <https://www.youtube.com/watch?v=qG70QJJ8Qz8>

⑩ <https://www.youtube.com/watch?v=vlyTthJugRQ>

★ Advantages: simple, robust to perturbation

★ Disadvantages: Corner-cutting, oscillation for non-holonomic robots



Control: Path tracking with controllers

★ AutonoVi

- ⑩ 2nd order pure-pursuit PID

- ⑩ Vehicle position + 2 points ahead on center of lane, trace arc between them

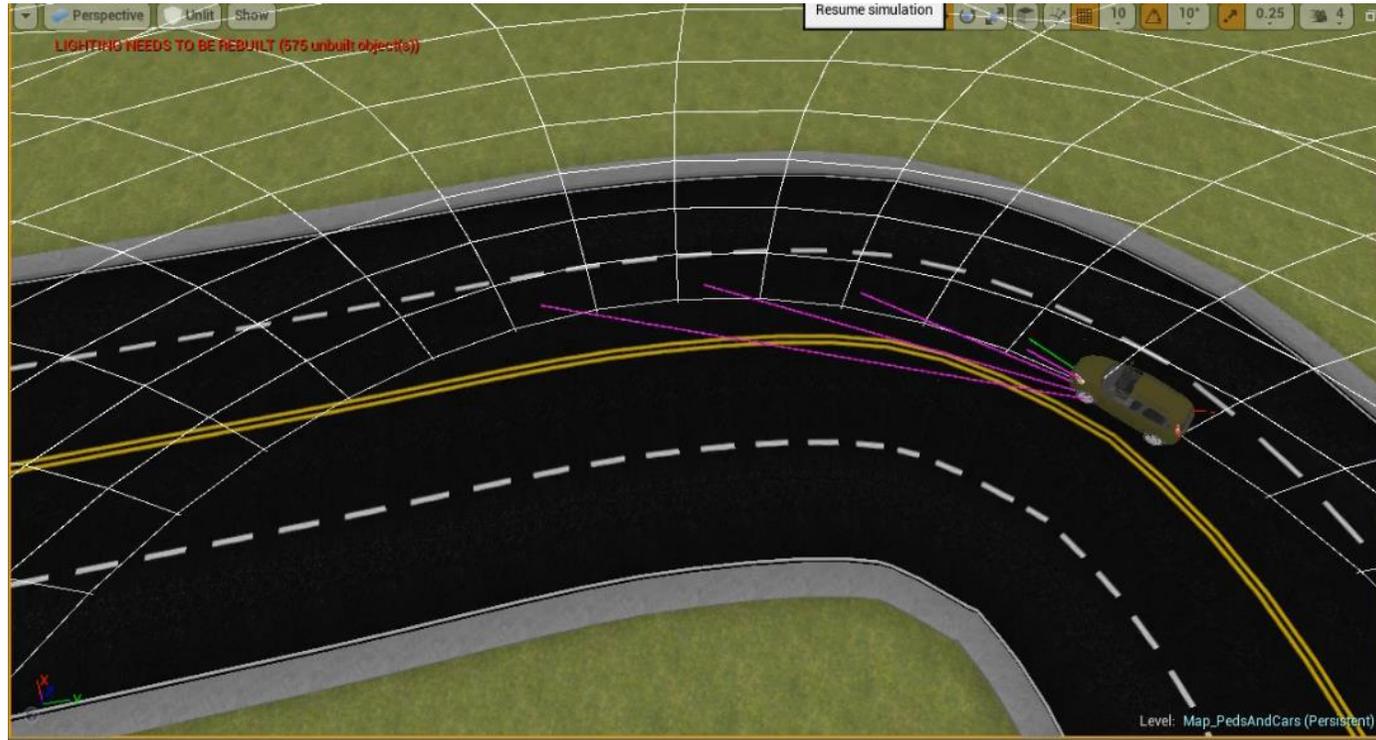
- ★ Advantages: simple, robust to perturbation, can represent kinematic limits in computed curves

- ★ Disadvantages: oscillation, prone to wide-turns, curvature prone to large shifts



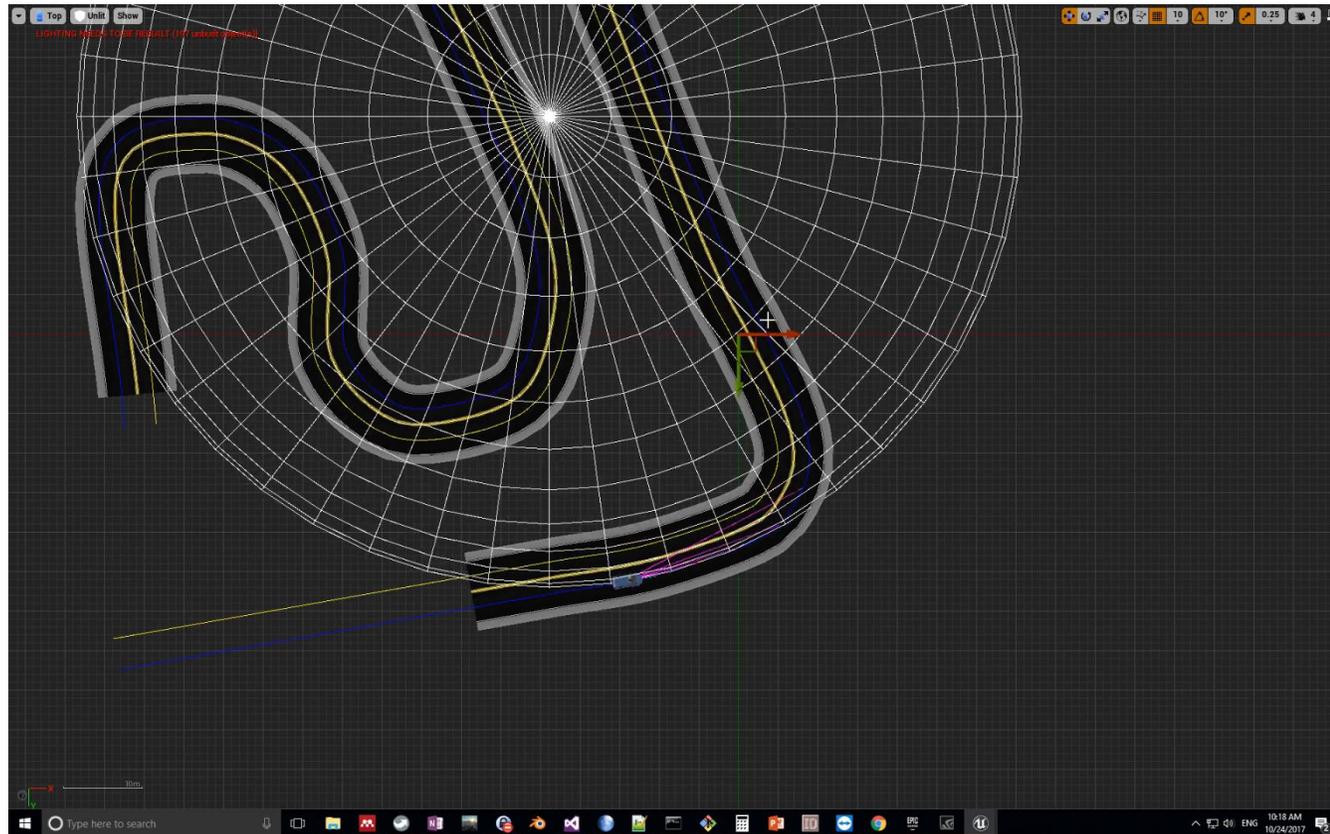
Control: Path tracking with controllers

★ AutonoVi



Control: Path tracking with controllers

✦ AutonoVi



Control: Path tracking with controllers

★ AutonoVi

⑩ NOTE: controllers have been demonstrated using arbitrary degree polynomials from N points on the path

★ Trade-offs in computational speed, robustness to perturbation, look-ahead computation



Control: Path tracking with controllers

★ Kinematic Car [De Luca 1998]

- ⑩ Attempts to simultaneously minimize heading error and cross-track error (distance to reference point on path)
- ⑩ Heading measured as path tangent orientation

$$\begin{aligned}\theta_e &= \theta - \theta_p(s) \\ \dot{s} &= v \cos(\theta_e) + \dot{\theta}_p e_{ra} \\ e_{ra} &= v \sin(\theta_e)\end{aligned}$$

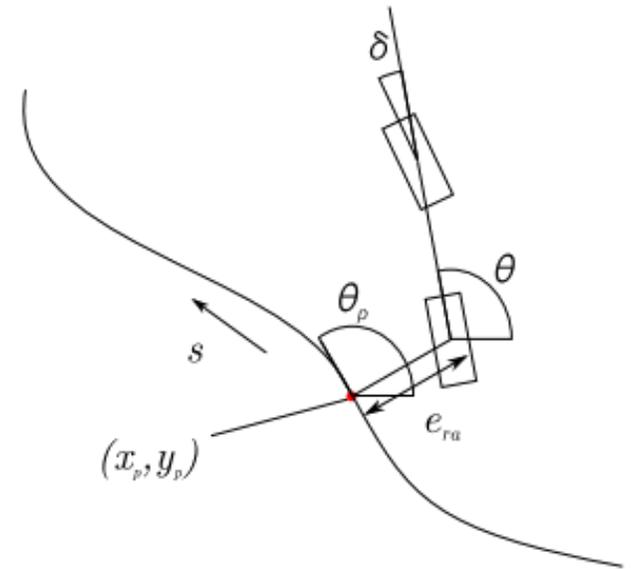


Figure 9. Path representation for kinematic car model



Control: Path tracking with controllers

◆ Kinematic Car [De Luca 1998]

⑩ Rewrite kinematics in “path coordinates”

$$\begin{bmatrix} \dot{s} \\ \dot{e}_{ra} \\ \dot{\theta}_e \\ \dot{\delta} \end{bmatrix} = \begin{bmatrix} \frac{\cos(\theta_e)}{1 - \dot{e}_{ra}\kappa(s)} \\ \sin(\theta_e) \\ \left(\frac{\tan\delta}{L}\right) - \frac{\kappa(s)\cos(\theta_e)}{1 - \dot{e}_{ra}\kappa(s)} \\ 0 \end{bmatrix} v \begin{bmatrix} 0 \\ 0 \\ 0 \\ 1 \end{bmatrix} \dot{\delta}$$

⑩ Goal becomes maximizing \dot{s} while minimizing \dot{e}_{ra} and $\dot{\theta}_e$

De Luca, A., Oriolo, G., & Samson, C. (1998). Feedback control of a nonholonomic car-like robot, 171–253. <http://doi.org/10.1007/BFb0036073>

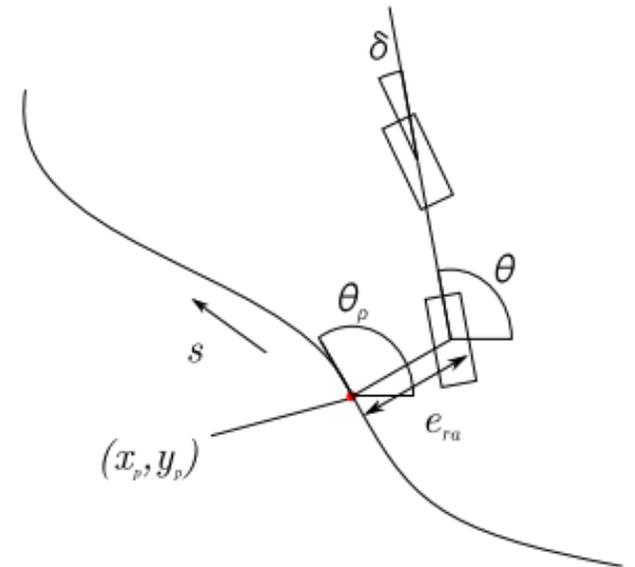


Figure 9. Path representation for kinematic car model

Control: Path tracking with controllers

★ Model-predictive

⑩ Given a model, i.e. kinematic car, perform repeated optimization over future states to determine optimal control

★ Advantages:

⑩ Robust to disturbance, reduces oversteer, requires model

★ Disadvantages:

⑩ Computationally expensive, model mismatch exacerbates errors

★ In my experience: a bad model in MPC performs worse than PID!



Control: Path tracking with controllers

★ Model-predictive

⑩ Examples:

⑩ <https://youtu.be/Bk7ES3Qd53s>

⑩ <https://youtu.be/C5UILYChPAc>

⑩ <https://youtu.be/5-hvtxeZNbo>

⑩ Code at: <https://github.com/parilo/CarND-MPC-Project>



Structure

- ★ Recap
- ★ Control
- ★ Traffic-Sim
 - ⑩ MATSim
 - ⑩ Sumo
 - ⑩ Hybrid Simulation
- ★ Prediction



Traffic-Sim: Rationale

★ Understand infrastructure

- ⑩ Evaluate efficiency of proposed changes to roads
- ⑩ Evaluate congestion points, failures, and improvements for existing roads
- ⑩ Test traffic control algorithms



Traffic-Sim: Methods

★ Agent-based:

⑩ Macroscopic: agents represented without physics or kinematics

★ Roads treated as edges in directed graph

★ Many agents supported, limited interactions

⑩ Microscopic: agents represented with kinematics or physics

★ Roads modelled with physical dimensions

★ Few agents supported, interactions can be modelled dynamically



Traffic-Sim: Methods

★ Flow-based:

- ⑩ Agents not explicitly represented
- ⑩ Flow computed over network, system evolves as “fluid” simulation



Structure

- ★ Recap
- ★ Control
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 - ⑩ MATSim
 - ⑩ Sumo
 - ⑩ Hybrid Simulation
- ★ Prediction



Traffic-Sim: MATSim

- ★ Agent-based, Macroscopic simulation

- ★ Supports millions of vehicles

- ★ <https://vimeo.com/124704874>

- ★ <https://youtu.be/VowP4f9ntCA?t=42s>

- ★ <https://youtu.be/VowP4f9ntCA?t=5m28s>

- ★ https://youtu.be/o60A4r6sSsE?list=PLLGIZCXnKbU6-9vy_rKZ6gW7E_ra42hfX



Traffic-Sim: MATSim

★ Features:

- ⑩ Millions of agents
- ⑩ Route import from loop detectors / traffic data
- ⑩ OpenStreetmap Import

★ Benefits:

- ⑩ Macro-scale modelling replicates usage data gathered over long periods
- ⑩ Simulation of alternate routes and large time-scales simply
- ⑩ Evaluate macro changes: for example, starting school 30m later



Structure

- ★ Recap
- ★ Control
- ★ Traffic-Sim
 - ⑩ MATSim
 - ⑩ **SUMO**
 - ⑩ Hybrid Simulation
- ★ Prediction



Traffic-Sim: SUMO

- ✦ Agent-based, Microscopic simulation
- ✦ Allows for modeling lane configuration, route-planning, vehicle size and shapes, preliminary pedestrians
- ✦ Online control and modification of network
- ✦ https://youtu.be/KgPSREMmA_0
- ✦ <https://youtu.be/a52U6CQQRcw?t=24s>
- ✦ <https://youtu.be/qewufs0Xsq0>



Traffic-Sim: SUMO

★ Notable Features:

- ⑩ OpenStreetmap Import, automatic processing of lane connectivity
- ⑩ Control and physics free
- ⑩ Multiple driver models, “person level” transport options

★ Benefits:

- ⑩ Allows detailed testing of traffic-lights and intersections
- ⑩ Widely used for V2X communication research



Structure

- ★ Recap
- ★ Control
- ★ Traffic-Sim
 - ⑩ MATSim
 - ⑩ SUMO
 - ⑩ **Hybrid Simulation**
- ★ Prediction



Traffic-Sim: Hybrid & Flow Models

★ Non-agent based models

- ⑩ Treat traffic as flow model, like liquid
- ⑩ Continuum formulation evolves road network
- ⑩ Allows for immense networks, but limits the ability to represent agentive phenomena



Traffic-Sim: Hybrid & Flow Models

Continuum Traffic Simulation

Jason Sewall
David Wilkie
Paul Merrell
Ming Lin



Traffic-Sim: Hybrid & Flow Models

★ Hybrid models

⑩ “Best of both worlds”

- ★ continuum evolution for “distant” traffic phenomena

- ★ Agent-based simulation for nearby vehicles

⑩ Captures driver behavior in micro-scale and accurately models aggregate information

- ⑩ <https://www.youtube.com/watch?v=eEnGFxfN2tE>

⑩ see me after class for more papers



Structure

- ★ Recap
- ★ Control
- ★ Traffic-Sim
 - ⑩ MATSim
 - ⑩ SUMO
 - ⑩ Hybrid Simulation
- ★ Prediction



Traffic-Sim: Recent Applications

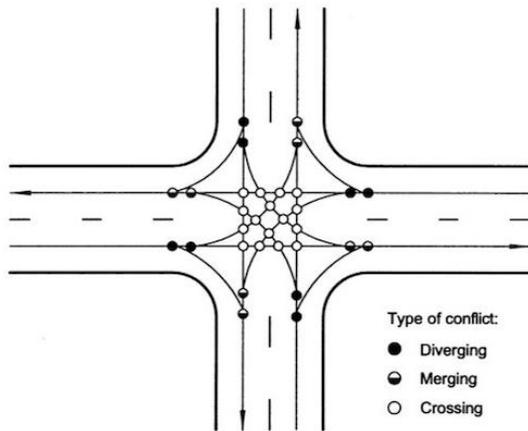
https://www.citylab.com/solutions/2013/01/could-these-crazy-intersections-make-us-safer/4467/?utm_source=SFFB

good article

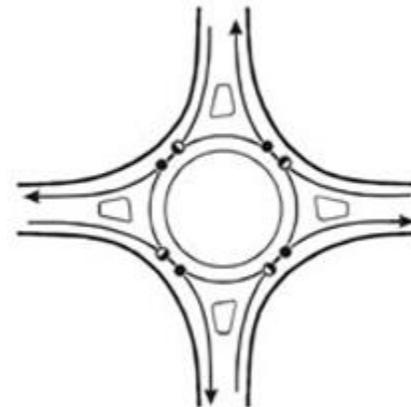
★ Safer intersections:

⑩ Geometric analysis performed to determine intersection danger

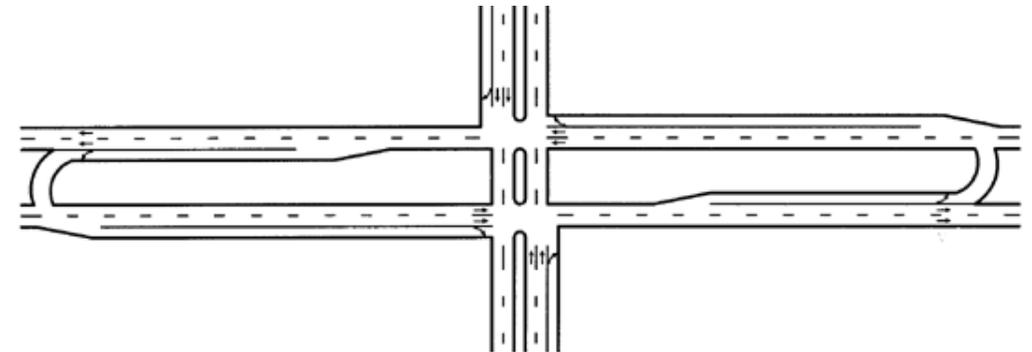
⑩ Design intersections which optimize flow & limit intersection points



32 collision points



8 collision points



18 collision points?

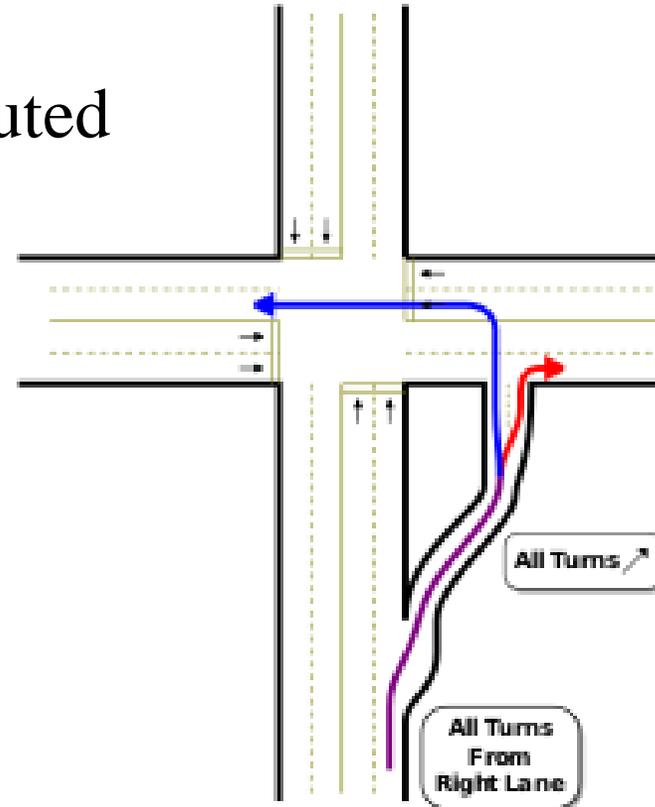


Traffic-Sim: Recent Applications

★ Jughandle:

⑩ Turns from minor road executed at special “handle”

⑩ <https://vimeo.com/58011852>

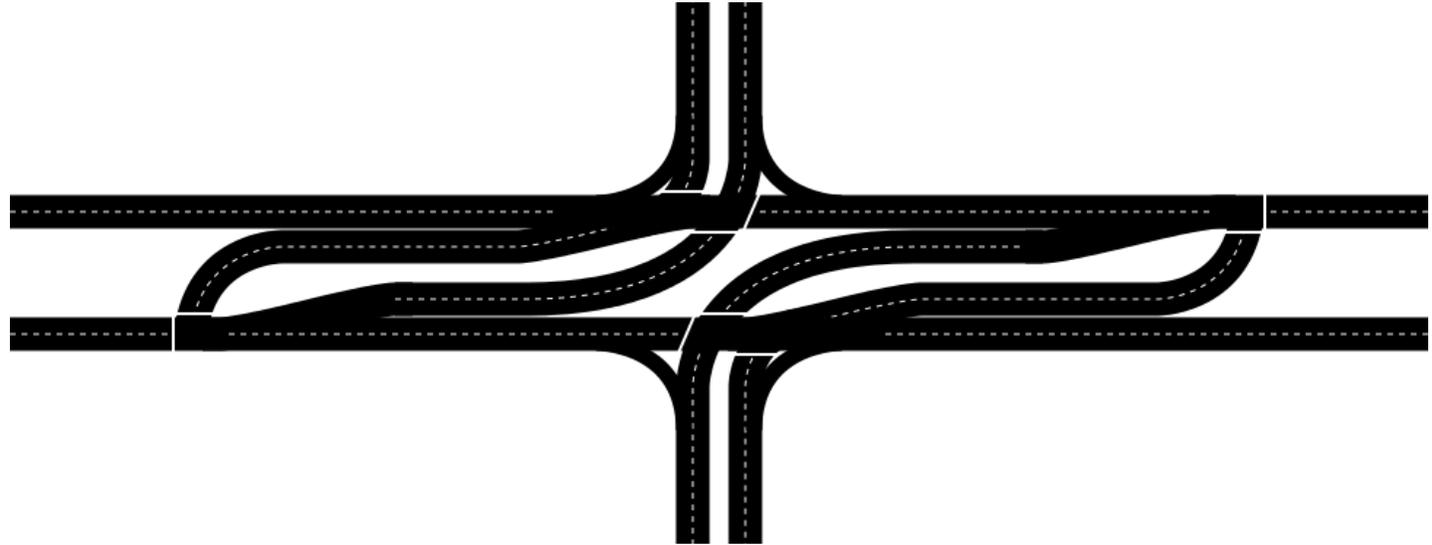


Traffic-Sim: Recent Applications

★ Superstreet:

⑩ Minor road NOT ALLOWED
to cross major road

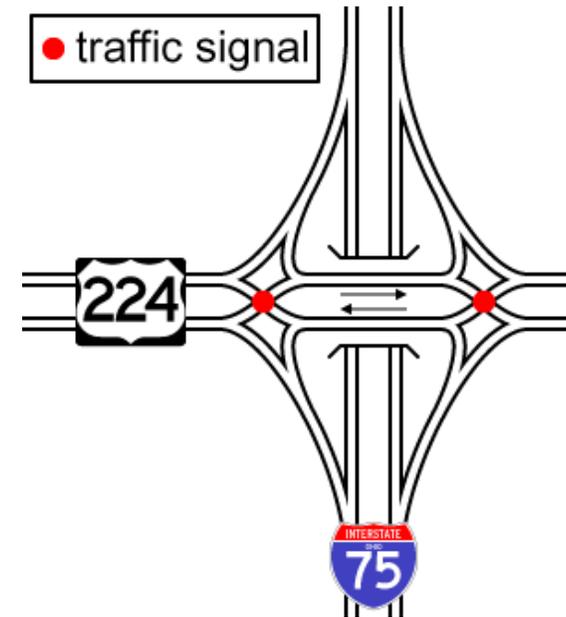
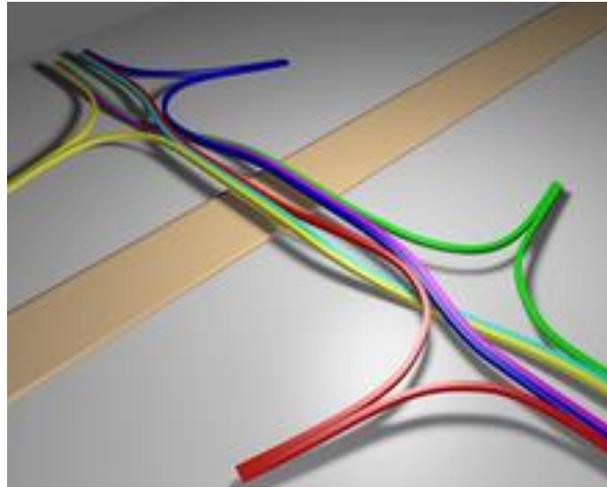
⑩ <https://vimeo.com/57973069>



Traffic-Sim: Recent Applications

★ Diverging Diamond:

- ⑩ Minor road crosses in X pattern
- ⑩ Allows continuous flow in 2 directions
- ⑩ <https://vimeo.com/57972903>



Traffic-Sim: Recent Applications

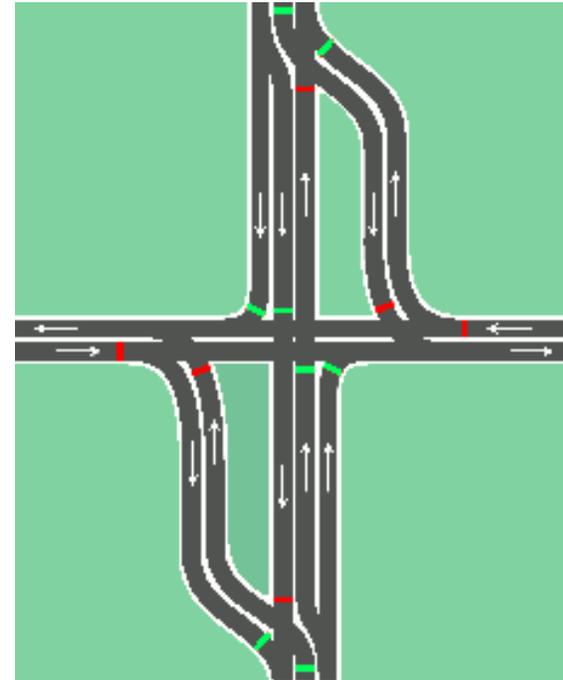
★ Continuous Flow:

⑩ Left turns pre-cross oncoming lanes

⑩ I grew up with one of these

⑩ <https://vimeo.com/57973241>

⑩ <https://vimeo.com/57973040>



Traffic-Sim: Recent Applications

- ★ What should traffic lights look like for AVs?
 - ⑩ Are they needed at all?
 - ⑩ How do we optimize for mixed AV and non-AV traffic?
 - ⑩ <https://vimeo.com/37751380>
- ★ Great resources at <https://goo.gl/3YUY2o>



Structure

- ★ Recap
- ★ Control
- ★ Traffic-Sim
- ★ **Prediction**



Limitations in Planning

★ Most autonomous navigation algorithms

- ⑩ Defensive

- ⑩ Opaque

- ⑩ Do not consider “interactions” with other participants

- ⑩ Assume a very simple model for estimating movement of other cars

★ Drivers have a tendency to rear end self-driving cars on the road [Consumer Affairs]

- ⑩ 19 such crashes out of 285 Waymo vehicles in CA in 2017



Structure

- ✦ Interaction-based planning
 - ⑩ Formal framework for 2-way interactions
 - ⑩ Probabilistic reasoning for multi-vehicle interactions



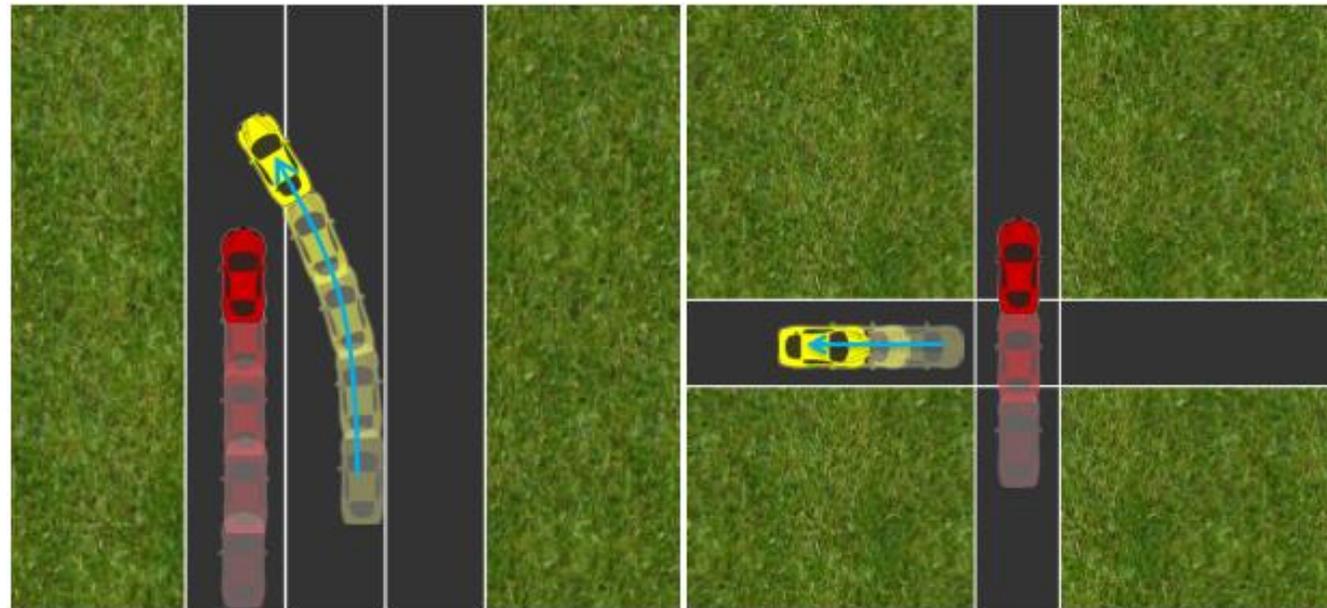
Formal Framework for 2-way interactions

- ★ Dorsa Sadigh, Shankar Sastry, Sanjit A. Seshia, and Anca D. Dragan. **Planning for Autonomous Cars that Leverages Effects on Human Actions.** In Proceedings of the Robotics: Science and Systems Conference (RSS), June 2016.
- ★ Our key insight is that other drivers do not operate in isolation:
 - ⑩ an autonomous car's actions will actually have effects on what other drivers will do.
 - ⑩ Leveraging these effects during planning will generate behaviors for autonomous cars that are more efficient and communicative.



Formal Framework for 2-way interactions

- ★ We model the interaction between an autonomous car and a human driver as a dynamical system, in which the robot's actions have immediate consequences on the state of the car, but also on human actions.



(a) Car merges *ahead* of human;
anticipates human *braking*

(b) Car *backs up* at 4way stop;
anticipates human *proceeding*



Formal Framework for 2-way interactions

- ✦ Let x represent the state of the system, which includes positions and velocities of the human and autonomous robot.
- ✦ Effect of robot controls: $x' = f_{\mathcal{R}}(x, u_{\mathcal{R}})$
- ✦ Effect of human actions: $x'' = f_{\mathcal{H}}(x', u_{\mathcal{H}})$
- ✦ Overall dynamics of the system: $x^{t+1} = f_{\mathcal{H}}(f_{\mathcal{R}}(x^t, u_{\mathcal{R}}^t), u_{\mathcal{H}}^t)$



Formal Framework for 2-way interactions

- ★ Formulate choosing robot controls as a reward maximization problem
- ★ Reward function of robot

$$r_{\mathcal{R}}(x^t, u_{\mathcal{R}}^t, u_{\mathcal{H}}^t).$$

- ⑩ Reward function depends on $u_{\mathcal{H}}$

- ★ MPC used at every iteration

- ⑩ Let x^0 be the current state

- ⑩ Reward over MPC time horizon t is :

$$R_{\mathcal{R}}(x^0, \mathbf{u}_{\mathcal{R}}, \mathbf{u}_{\mathcal{H}}) = \sum_{t=1}^N r_{\mathcal{R}}(x^t, u_{\mathcal{R}}^t, u_{\mathcal{H}}^t)$$



Formal Framework for 2-way interactions

★ At every iteration, the robot needs to find the \mathbf{u}_R that maximizes this reward:

$$\mathbf{u}_R^* = \arg \max_{\mathbf{u}_R} R_{\mathcal{R}}(x^0, \mathbf{u}_R, \mathbf{u}_{\mathcal{H}}^*(x^0, \mathbf{u}_R))$$

⑩ $\mathbf{u}_{\mathcal{H}}^*(x^0, \mathbf{u}_R)$ is what the human would do over the next N steps if the robot were to execute \mathbf{u}_R .

★ Typical solutions assume that the human will maintain current velocity

$$\mathbf{u}_{\mathcal{H}}^*(x^0, \mathbf{u}_R) = \mathbf{u}_{\mathcal{H}}^*(x^0)$$

⑩ Instead they assume that humans would maximize their own reward function.



Formal Framework for 2-way interactions

★ Human driver reward

⑩ Use Inverse Reinforcement Learning (IRL) over driver demonstrations in simulation.

⑩ Assume a simple parameterization of human reward

★ Given a human reward function

⑩ Solve the optimization problem using quasi-Newton methods like L-BFGS

$$\mathbf{u}_{\mathcal{R}}^* = \arg \max_{\mathbf{u}_{\mathcal{R}}} R_{\mathcal{R}}(x^0, \mathbf{u}_{\mathcal{R}}, \mathbf{u}_{\mathcal{H}}^*(x^0, \mathbf{u}_{\mathcal{R}}))$$



Experiments

- ★ Assume a simple dynamics model of the car.
- ★ 3 Scenarios
 - ⑩ Make human slow down
 - ⑩ Make human change lanes
 - ⑩ Make human go first through intersection
- ★ In each case, hand engineer the robot reward function achieve the desired effect on human behavior



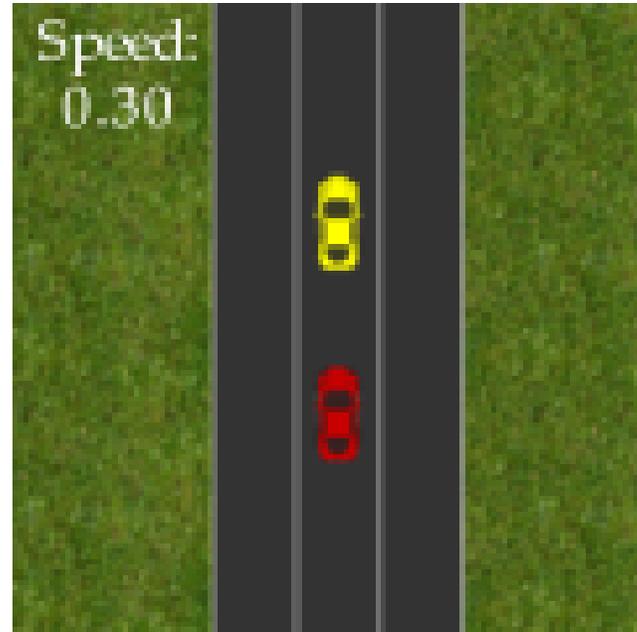
Experiments: Make human slow down

- ✦ The robot plans to move in front of the person, expecting that this will make them slow down.
- ✦ Achieved by augmenting the robot's reward with the negative of the square of the human velocity.



Experiments: Make human change lanes

- ★ The robot plans to purposefully occupy two lanes, expecting this will make the human move around it by using the unoccupied lane.
- ★ Achieved by augmenting the robot's reward with the lateral position of the human



Experiments: Make human cross intersection first

- ★ The robot plans to purposefully back up slightly, expecting this will make the human cross first.
- ★ Achieved by augmenting the robot's reward with a feature based on the position of the human car relative to the middle of the intersection.
 - ⑩ Communication behavior emerges naturally out of reward optimization.



Structure

★ Interaction-based planning

⑩ Formal framework for 2-way interactions

⑩ Probabilistic reasoning for multi-vehicle interactions



Behavior Prediction

- ★ Galceran, E., Cunningham, A. G., Eustice, R. M., & Olson, E. (2017). **Multipolicy decision-making for autonomous driving via changepoint-based behavior prediction: Theory and experiment.** *Autonomous Robots*, 1-16.
- ★ Choose ego-vehicle actions that maximize a reward function over time within a dynamic, uncertain environment with tightly coupled inter-actions between multiple agents.



Behavior Prediction

- ★ Assume a set of a priori known policies
 - ⑩ Go straight, change lanes, merge left, merge right etc
- ★ Leverage Bayesian change-point detection to estimate the policy that a given vehicle was executing at each point in its history of actions.
 - ⑩ Given current policy, infer the likelihood of actions or intentions.
- ★ Statistical test for detecting anomalous behaviors.



Behavior Prediction

★ Bayesian change-point detection over 30 s windows

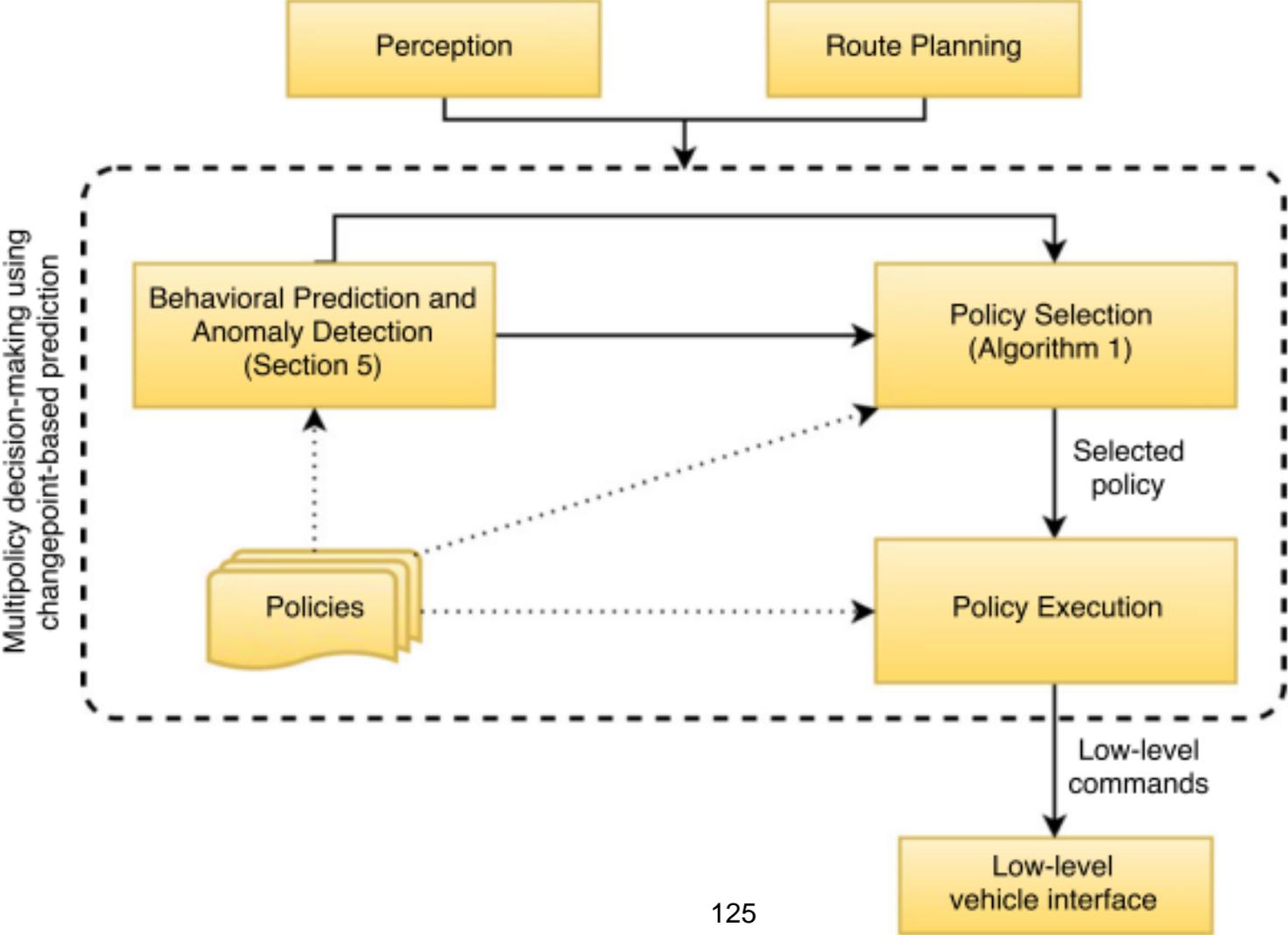


Multi-policy decision making

- ★ Draw set of sample policies over distribution for neighbor vehicles
 - ⑩ For each sample set
 - ★ Simulate other vehicles forward
 - ★ Choose a policy for ego vehicle that maximizes reward in this instance
 - ★ Track best reward
- ★ Choose policy for ego vehicle with the best reward



Approach



Conclusion

- ★ Proof of concept tests in real world and simulation
 - ⑩ Good real world results in “offline” behavior prediction
- ★ Limitations
 - ⑩ No guarantees in decision making
 - ⑩ A very coarse approximation of POMDP
 - ⑩ Decision making is slow
 - ★ 2-4 neighbors with small set of policy samples
 - ★ Anomalous detection does not influence decision making



Questions?



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