

# Comp 790-058 Lecture 10: Autonomous Driving: Control, Traffic, Predictions

October 24, 2017

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# Administrative

- ✦ Homework 2 due:
  - ⑩ 11:59 PM October 30<sup>th</sup>
- ✦ Homework 3:
  - ⑩ Not today! But this week.
- ✦ Project Updates:
  - ⑩ Remember to work consistently on projects
  - ⑩ It WILL sneak up on you
- ✦ AutonoVi Updates:
  - ⑩ Git setup
  - ⑩ If you need access, please see me after class



# Structure

## ★ Recap

- ⑩ Perception

- ⑩ Localization

- ⑩ State / Kinematics / Dynamics

- ⑩ Planning

## ★ Control

## ★ Traffic-Sim

## ★ Prediction



# Autonomous Driving

- ★ **Autonomous vehicle**: a motor vehicle that uses artificial intelligence, sensors and global positioning system coordinates to drive itself without the active intervention of a human operator
- ★ Focus of enormous investment [\$1b+ in 2015]



Tesla



Waymo



Nutonomy



# Autonomous Driving: Levels of Autonomy

- ★ 0: Standard Car
- ★ 1: Assist in some part of driving
  - ⑩ Cruise control
- ★ 2: Perform some part of driving
  - ⑩ Adaptive CC + lane keeping
- ★ 3: Self-driving under ideal conditions
  - ⑩ Human must remain fully aware
- ★ 4: Self-driving under near-ideal conditions
  - ⑩ Human need not remain constantly aware
- ★ 5: Outperforms human in all circumstances



# Autonomous Driving: Main Components

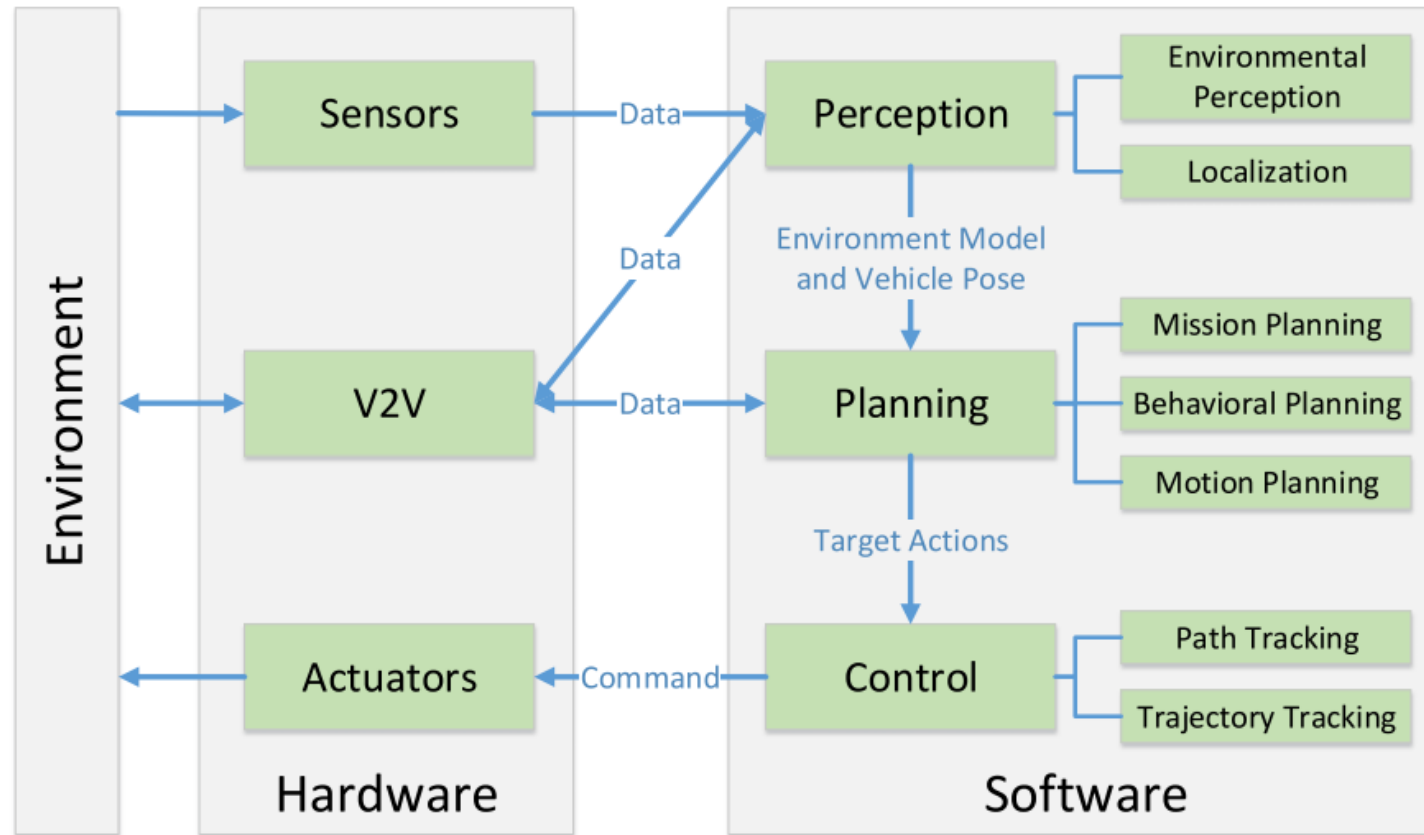


Figure 2. A typical autonomous vehicle system overview, highlighting core competencies.



# Structure

## ★ Recap

⑩ **Perception**

⑩ Localization

⑩ State / Kinematics / Dynamics

⑩ Planning

## ★ Control

## ★ Traffic-Sim

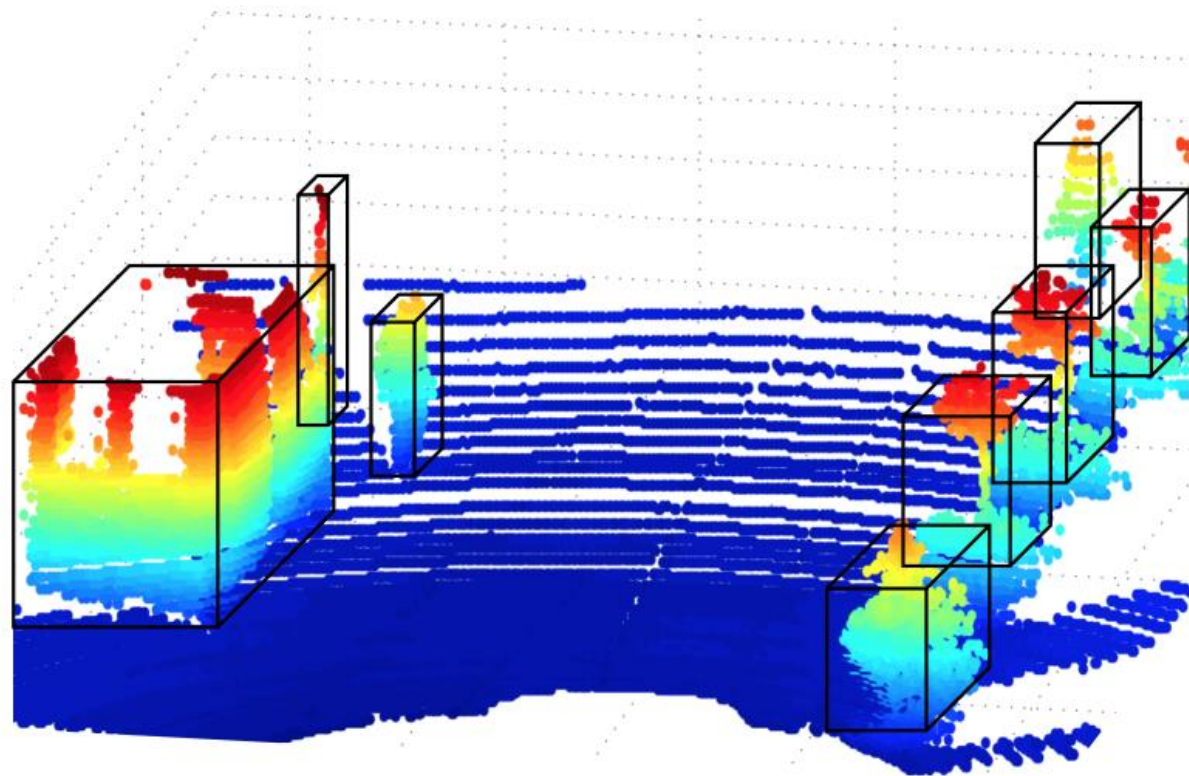
## ★ Prediction



# Autonomous Driving: Perception using LIDAR

## ★ Light Detection and Ranging

- ⑩ Illuminate target using pulsed laser lights, and measure reflected pulses using a sensor





# Autonomous Driving: Perception using LIDAR

## ★ LIDAR in practice

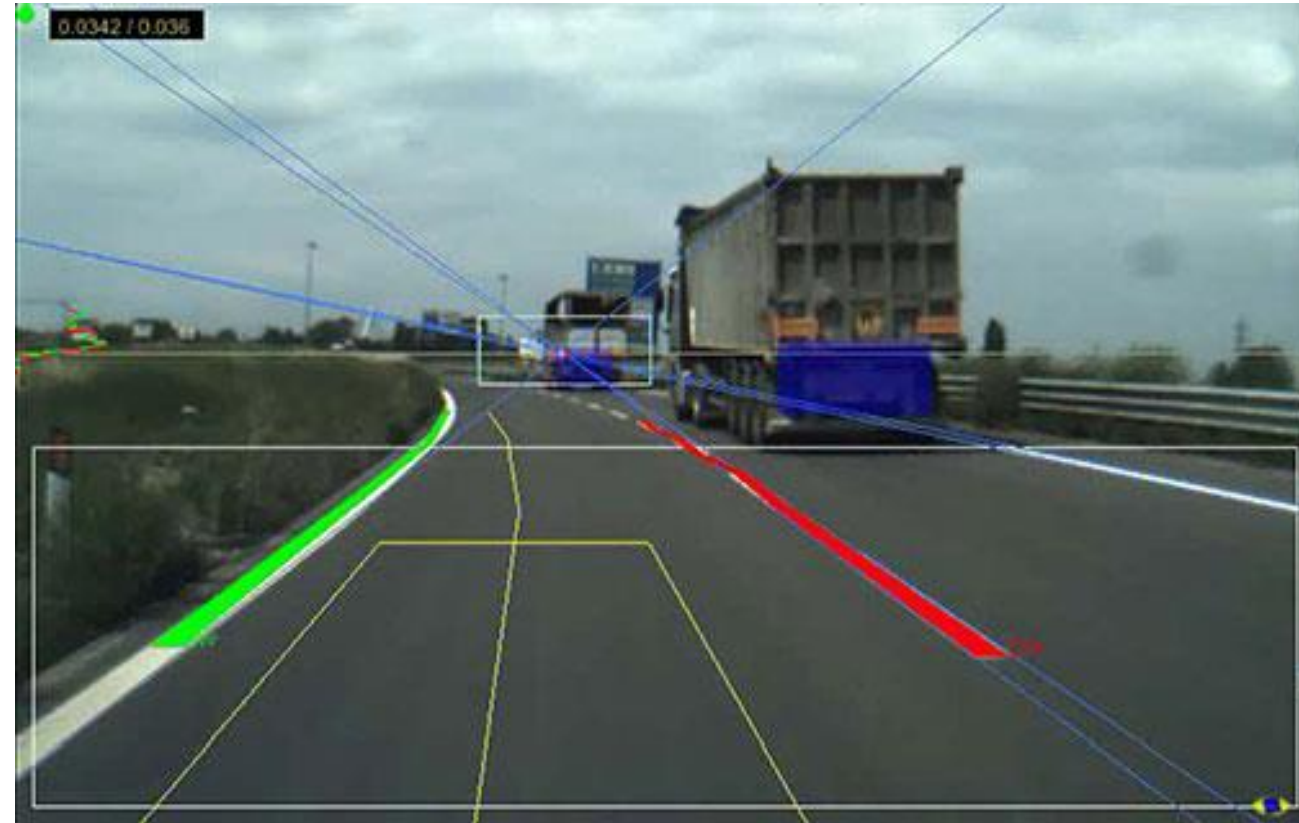
### ⑩ Velodyne 64HD lidar

★ [https://www.youtube.com/watch?v=nXlqv\\_k4P8Q](https://www.youtube.com/watch?v=nXlqv_k4P8Q)



# Autonomous Driving: Perception using Cameras

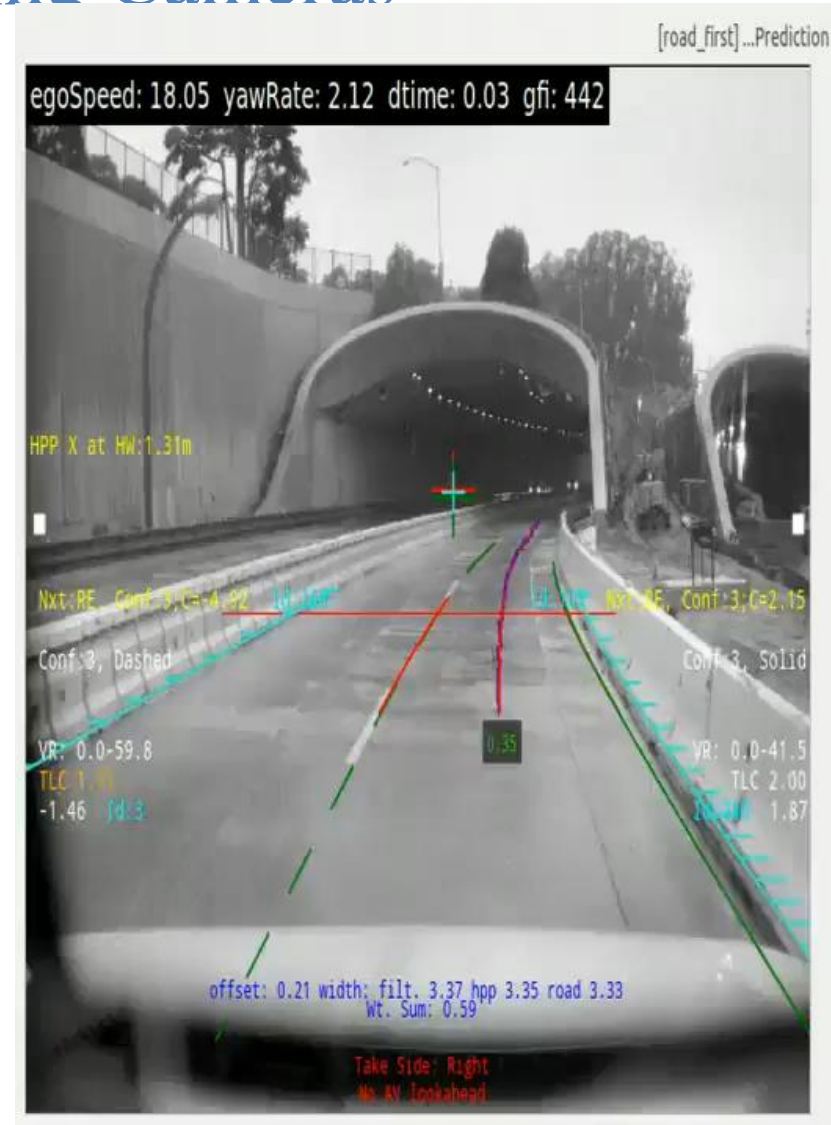
- ★ Camera based vision
  - ⑩ Road detection
    - ★ Lane marking detection
    - ★ Road surface detection
  - ⑩ On-road object detection



# Autonomous Driving: Perception using Cameras

## ★ Sensing Challenges

- ⑩ Sensor Uncertainty
- ⑩ Sensor Configuration
- ⑩ Weather / Environment



# Structure

## ★ Recap

- ⑩ Perception

- ⑩ **Localization**

- ⑩ State / Kinematics / Dynamics

- ⑩ Planning

## ★ Control

## ★ Traffic-Sim

## ★ Prediction



# Autonomous Driving: Vehicle Localization

- ✦ Determining the pose of the ego vehicle and measuring its own motion
- ✦ Fusing data
  - ⑩ Satellite-based navigation system
  - ⑩ Inertial navigation system
- ✦ Map aided localization
  - ⑩ SLAM



# Structure

## ★ Recap

⑩ Perception

⑩ Localization

⑩ **State / Kinematics / Dynamics**

⑩ Planning

## ★ Control

## ★ Traffic-Sim

## ★ Prediction



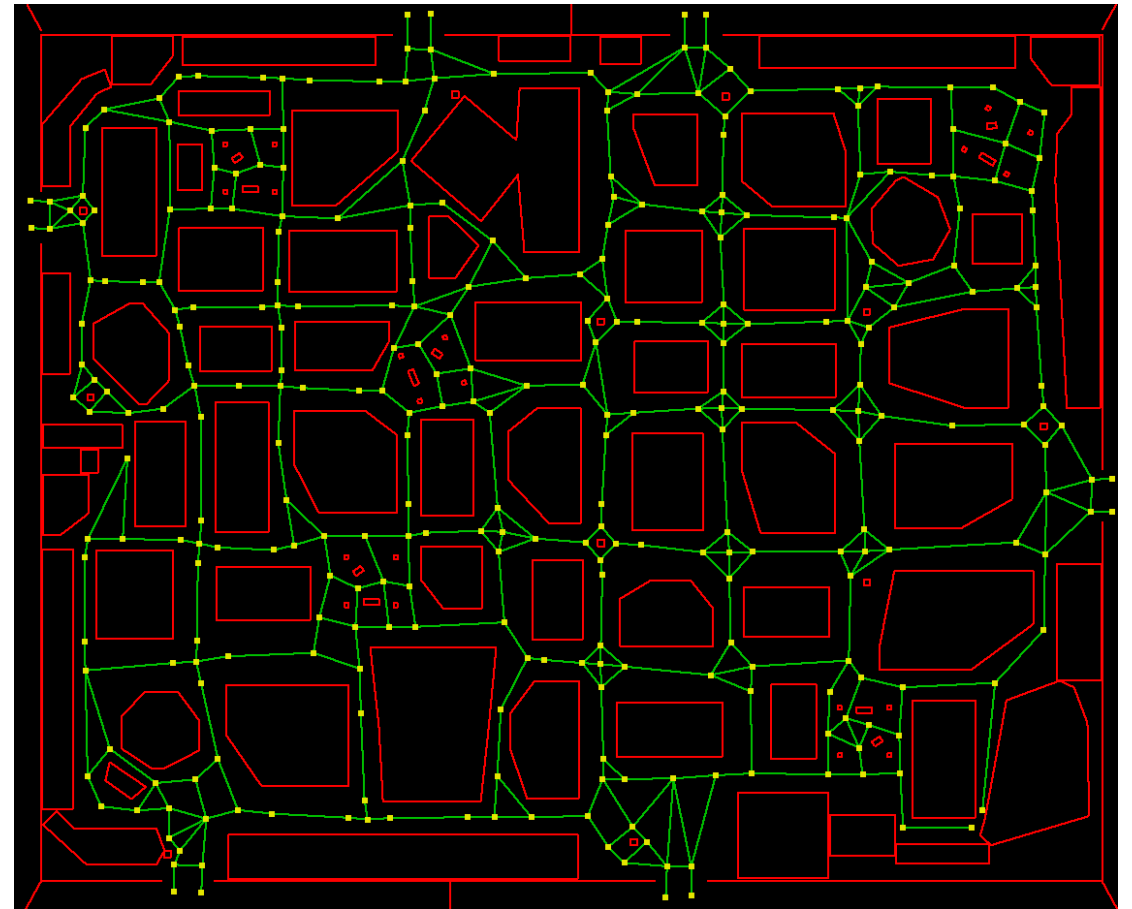
# Autonomous Driving: State Space

- ★ “The set of attribute values describing the condition of an autonomous vehicle at an instance in time and at a particular place during its motion is termed the ‘state’ of the vehicle at that moment”
- ★ Typically a vector with position, orientation, linear velocity, angular velocity
- ★ **State Space**: set of all states the vehicle could occupy



# Autonomous Driving: State Space

- ★ Recall Pedestrian Planning:
  - ⑩ Roadmap is essential a graph of potential agent states





# Autonomous Driving: State Space

## ★ Examples:

⑩ 2D space with blinker booleans

★  $(\vec{p}, \theta, \vec{v}, \omega, bl_l, bl_r)$

⑩ State contains everything we need to describe the robot's current configuration!

⑩ Neglect some state variables when planning



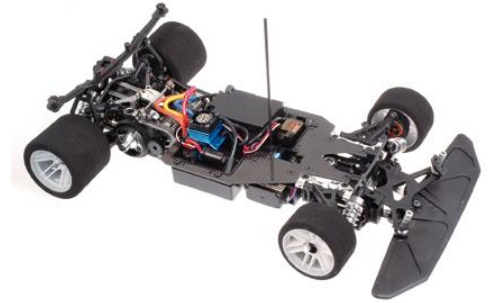
# Structure

- ★ Recap
- ★ State, Kinematics, and Dynamics Models
  - ⑩ State Space
  - ⑩ **Kinematic constraint models of the vehicle**
  - ⑩ Dynamic constraint models of the vehicle
- ★ Planning
- ★ AutonoVi-Sim



# Autonomous Driving: Holonomicity

- ★ Cars are “non-holonomic” robots
  - ⑩ Typically 5 values describing physical
    - ★ (2 Cartesian coordinates, orientation, linear speed, angular speed)
  - ⑩ 2 “kinematic” constraints
    - ★ Can only move forward or backward, tangent to body direction
    - ★ Can only steer in bounded radius



# Kinematic Constraints

## ★ Kinematics of Motion

- ⑩ “the branch of mechanics that deals with pure motion, without reference to the masses or forces involved in it”
- ⑩ Equations describing conversion between control and motion
- ⑩ Control: inputs to the system
  - ★ In vehicle: steering and throttle
  - ★ Also referred to as “Action” in literature



# Autonomous Driving: Holonomicity

- ★ kinematic and dynamic constraints can be considered “rules” governing the state evolution function
- ★ For state  $s_t \in S$ , control input  $u_t \in U$ , time  $t \in T$ :
  - ⑩  $F(s_t, u_t, \Delta t) \rightarrow s_{t+1}$
- ★ Ex:
  - ⑩ A car cannot turn in place. No amount of steering will accomplish this
  - ⑩ A Roomba can turn in place



# Kinematic Constraints

## ★ Kinematic models of a car

### ⑩ Single-track Bicycle (or simple car model)

★ 3-DOF configuration:  $(x, y, \theta)$

★ 2-DOF control: steering  $(\phi)$ , speed  $(v)$

★ Full state:  $(x, y, \theta, v, \phi, L)$

### ⑩ Equations of motion:

$$\dot{p}_x = v * \cos(\theta) \quad \dot{p}_y = v * \sin(\theta)$$

$$\dot{\theta} = \frac{\tan(\phi)}{L}$$

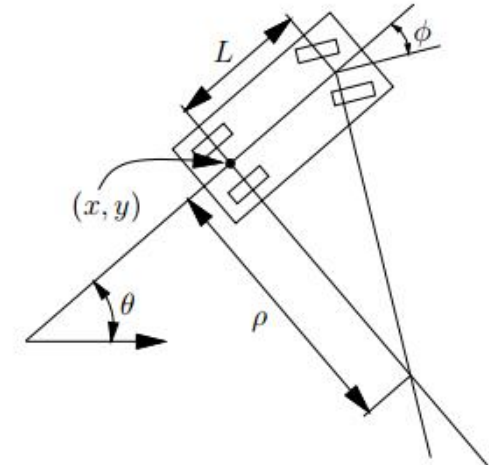
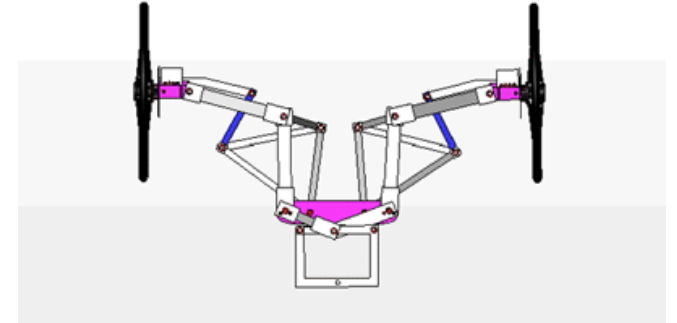


Figure 13.1: The simple car has three degrees of freedom, but the velocity space at any configuration is only two-dimensional.



# Kinematic Constraints

- ★ Single-track bicycle example
  - ⑩ [github link to my project]

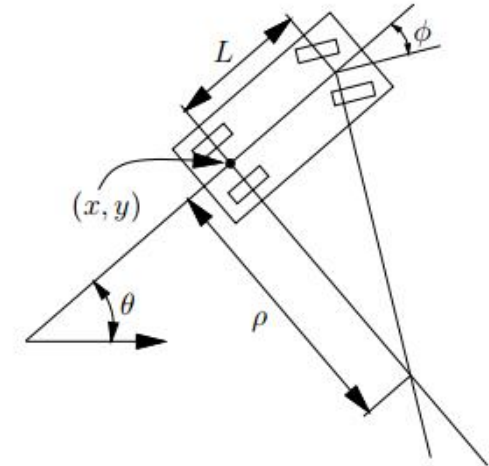
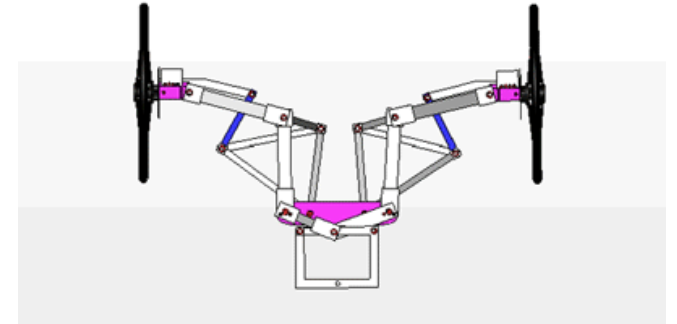


Figure 13.1: The simple car has three degrees of freedom, but the velocity space at any configuration is only two-dimensional.



# Structure

- ★ Recap
- ★ State, Kinematics, and Dynamics Models
  - ⑩ State Space
  - ⑩ Kinematic constraint models of the vehicle
  - ⑩ **Dynamic constraint models of the vehicle**
- ★ Planning
- ★ AutoNoVi-Sim





# Dynamic Constraints

- ★ “the branch of mechanics concerned with the motion of bodies under the action of forces.”
- ★ Tires subject to lateral and longitudinal force during steering / accelerating
  - ⑩ If lateral force exceeds friction force
    - ★ Fishtailing
  - ⑩ If longitudinal force exceeds friction force
    - ★ Peel out / skid



# Dynamic Constraints

- ✦ No longer directly control acceleration and steering
  - ⑩ Apply engine force
  - ⑩ Apply steering force
- ✦ Diminishing returns on each force at limits of control



# Dynamic Constraints

## ★ Dynamic Bicycle model with linear tires

- ⑩ No load transfer between tires
- ⑩ Larger state space including tire stiffness

- ★  $F_x$  longitudinal force
- ★  $F_y$  lateral force
- ★  $m$  mass
- ★  $I_z$  yaw moment of inertia

$$\begin{aligned}
 F_{xf} \cos \delta - F_{yf} \sin \delta + F_{xr} &= m(\dot{v}_x - v_y \dot{\psi}) \\
 F_{xf} \sin \delta + F_{yf} \cos \delta + F_{yr} &= m(\dot{v}_y + v_x \dot{\psi}) \\
 (F_{xf} \sin \delta + F_{yf} \cos \delta)b - F_{yr}c &= I_z \ddot{\psi} \\
 F_y &= C_\alpha \alpha
 \end{aligned}$$

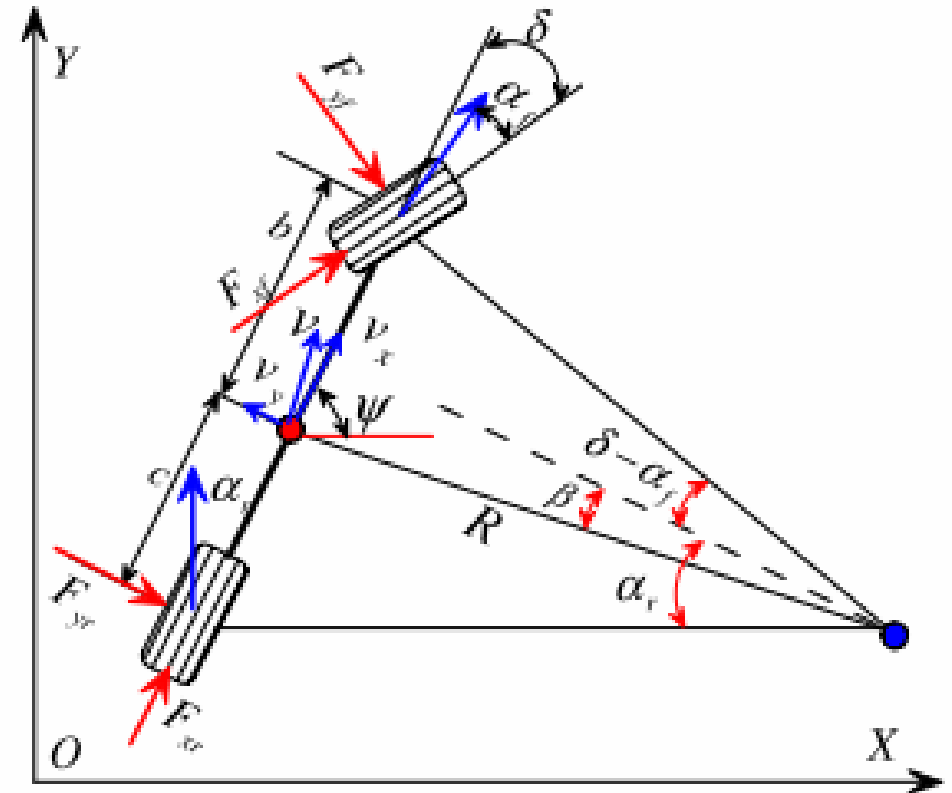
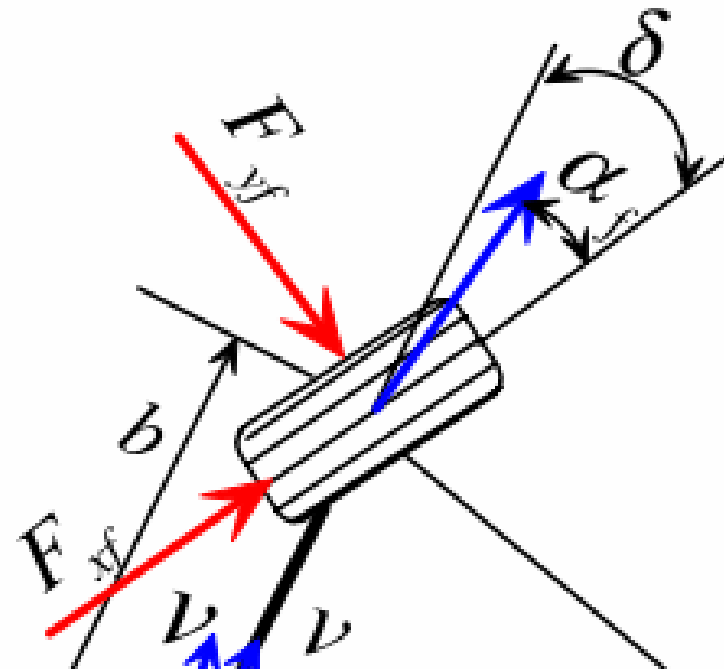


Fig. 1. Bicycle model of vehicle



# Dynamic Constraints

- ★ Dynamic Bicycle model with linear tires
  - ⑩  $F_y$  lateral force on tire
  - ⑩  $F_x$  longitudinal force on tire
  - ⑩  $\alpha_f$  “slip angle” of tire
  - ⑩  $\delta$  steering angle



# Dynamic Constraints

★ Models increase in complexity as needed for performance tuning

⑩ Aerodynamic drag force  $F_{wind} = (C_w A_w v_t^2 g) / 16$

⑩ Maximum engine torque  $\frac{F_{max}}{m} = 1 + \frac{3}{1 + e^{(\frac{v_t - 12}{4})}}$

★ Each layer of dynamics:

⑩ Increases accuracy of model

⑩ Increases computational complexity



# Structure

## ★ Recap

⑩ Perception

⑩ Localization

⑩ State / Kinematics / Dynamics

⑩ **Planning**

## ★ Control

## ★ Traffic-Sim

## ★ Prediction



# Autonomous Driving: Main Components

## ✦ Planning

- ⑩ Making purposeful decisions in order to achieve the robot's higher order goals

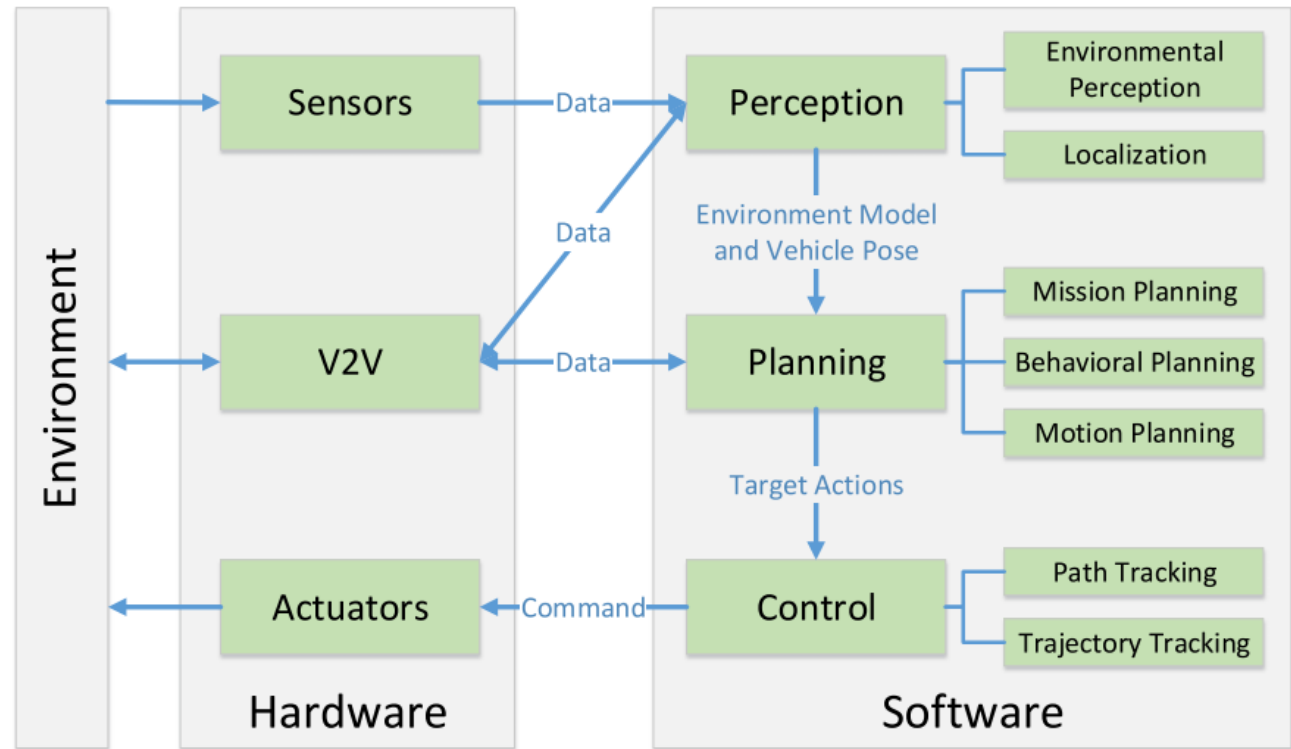


Figure 2. A typical autonomous vehicle system overview, highlighting core competencies.



## Main Idea

- ★ **Motion Planning**: term used in robotics for the process of breaking down a desired movement task into discrete **motions** that satisfy movement constraints and possibly optimize some aspect of the movement





# Autonomous Driving: Planning

## ★ Compare to Pedestrian Techniques:

- ⑩ Route Planning: road selection (global)
- ⑩ Path Planning: preferred lanes (global)
- ⑩ Maneuver-search: high level maneuvers (local)
- ⑩ Trajectory planning: Lowest level of planning (local)

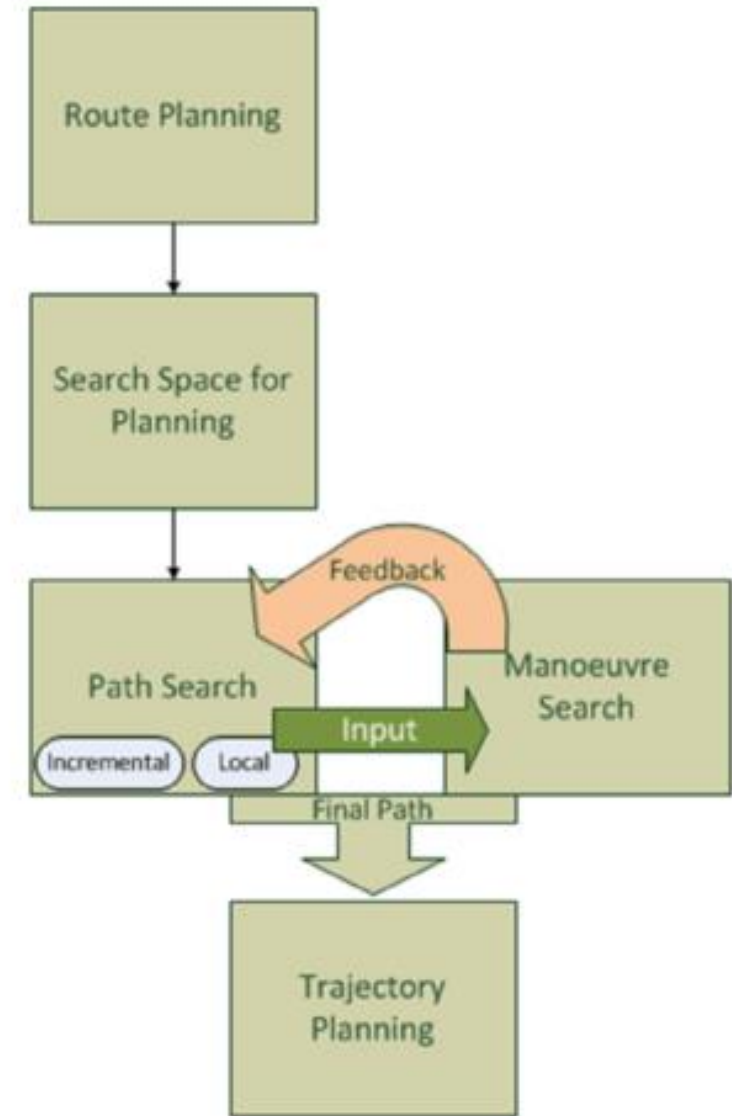


Fig. 2. A flow chart of planning modules.



# Mission Planner (Route Planning)

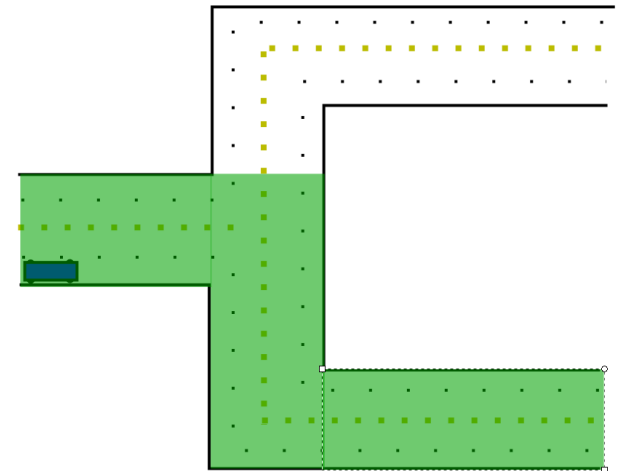
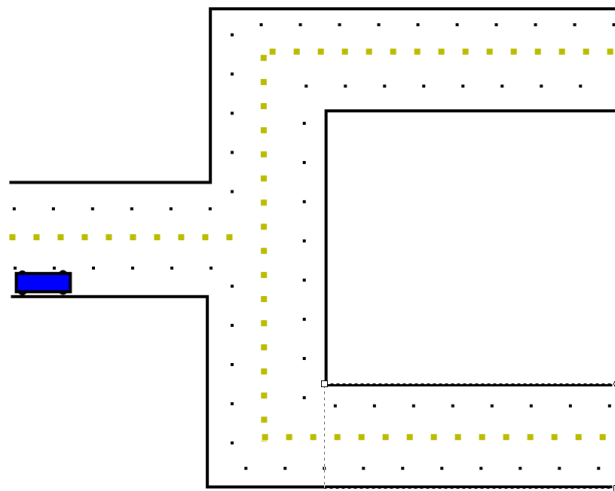
- ★ Pendleton: “considers high level objectives, such as assignment of pickup/dropoff tasks and which roads should be taken to achieve the task”
- ★ Typical approaches:

- ⑩ RNG (Road-network Graph)

- ★ A\*

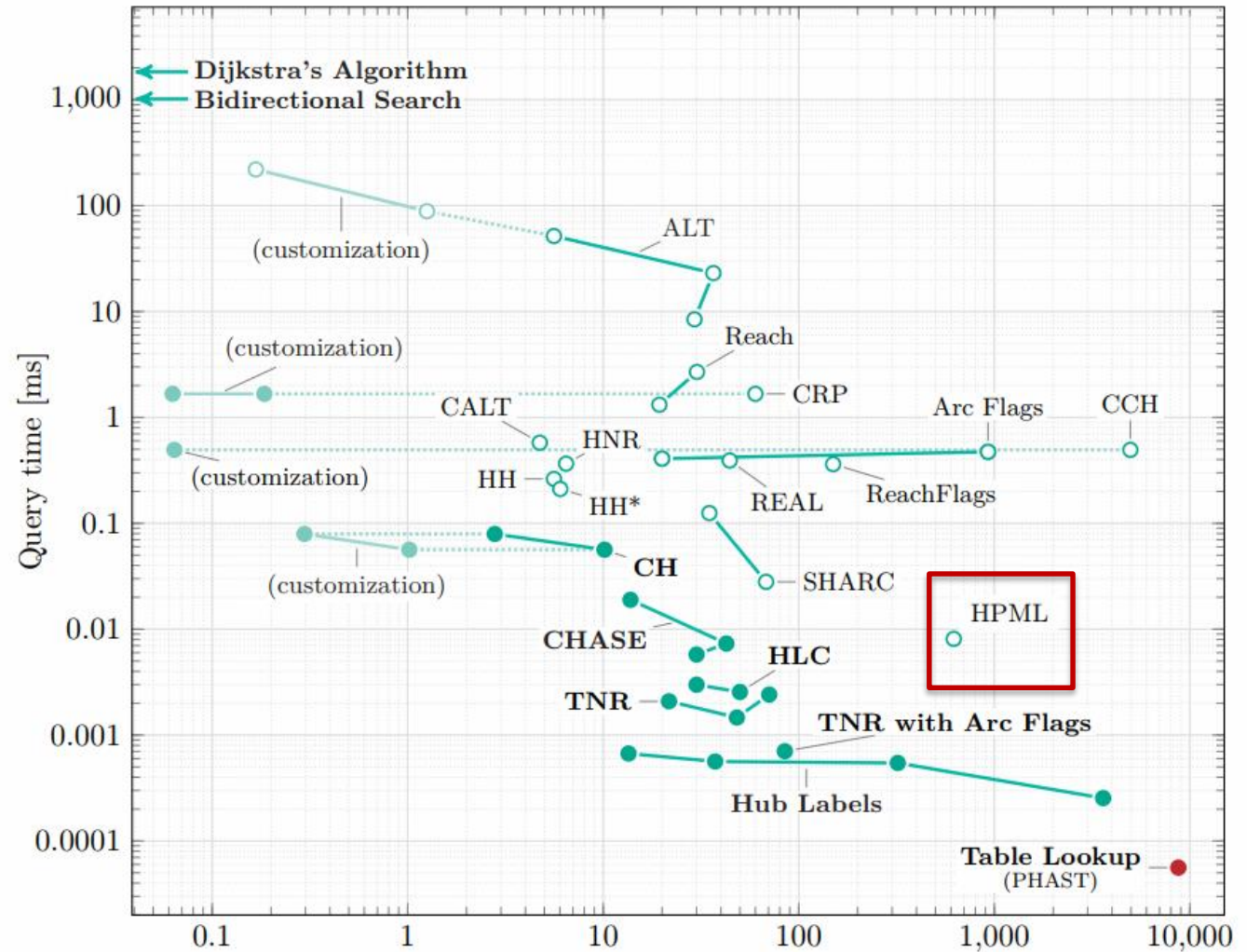
- ★ Dijkstras

- ⑩ Scale poorly!



# Mission Planner (Route Planning)

- ★ Massive-scale algorithms needed for routing
- ★ 18 million vertices, 42.5 million edges
  - ⑩ Partial Western Europe dataset



# Behavior Planner

## ★ Finite State Machines

- ⑩ Set of “states” and transition functions between them
- ⑩ Separate from configuration state

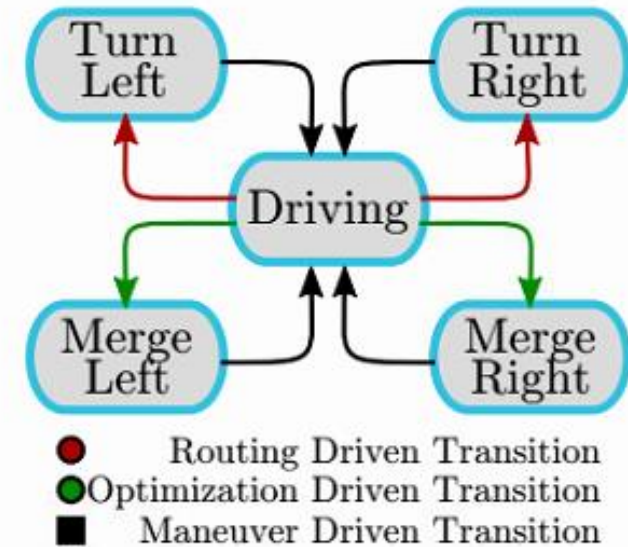
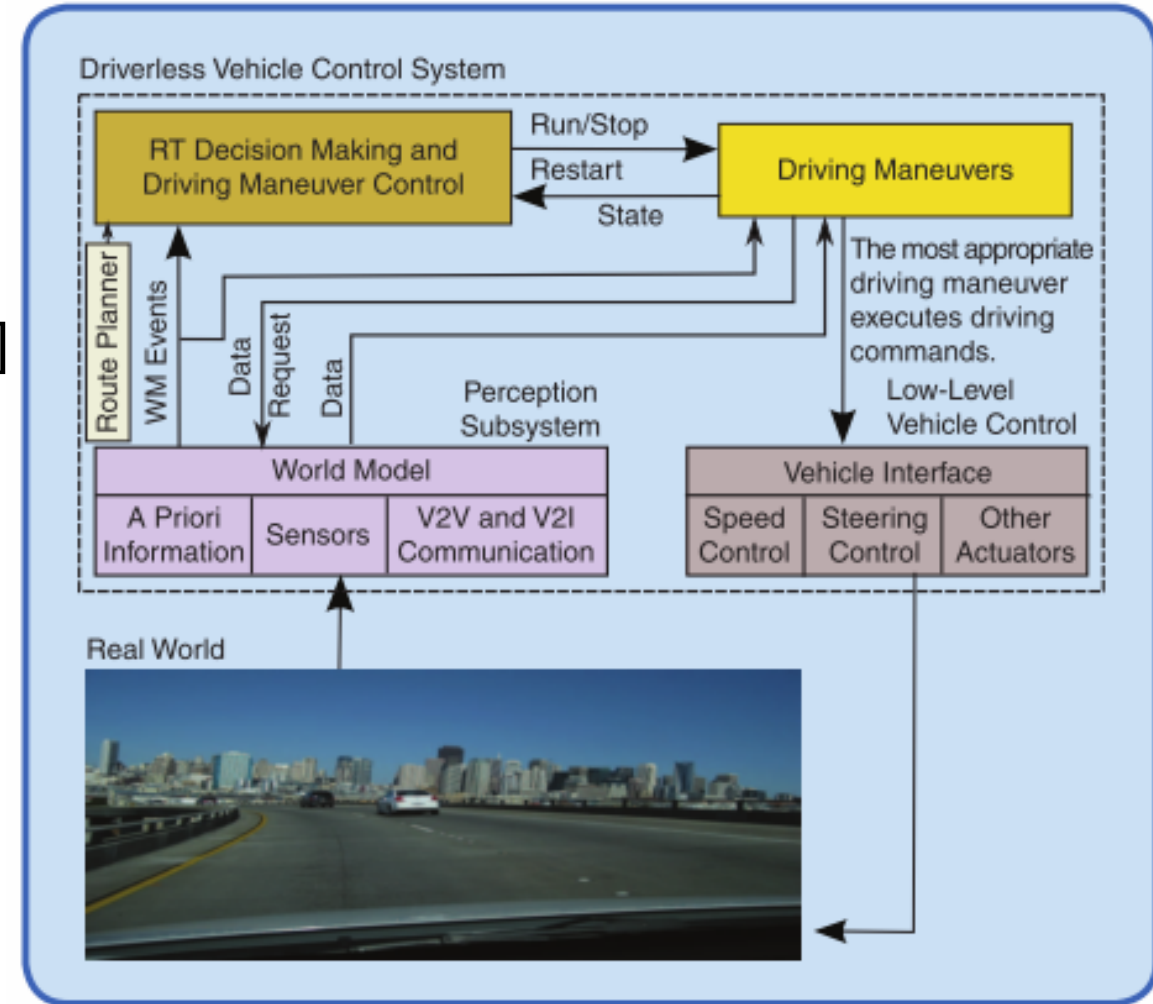
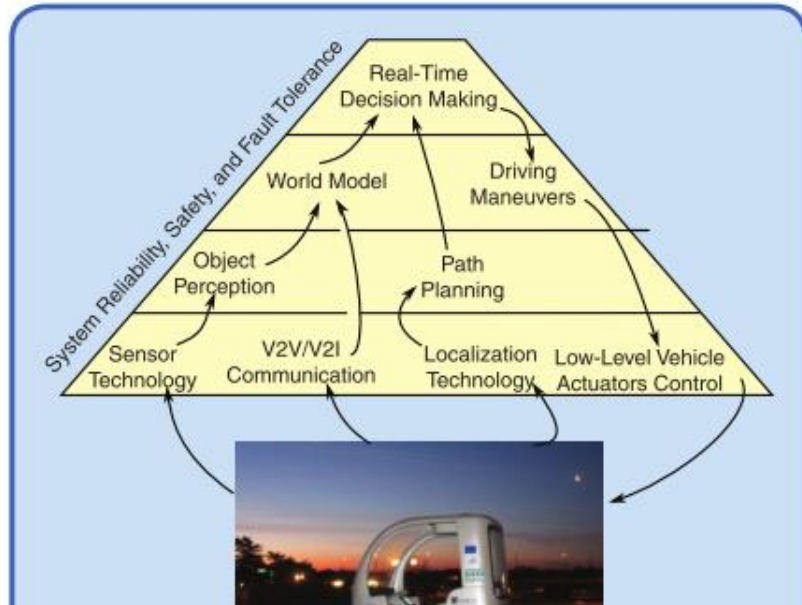


Fig. 2. **Finite State Machine:** We highlight different behavior states that are determined by the routing and optimization algorithms. When executing turns, the routing algorithm transitions the behavior state to a turning state. When the optimization-based maneuver algorithm plans a lane change, the behavior state is transitioned to merging.



# Behavior Planner

- ◆ FSMs limited in some cases
  - ⑩ What to do in unseen situations?
- ◆ Real-time decision making [Furda et al 2011]



# Motion Planner

★ Generally two stages:

- ⑩ Path planner - Computes the geometric representation of the path to be followed. I.e. the curve, spline, track, line, etc. we are following
- ⑩ Trajectory Planner / Path tracker - Computes the specific physical targets for following the path. I.e. velocity, acceleration, heading, steering, etc.



# Motion Planner

## ★ Basic overview

- ⑩ **Complete planning** - continuous plan in configuration space
  - ★ Exponential in dimensions of c-space (curse of dimensionality)
  - ★ "Complete"
- ⑩ Combinatorial Planning - discrete planning over an exact decomposition of the configuration space
- ⑩ Sample-Based planning:



# Motion Planner

## ★ Basic overview

⑩ Complete planning

⑩ **Combinatorial Planning** - discrete planning over an exact decomposition of the configuration space

★ Exponential in dimensions of c-space discretization (curse of dimensionality)

★ "resolution complete"

⑩ Sample-Based planning





# Motion Planner

## ★ Basic overview

⑩ Complete planning

⑩ Combinatorial Planning

⑩ **Sample-Based planning** - Sample in space to find controls / positions which are collision free and linked

★ Probabilistically complete

⑩ Some “probabilistically optimal”

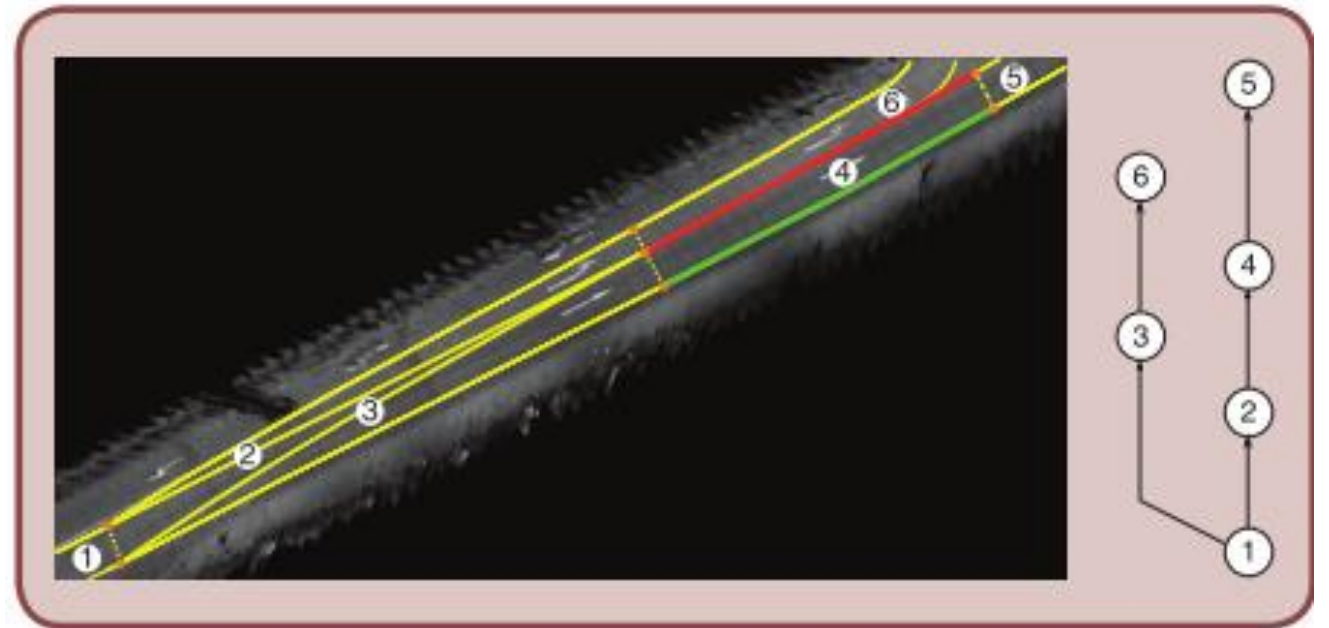
★ NOT exponential in configuration space



# Motion Planner: Combinatorial Planners

## ★ Driving Corridors:

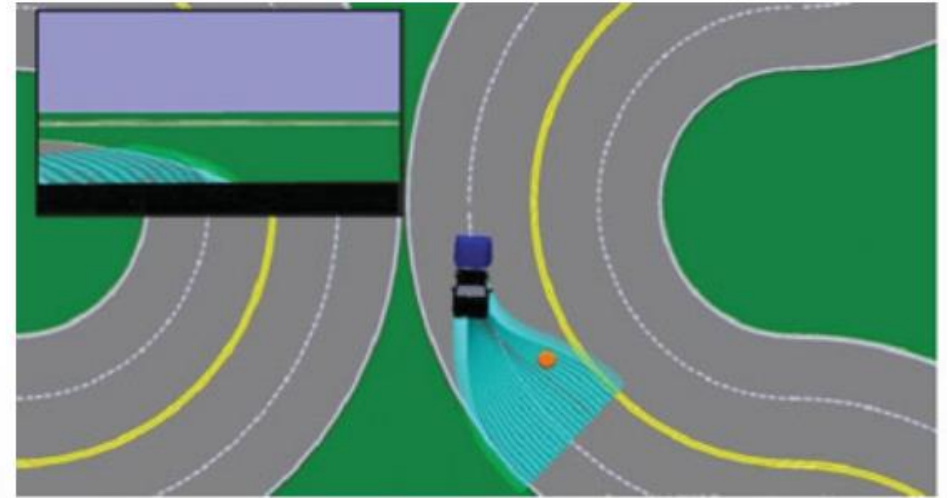
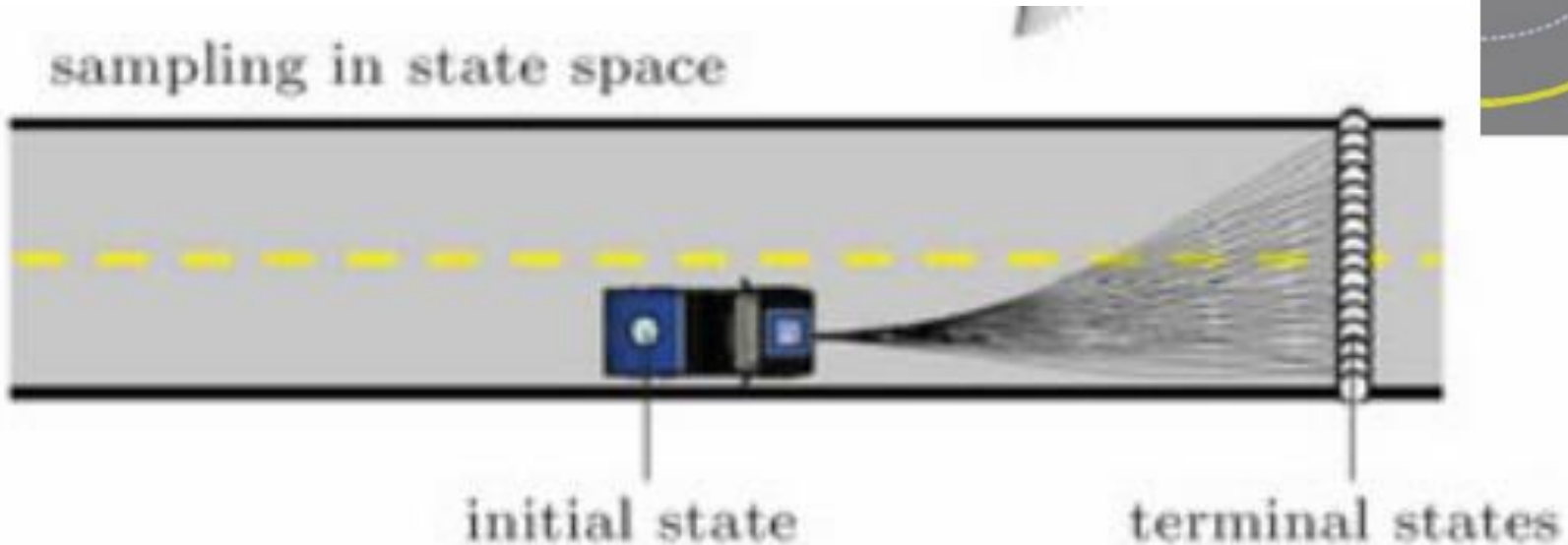
- ⑩ Decompose lanes into polygonal lanelets
- ⑩ Represent obstacles as polygonal bounding boxes or overlapping discs
- ⑩ Adjust lanelets to obstacle constraints



# Motion Planner: Combinatorial Planners

★ Darpa Urban Challenge:

⑩ BOSS: kinodynamic reachable set



# Maneuver Planner: Sample-based Planners

- ★ Sample-based Planning specifically for cars:
  - ⑩ Dynamics computation
  - ⑩ Inevitable collision states
  - ⑩ “Space-time planning approaches”
- ★ Pendleton: “Incorporating differential constraints into state-sampling planners is still a challenging matter, and requires a steering function to draw an optimal path between two given states which obeys control constraints (if such a path exists), as well as efficient querying methods to tell whether a sampled state is reachable from a potential parent state”



# Maneuver Planner: Sample-based Planners

## ★ RRT:

- ⑩ Given at-least one initial configuration in free-space and a goal configuration
  - ★ Sample a point  $p$  in configuration space, determine if it is collision free
  - ★ If so, find nearest node  $n$  to the point, move some  $\delta$  towards the point
  - ★ If  $n$  to  $n + \delta$  is CLEAR, connect to the tree



# Maneuver Planner: Sample-based Planners

## ★ State-lattice planners

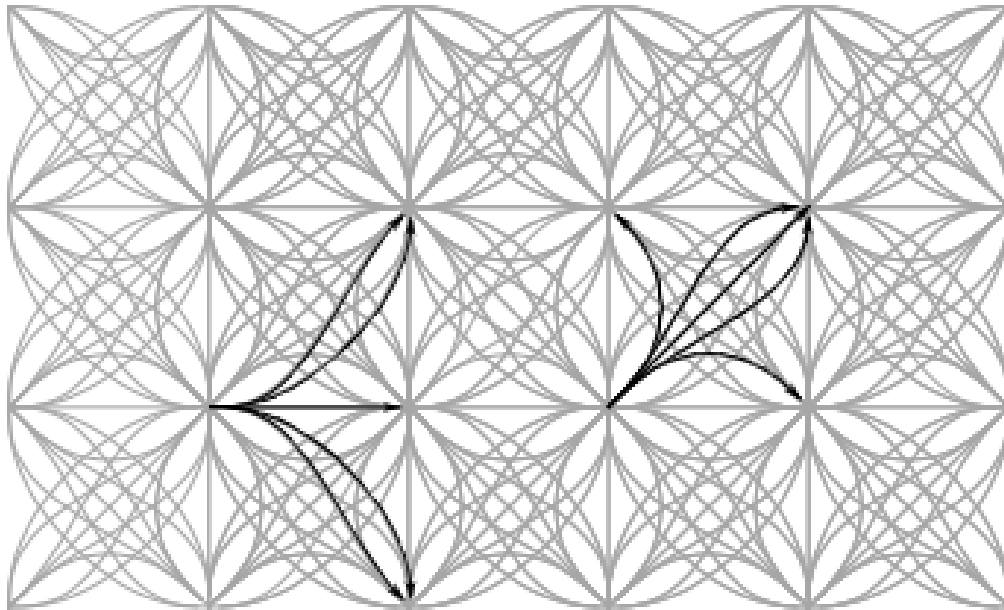
- ⑩ Generate set of potential future states through solving boundary-value problem
- ⑩ Generate connected “lattice” of potential future states expanding in time and space



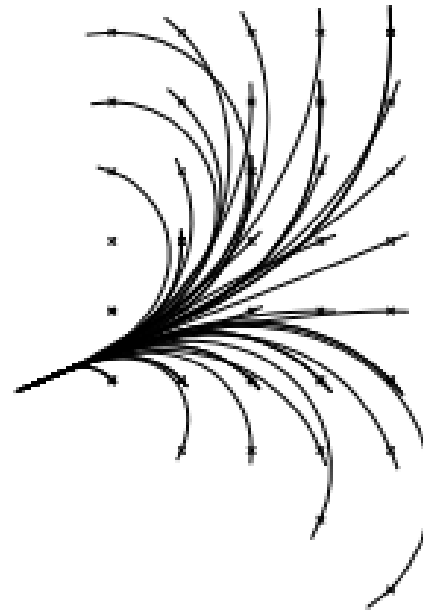
# Maneuver Planner: Sample-based Planners

## ★ State-lattice planners

### ⑩ Ex: Configurations in space



(a)



(b)

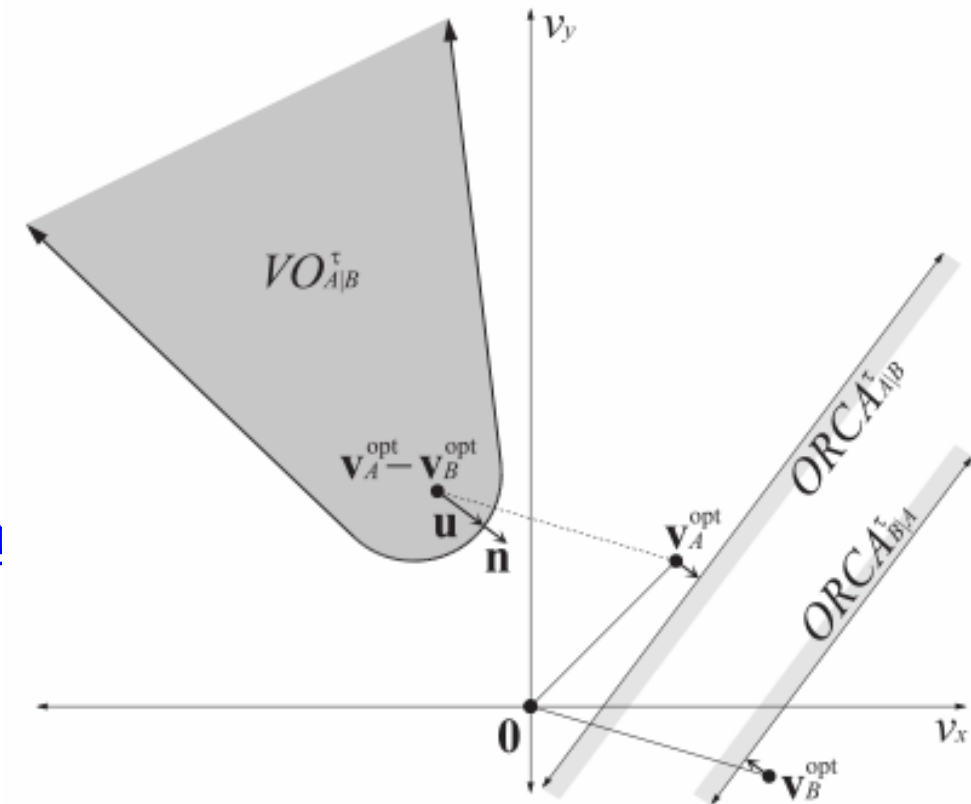


# Maneuver Planner: Obstacle Representation

## ★ RVOs: Reciprocal-velocity Obstacles

⑩ Constructs mutually exclusive velocity set choices for multiple robots

⑩ <https://youtu.be/1Fn3Mz6f5xA?t=1n24s>





# Structure

- ★ Recap
- ★ Control
  - ⑩ **Core concepts**
  - ⑩ PID
  - ⑩ MPC
- ★ Traffic-Sim
- ★ Prediction



# Autonomous Driving: Main Components

## ★ Control

- ⑩ Executing the planned maneuvers accounting for error / uncertainty
- ⑩ Commands sent to actuators

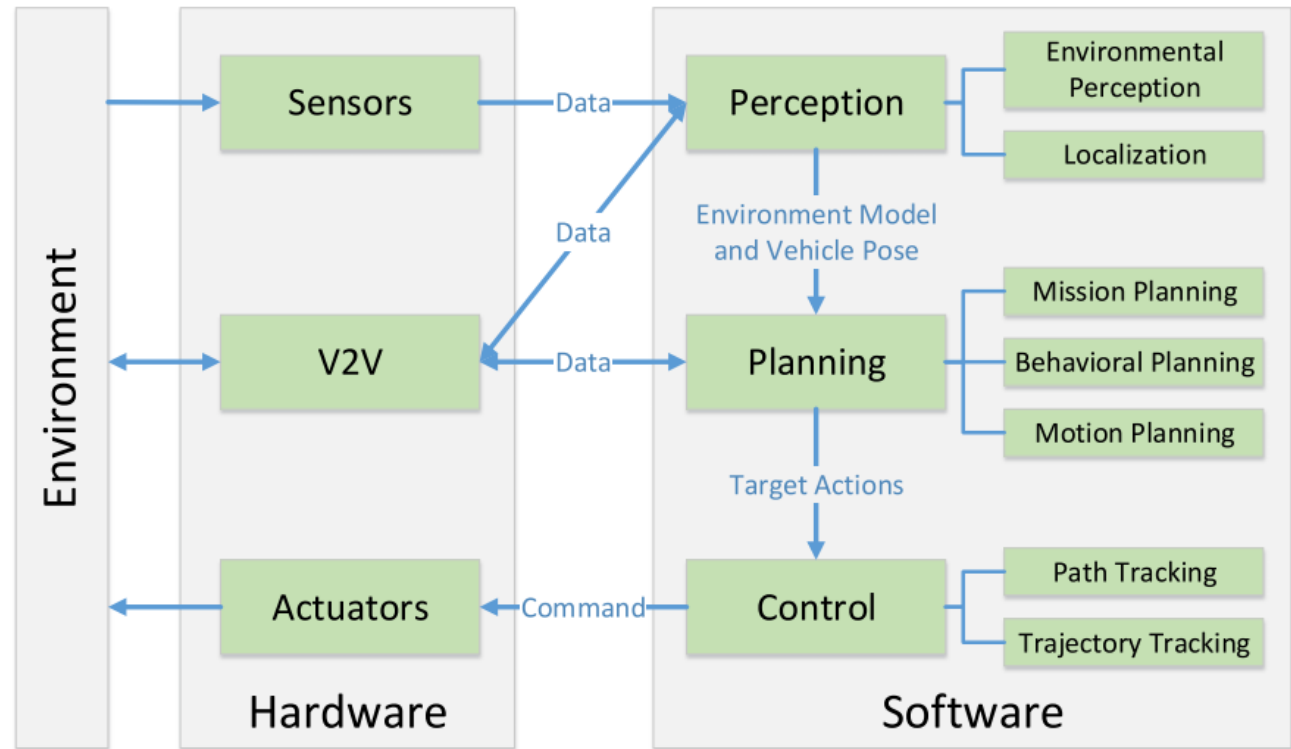


Figure 2. A typical autonomous vehicle system overview, highlighting core competencies.



# Control: Core Concepts

- ★ **Automatic control** in engineering and technology is a wide generic term covering the application of mechanisms to the operation and regulation of processes without continuous direct human intervention
  - ⑩ Open-loop control: Control input delivered independent of measurements
  - ⑩ Closed-loop control: Control input determined by system outputs



# Control: Core Concepts

## ★ Open-loop control examples

### ⑩ Timers:

- ★ Electronic timing switches
- ★ Clothes Dryer

### ⑩ Simple throttle (non-electronic)

- ★ Motorbikes, go-karts
- ★ Stove-top gas

### ⑩ Sinks / simple valves

- ★ Hot water / cold water



# Control: Core Concepts

## ★ Closed-loop control examples

### ⑩ Thermostat:

- ★ Engages air-conditioning depending on temperature

### ⑩ Oven:

- ★ Heating element controlled by temperature

### ⑩ Cruise-control:

- ★ Throttle controlled by current speed / acceleration

### ⑩ Used EXTENSIVELY in plant control (i.e. chemical, energy)



# Control: Core Concepts

- ✦ Process Variable (PV): The system output we wish to control
- ✦ Set Point (SP): Target value of the process Variable
- ✦ Control Output (CO): Output of the controller (input to the system)
- ✦ Error (E): Difference between SP and PV

<https://www.dataforth.com/introduction-to-pid-control.aspx>



# Control: Core Concepts

- ◆ Example: Water Plant Thermal Control
  - ⑩ Water kept at constant temperature by gas heater
  - ⑩ If level rises, gas reduced to stabilize
- ◆ PV: Temperature of water
- ◆ SP: Desired Temperature
- ◆ CO: Level of gas applied to burner

<https://www.dataforth.com/introduction-to-pid-control.aspx>

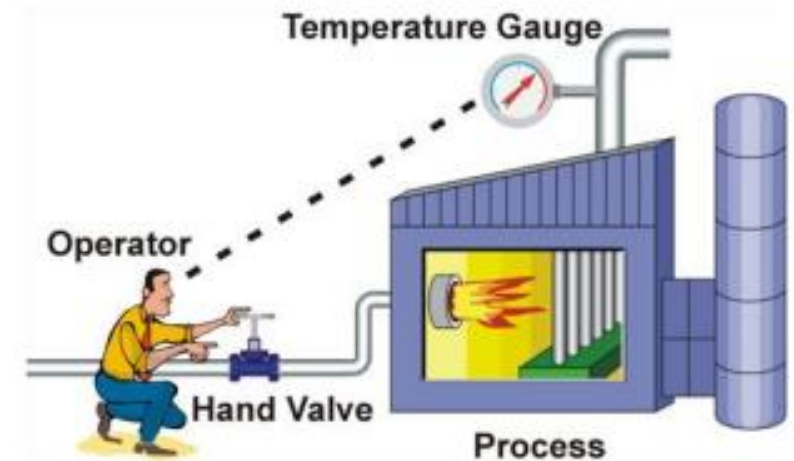


Figure 1  
An Operator Performing Manual Control



# Control: Core Concepts

✦ Can we replace the manual control with automatic controller?

✦

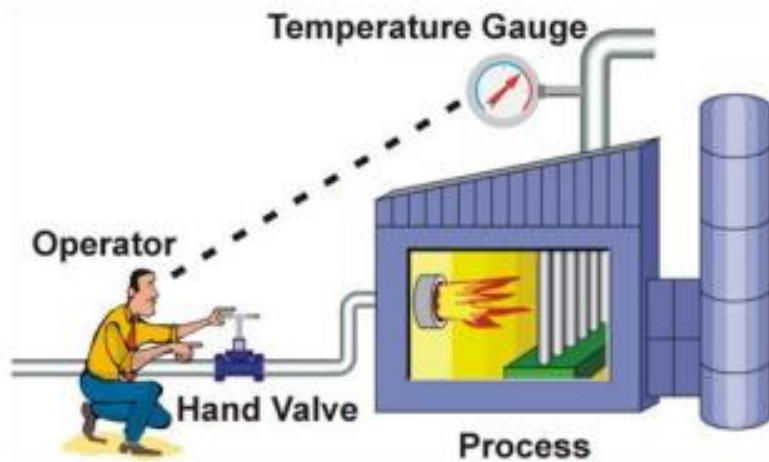


Figure 1  
An Operator Performing Manual Control

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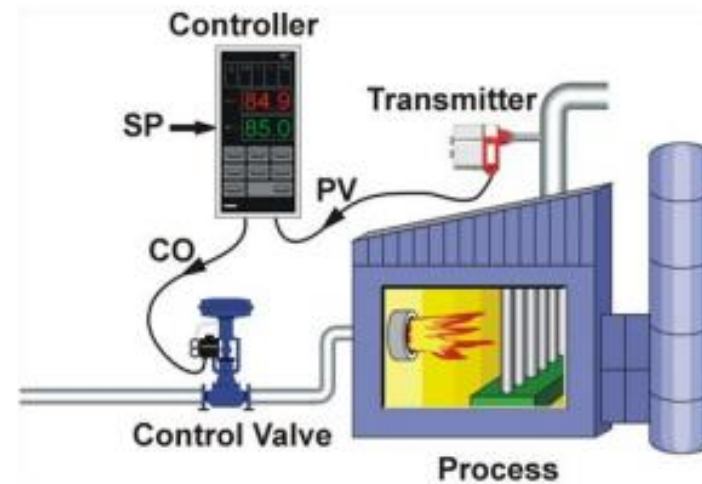


Figure 2  
A PID Controller Performing Automatic Control

✦ Of course, we can!





# Structure

- ★ Recap
- ★ Control
  - ⑩ Core concepts
  - ⑩ **PID**
  - ⑩ MPC
  - ⑩ Path Tracking
- ★ Traffic-Sim
- ★ Prediction



## Control: PID

- ★ **Proportional-Integral-Derivative** Controller: control loop feedback mechanism widely used in industrial control systems and a variety of other applications requiring continuously modulated control.
  - ⑩ Continuously calculates E, applies correction based on proportional, integral, and derivative terms (denoted P, I, and D respectively)
  - ⑩ Proportion (P): Current error, E (typically  $SP - PV$ )
  - ⑩ Integral (I): integral of E (sum of errors over time)
  - ⑩ Derivative (D): derivative of E (typically finite difference)



## Control: PID

- ★ **Proportional-Integral-Derivative** Controller: control loop feedback mechanism widely used in industrial control systems and a variety of other applications requiring continuously modulated control.

$$u(t) = K_p e(t) + K_i \int_0^t e(\tau) d\tau + K_d \frac{de(t)}{dt}$$



# Control: PID

- ✦ Proportion: Output controlled by error and Controller Gain ( $K_p$ )
- ✦ Control output proportional to error
  - ⑩ Choice of error function, but typically  $SP - PV$
- ✦ High gain: can cause oscillation
- ✦ Low gain: fails to correct to Set Point

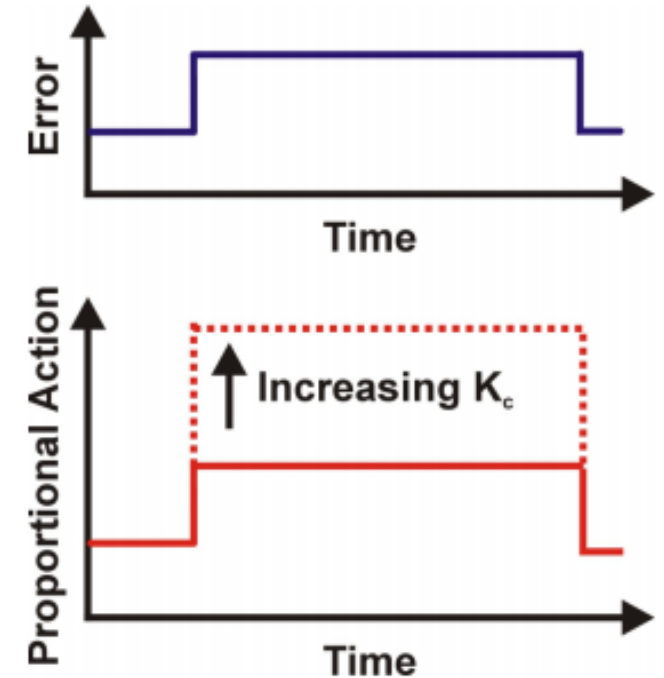
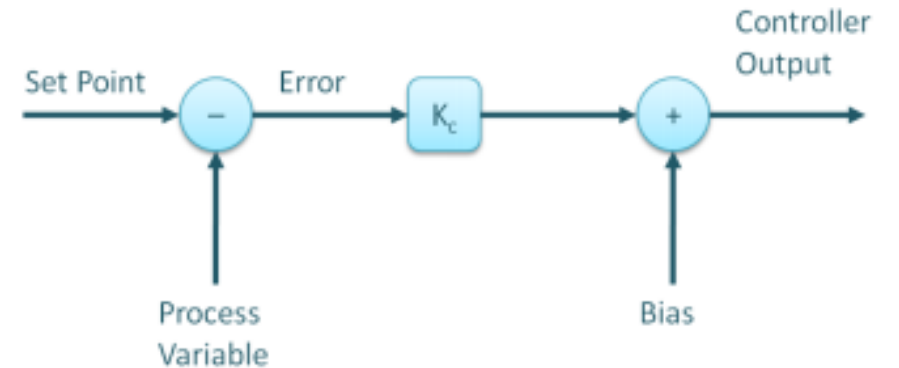


Figure 3  
Proportional Control Action



# Control: PID

- ✦ Proportion-only controller: Output controlled by error and Controller Gain ( $K_p$ )
- ✦ Control output proportional to error
  - ⑩ Choice of error function, but typically  $SP - PV$
- ✦ Add bias point for steady output at 0 error



**Figure 4**  
**A Proportional-Only Controller Algorithm**



# Control: PID

- ✦ P-only controller

  - ⑩ Bias controls steady output

- ✦ <https://sites.google.com/site/fpgaandco/pid>

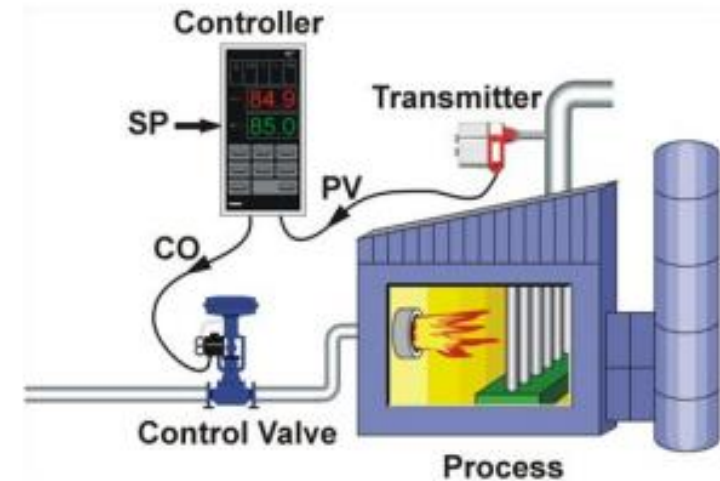


Figure 2  
A PID Controller Performing Automatic Control



# Control: PID

- ✦ Integral Control: Output term controlled by integral of error and Integral Gain ( $K_i$ )
- ✦ Corrects “steady-state” error
- ✦ Requires a “time” factor for integration ( $T_i$ )
- ✦ Longer time = less integral action

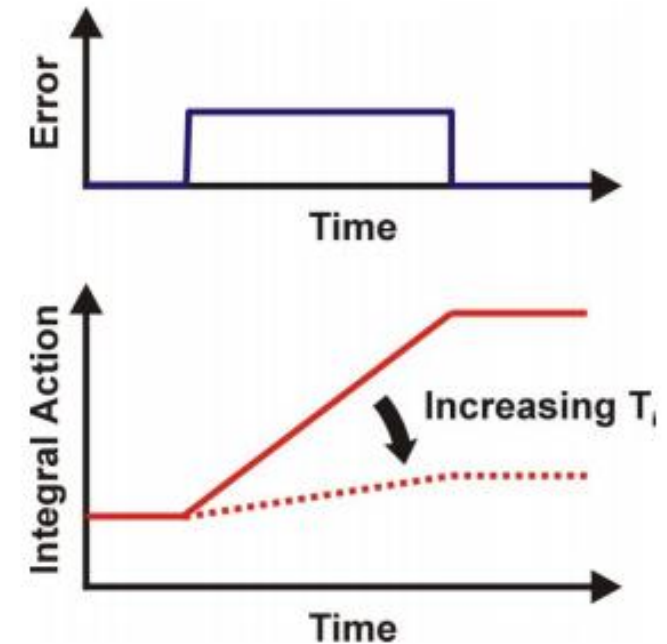
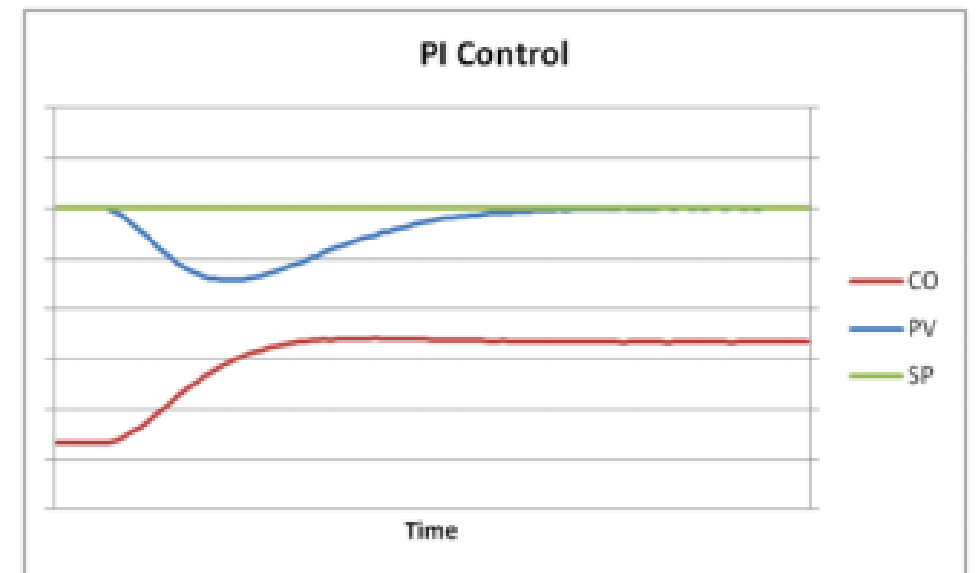


Figure 7  
Integral Control Action



# Control: PID

- ✦ PI Controller: Proportion and integral terms
- ✦ Corrects steady-state error, converges rather than oscillates



**Figure 9**  
**A PI Controller's Response to a Disturbance**





# Control: PID

- ◆ Derivative: Output term controlled by derivative of error and Derivative Gain ( $K_d$ )
- ◆ Assists in rapid response to disturbance
- ◆ Requires time parameter to operate

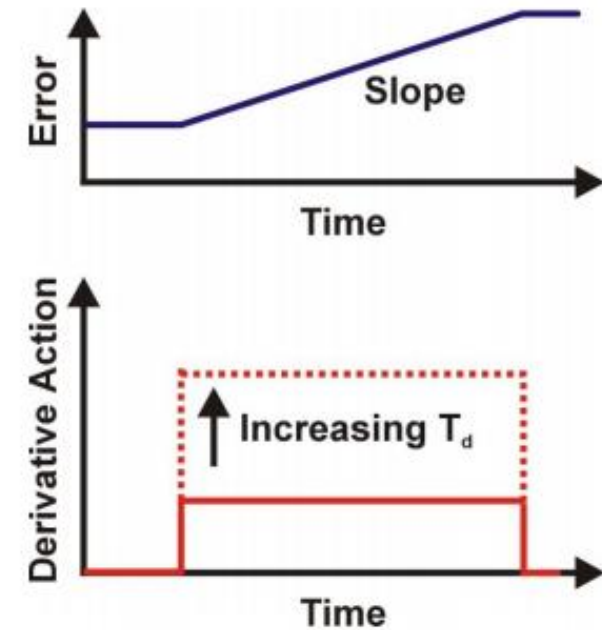
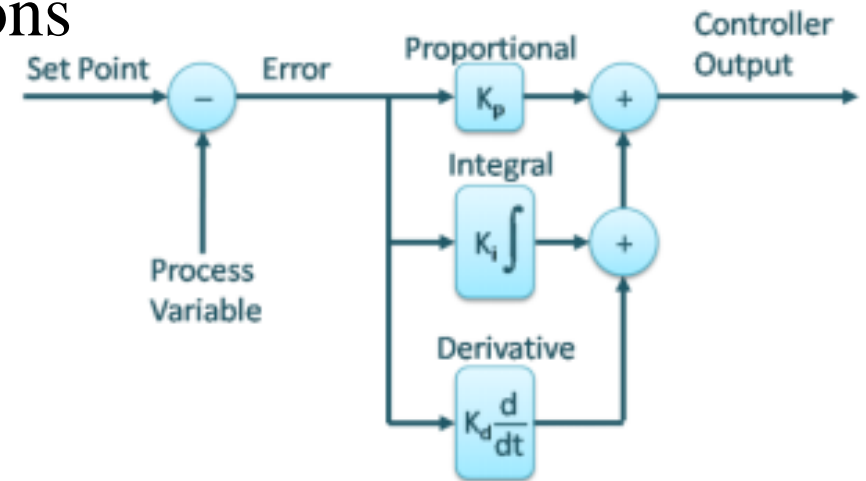


Figure 10  
Derivative Control Action



# Control: PID

- ★ PID Controller: Proportion, Integral, Derivative terms
- ★ Complete closed-loop controller
  - ⑩ Used in AutoVi and countless applications



**Figure 12**  
**The Parallel PID Controller Algorithm**



# Control: PID Tuning

## ★ Rules of thumb for tuning a PID controller:

★ [https://upload.wikimedia.org/wikipedia/commons/3/33/PID\\_Compensation\\_Animated.gif](https://upload.wikimedia.org/wikipedia/commons/3/33/PID_Compensation_Animated.gif)

### Effects of increasing a parameter independently<sup>[20][21]</sup>

Parameter	Rise time	Overshoot	Settling time	Steady-state error	Stability
$K_p$	Decrease	Increase	Small change	Decrease	Degrade
$K_i$	Decrease	Increase	Increase	Eliminate	Degrade
$K_d$	Minor change	Decrease	Decrease	No effect in theory	Improve if $K_d$ small



# Control: PID Tuning

## ★ Ziegler–Nichols Tuning

⑩ Tune  $K_p$  until the control loop begins to oscillate

★ Called Ultimate control point ( $K_u$ )

⑩  $K_u$  and oscillation period  $T_u$  used to tune parameters as follows

**Ziegler–Nichols method**

Control Type	$K_p$	$K_i$	$K_d$
<i>P</i>	$0.50K_u$	—	—
<i>PI</i>	$0.45K_u$	$0.54K_u/T_u$	—
<i>PID</i>	$0.60K_u$	$1.2K_u/T_u$	$3K_uT_u/40$



# Control: PID Examples

## ★ More examples of PID:

- ⑩ Cruise-control

- ⑩ Quad-rotor Autopilot

- ⑩ Mobile robot control

  - ★ PID for steering + PID for speed

- ⑩ Spaceships

- ⑩ ...

- ⑩ ...

- ⑩ Innumerable examples of PID control



# Control: PID Examples

## ★ PID for QuadRotor

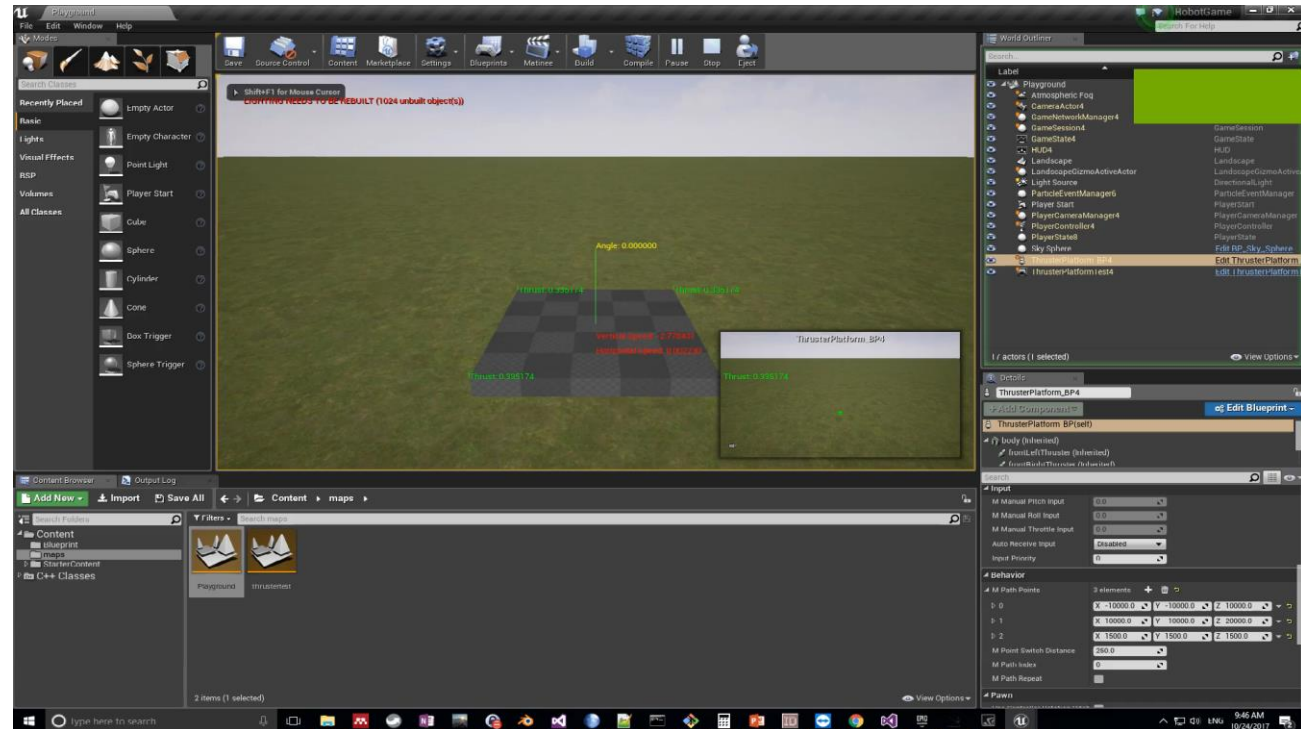
⑩ Pure pursuit

⑩ Target speed specified

⑩ 2 layer PID

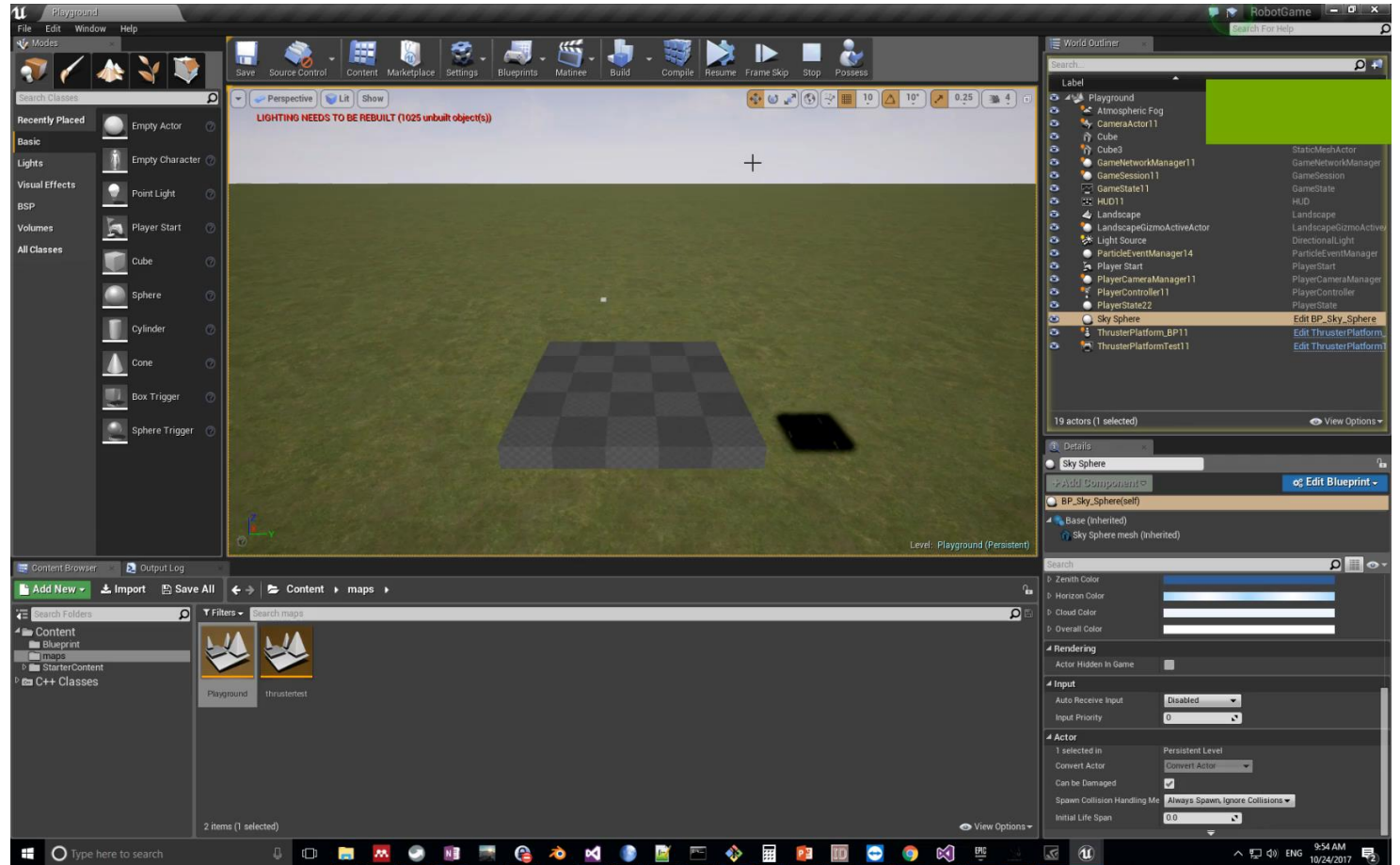
★ 1. Mix rotors for vertical speed

★ 2. Mix rotors for horizontal speed



# Control: PID Examples

- ★ PID for QuadRotor
- ⑩ Robust to perturbation



# Structure

- ★ Recap
- ★ Control
  - ⑩ Core concepts
  - ⑩ PID
  - ⑩ **MPC**
  - ⑩ Path Tracing
- ★ Traffic-Sim
- ★ Prediction





# Control: MPC

- ★ **Model-Predictive** Controller: control loop relying on an underlying system model to generate feed-forward control
  - ⑩ Augment feedback control system to generate predicted future values and predicted control outputs
  - ⑩ Non-linear systems typically linearized over small timescales of MPC
  - ⑩ <https://www.youtube.com/watch?v=oMUtYZOgsng>
    - ★ Very good introduction
  - ⑩ <https://www.youtube.com/watch?v=DFqOf5wbQtc>
    - ★ Lecture series is helpful for MPC



# Control: MPC

- ★ MPC is very useful when process model is available
  - ⑩ Reduces overshoot substantially
  - ⑩ Using cached table of input responses, optimization can be done quickly
- ★ MPC uses in automotive context:
  - ⑩ Traction control [Borelli 2006]
  - ⑩ Braking control [Falcone 2007]
  - ⑩ Steering [Falcone 2007]
  - ⑩ Lane-keeping [Liu 2015]



# Structure

- ★ Recap
- ★ Control
  - ⑩ Core concepts
  - ⑩ PID
  - ⑩ MPC
  - ⑩ **Path Tracking**
- ★ Traffic-Sim
- ★ Prediction



# Control: Path tracking with controllers

- ★ Given a path computed by the motion planner, we use controls to follow or “achieve” the path
- ★ Many methods for path tracking:
  - ⑩ Pure-pursuit
  - ⑩ AutonoVi (Arcs)
  - ⑩ Kinematic Bicycle
  - ⑩ Model-Predictive Control



# Control: Path tracking with controllers

## ★ Pure-pursuit

⑩ Given a geometric path, track a point ahead of the vehicle according to a fixed lookahead (can be a function of speed)

⑩ <https://www.youtube.com/watch?v=qG70QJJ8Qz8>

⑩ <https://www.youtube.com/watch?v=vlyTthJugRQ>

★ Advantages: simple, robust to perturbation

★ Disadvantages: Corner-cutting, oscillation for non-holonomic robots



# Control: Path tracking with controllers

## ★ AutonoVi

- ⑩ 2<sup>nd</sup> order pure-pursuit PID

- ⑩ Vehicle position + 2 points ahead on center of lane, trace arc between them

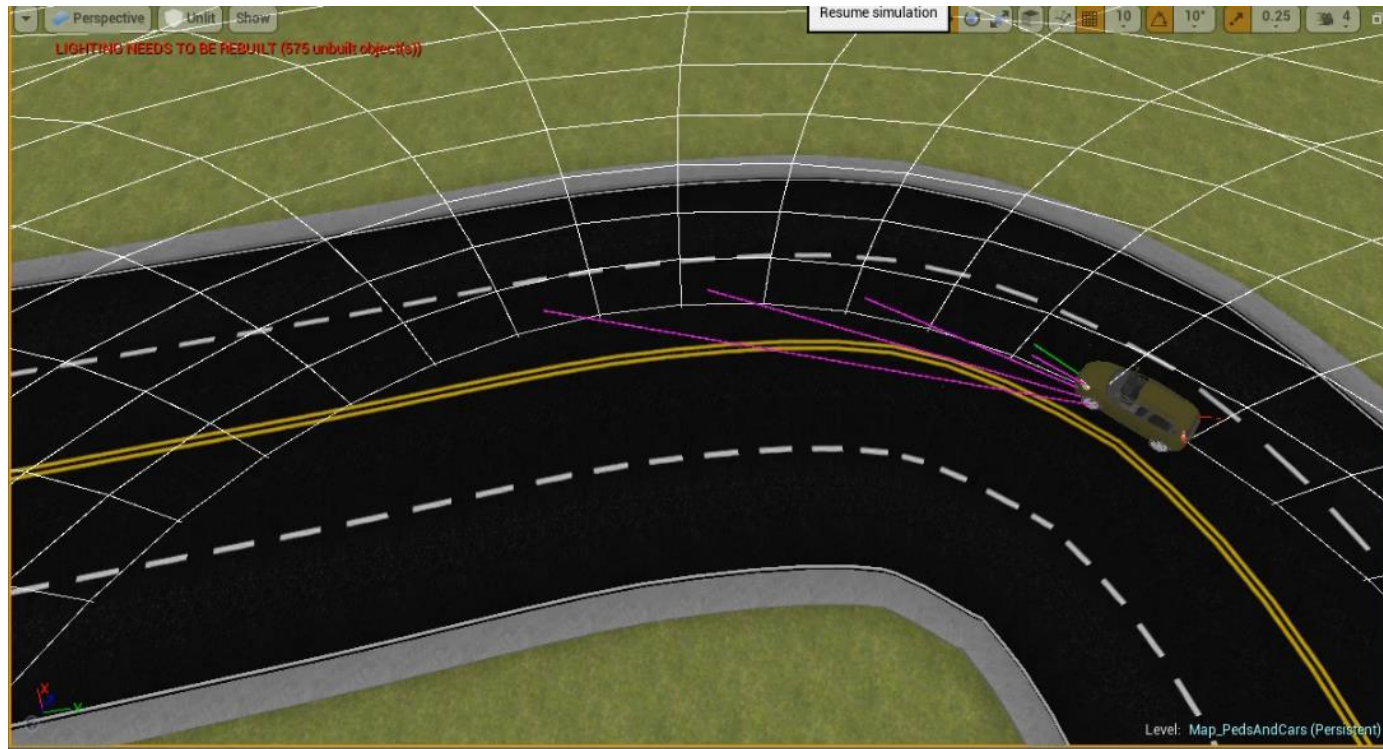
- ★ Advantages: simple, robust to perturbation, can represent kinematic limits in computed curves

- ★ Disadvantages: oscillation, prone to wide-turns, curvature prone to large shifts



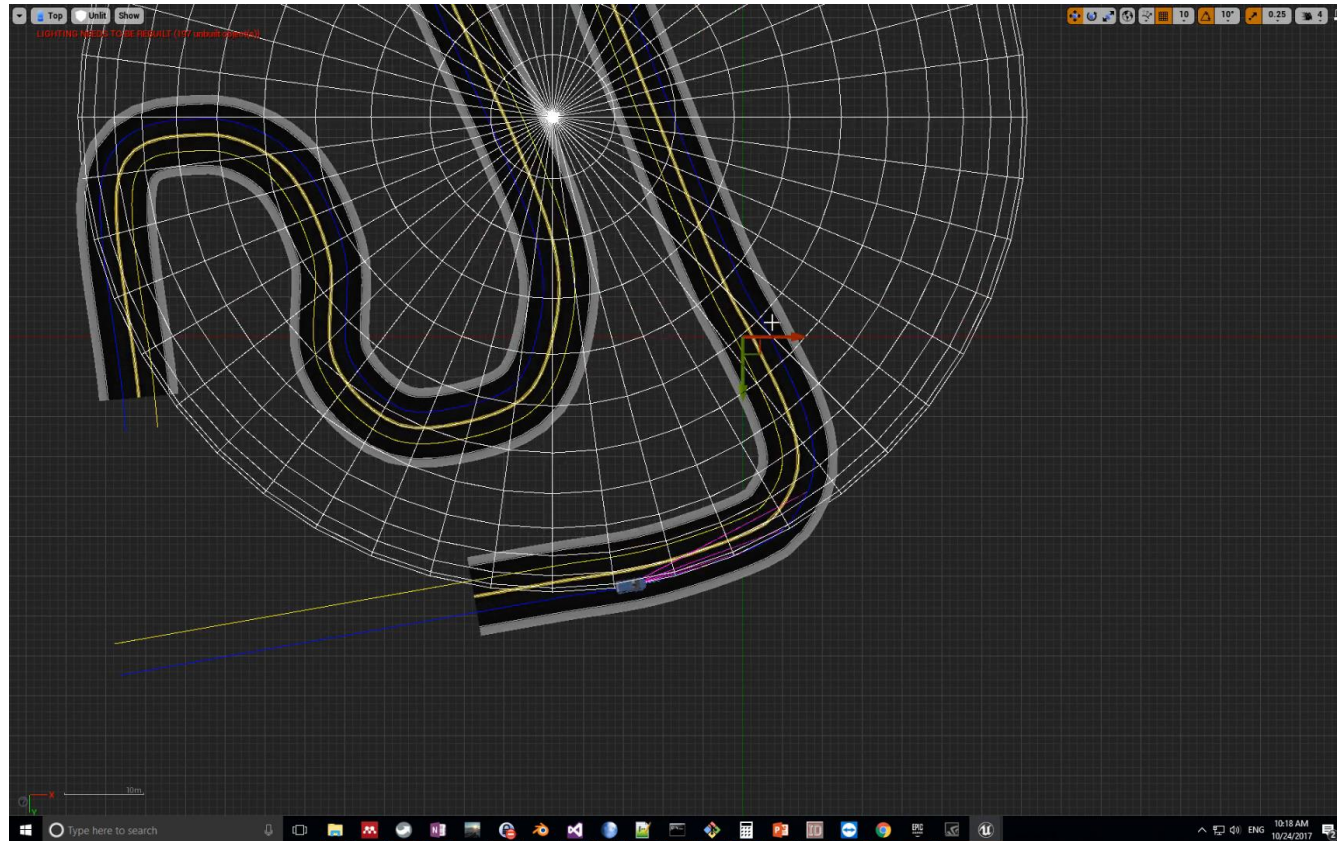
# Control: Path tracking with controllers

## ★ AutonoVi



# Control: Path tracking with controllers

## ✦ AutonoVi





# Control: Path tracking with controllers

## ★ AutonoVi

- ⑩ NOTE: controllers have been demonstrated using arbitrary degree polynomials from  $N$  points on the path
  - ★ Trade-offs in computational speed, robustness to perturbation, look-ahead computation



# Control: Path tracking with controllers

## ★ Kinematic Car [De Luca 1998]

- ⑩ Attempts to simultaneously minimize heading error and cross-track error (distance to reference point on path)
- ⑩ Heading measured as path tangent orientation

$$\begin{aligned}\theta_e &= \theta - \theta_p(s) \\ \dot{s} &= v \cos(\theta_e) + \dot{\theta}_p e_{ra} \\ e_{ra} &= v \sin(\theta_e)\end{aligned}$$

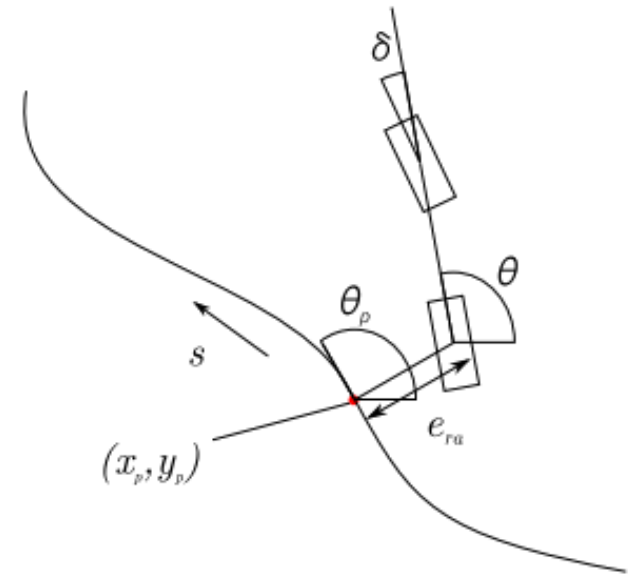


Figure 9. Path representation for kinematic car model



# Control: Path tracking with controllers

## ◆ Kinematic Car [De Luca 1998]

### ⑩ Rewrite kinematics in “path coordinates”

$$\begin{bmatrix} \dot{s} \\ \dot{e}_{ra} \\ \dot{\theta}_e \\ \dot{\delta} \end{bmatrix} = \begin{bmatrix} \frac{\cos(\theta_e)}{1 - \dot{e}_{ra}\kappa(s)} \\ \sin(\theta_e) \\ \left(\frac{\tan\delta}{L}\right) - \frac{\kappa(s)\cos(\theta_e)}{1 - \dot{e}_{ra}\kappa(s)} \\ 0 \end{bmatrix} v \begin{bmatrix} 0 \\ 0 \\ 0 \\ 1 \end{bmatrix} \dot{\delta}$$

### ⑩ Goal becomes maximizing $\dot{s}$ while minimizing $\dot{e}_{ra}$ and $\dot{\theta}_e$

De Luca, A., Oriolo, G., & Samson, C. (1998). Feedback control of a nonholonomic car-like robot, 171–253. <http://doi.org/10.1007/BFb0036073>

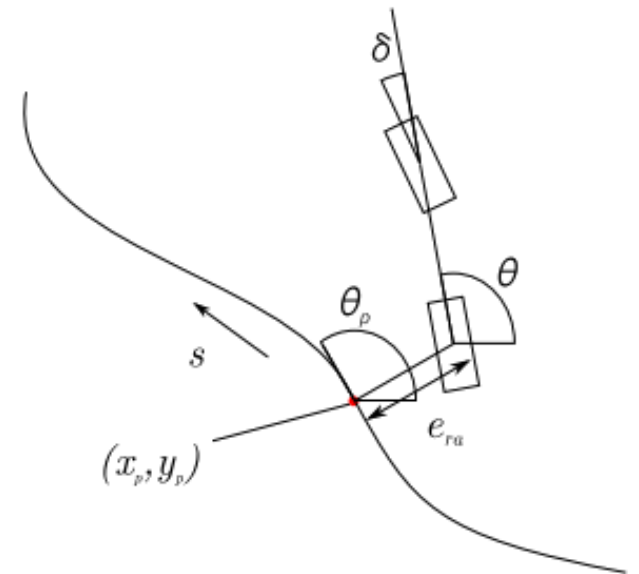


Figure 9. Path representation for kinematic car model

# Control: Path tracking with controllers

- ★ Model-predictive

- ⑩ Given a model, i.e. kinematic car, perform repeated optimization over future states to determine optimal control

- ★ Advantages:

- ⑩ Robust to disturbance, reduces oversteer, requires model

- ★ Disadvantages:

- ⑩ Computationally expensive, model mismatch exacerbates errors

- ★ In my experience: a bad model in MPC performs worse than PID!



# Control: Path tracking with controllers

## ★ Model-predictive

⑩ Examples:

⑩ <https://youtu.be/Bk7ES3Qd53s>

⑩ <https://youtu.be/C5UILYChPAc>

⑩ <https://youtu.be/5-hvtxeZNbo>

⑩ Code at: <https://github.com/parilo/CarND-MPC-Project>



# Structure

- ★ Recap
- ★ Control
- ★ Traffic-Sim
  - ⑩ MATSim
  - ⑩ Sumo
  - ⑩ Hybrid Simulation
- ★ Prediction



# Traffic-Sim: Rationale

## ★ Understand infrastructure

- ⑩ Evaluate efficiency of proposed changes to roads
- ⑩ Evaluate congestion points, failures, and improvements for existing roads
- ⑩ Test traffic control algorithms



# Traffic-Sim: Methods

## ★ Agent-based:

⑩ Macroscopic: agents represented without physics or kinematics

★ Roads treated as edges in directed graph

★ Many agents supported, limited interactions

⑩ Microscopic: agents represented with kinematics or physics

★ Roads modelled with physical dimensions

★ Few agents supported, interactions can be modelled dynamically





# Traffic-Sim: Methods

## ✦ Flow-based:

- ⑩ Agents not explicitly represented
- ⑩ Flow computed over network, system evolves as “fluid” simulation



# Structure

- ★ Recap
- ★ Control
- ★ Traffic-Sim
  - ⑩ MATSim
  - ⑩ Sumo
  - ⑩ Hybrid Simulation
- ★ Prediction



# Traffic-Sim: MATSim

- ★ Agent-based, Macroscopic simulation

- ★ Supports millions of vehicles

- ★ <https://vimeo.com/124704874>

- ★ <https://youtu.be/VowP4f9ntCA?t=42s>

- ★ <https://youtu.be/VowP4f9ntCA?t=5m28s>

- ★ [https://youtu.be/o60A4r6sSsE?list=PLLGIZCXnKbU6-9vy\\_rKZ6gW7E\\_ra42hfX](https://youtu.be/o60A4r6sSsE?list=PLLGIZCXnKbU6-9vy_rKZ6gW7E_ra42hfX)



# Traffic-Sim: MATSim

## ★ Features:

- ⑩ Millions of agents
- ⑩ Route import from loop detectors / traffic data
- ⑩ OpenStreetmap Import

## ★ Benefits:

- ⑩ Macro-scale modelling replicates usage data gathered over long periods
- ⑩ Simulation of alternate routes and large time-scales simply
- ⑩ Evaluate macro changes: for example, starting school 30m later



# Structure

- ★ Recap
- ★ Control
- ★ Traffic-Sim
  - ⑩ MATSim
  - ⑩ **SUMO**
  - ⑩ Hybrid Simulation
- ★ Prediction



# Traffic-Sim: SUMO

- ★ Agent-based, Microscopic simulation
- ★ Allows for modeling lane configuration, route-planning, vehicle size and shapes, preliminary pedestrians
- ★ Online control and modification of network
- ★ [https://youtu.be/KgPSREMmA\\_0](https://youtu.be/KgPSREMmA_0)
- ★ <https://youtu.be/a52U6CQQRcw?t=24s>
- ★ <https://youtu.be/qewufs0Xsq0>



# Traffic-Sim: SUMO

## ★ Notable Features:

- ⑩ OpenStreetmap Import, automatic processing of lane connectivity
- ⑩ Control and physics free
- ⑩ Multiple driver models, “person level” transport options

## ★ Benefits:

- ⑩ Allows detailed testing of traffic-lights and intersections
- ⑩ Widely used for V2X communication research



# Structure

- ★ Recap
- ★ Control
- ★ Traffic-Sim
  - ⑩ MATSim
  - ⑩ SUMO
  - ⑩ **Hybrid Simulation**
- ★ Prediction





# Traffic-Sim: Hybrid & Flow Models

## ★ Non-agent based models

- ⑩ Treat traffic as flow model, like liquid
- ⑩ Continuum formulation evolves road network
- ⑩ Allows for immense networks, but limits the ability to represent agentive phenomena



## Traffic-Sim: Hybrid & Flow Models

# Continuum Traffic Simulation

Jason Sewall  
David Wilkie  
Paul Merrell  
Ming Lin



# Traffic-Sim: Hybrid & Flow Models

## ★ Hybrid models

### ⑩ “Best of both worlds”

★ continuum evolution for “distant” traffic phenomena

★ Agent-based simulation for nearby vehicles

### ⑩ Captures driver behavior in micro-scale and accurately models aggregate information

⑩ <https://www.youtube.com/watch?v=eEnGFxfN2tE>

⑩ see me after class for more papers



# Structure

- ★ Recap
- ★ Control
- ★ Traffic-Sim
  - ⑩ MATSim
  - ⑩ SUMO
  - ⑩ Hybrid Simulation
- ★ Prediction



# Traffic-Sim: Recent Applications

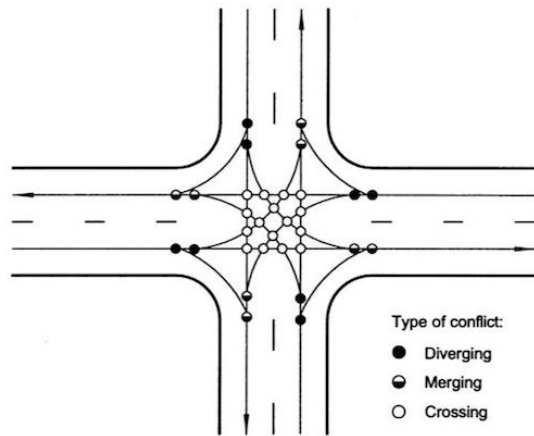
[https://www.citylab.com/solutions/2013/01/could-these-crazy-intersections-make-us-safer/4467/?utm\\_source=SFFB](https://www.citylab.com/solutions/2013/01/could-these-crazy-intersections-make-us-safer/4467/?utm_source=SFFB)

good article

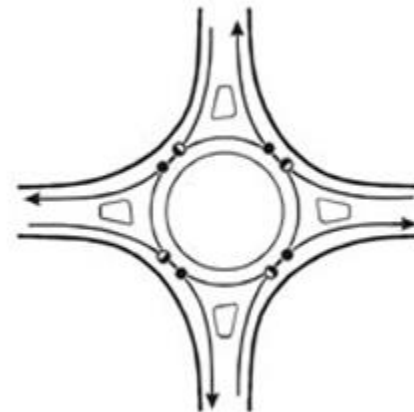
## ★ Safer intersections:

⑩ Geometric analysis performed to determine intersection danger

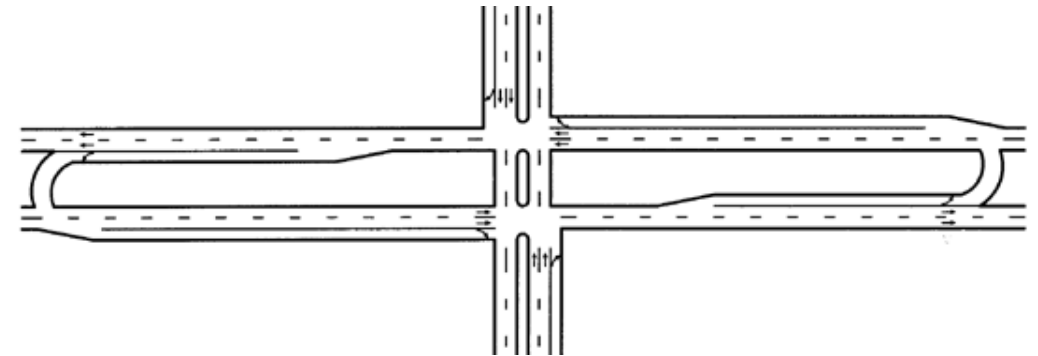
⑩ Design intersections which optimize flow & limit intersection points



32 collision points



8 collision points



18 collision points?

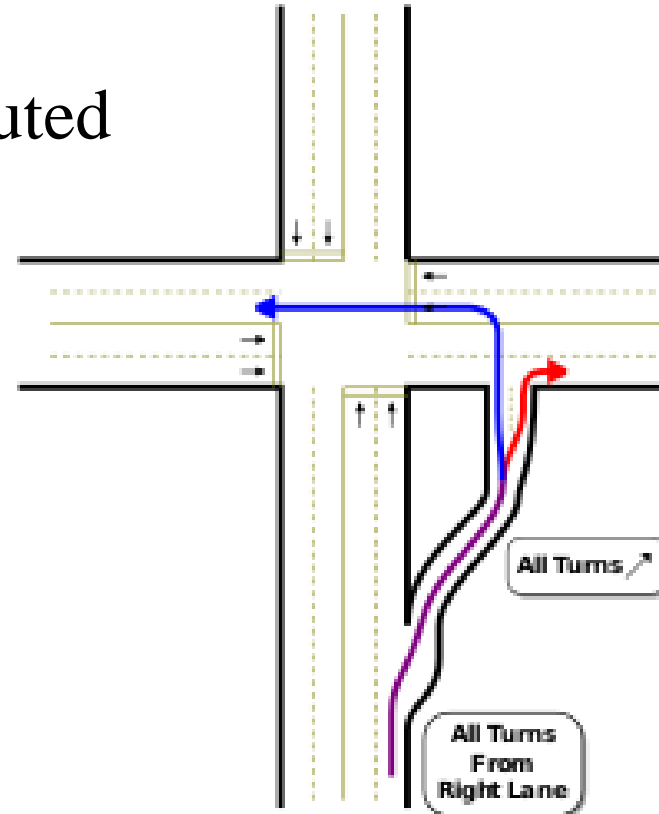


# Traffic-Sim: Recent Applications

## ✦ Jughandle:

⑩ Turns from minor road executed at special “handle”

⑩ <https://vimeo.com/58011852>

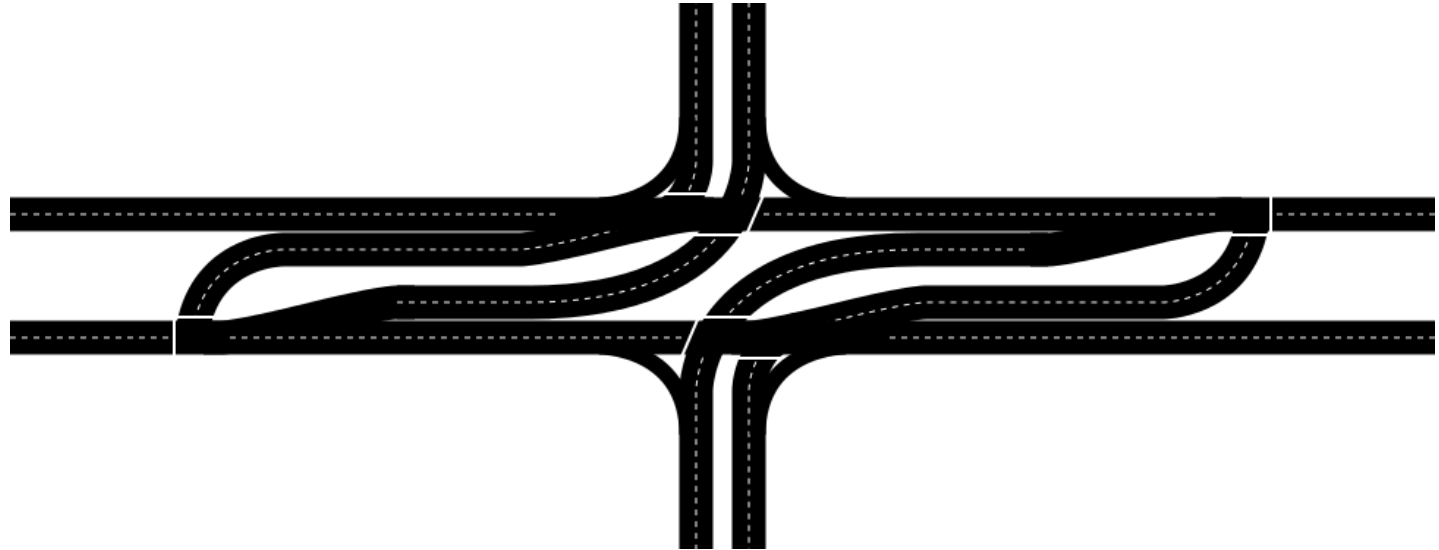


# Traffic-Sim: Recent Applications

## ★ Superstreet:

⑩ Minor road NOT ALLOWED  
to cross major road

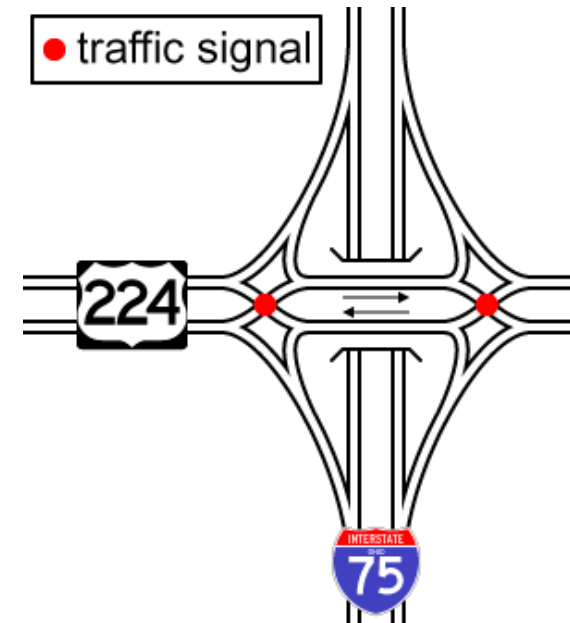
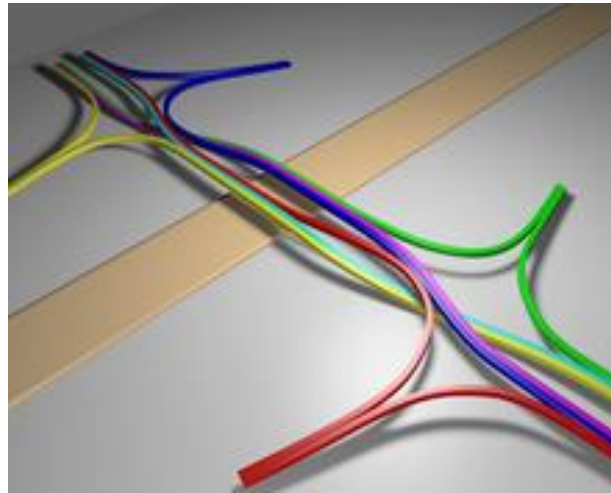
⑩ <https://vimeo.com/57973069>



# Traffic-Sim: Recent Applications

## ★ Diverging Diamond:

- ⑩ Minor road crosses in X pattern
- ⑩ Allows continuous flow in 2 directions
- ⑩ <https://vimeo.com/57972903>





# Traffic-Sim: Recent Applications

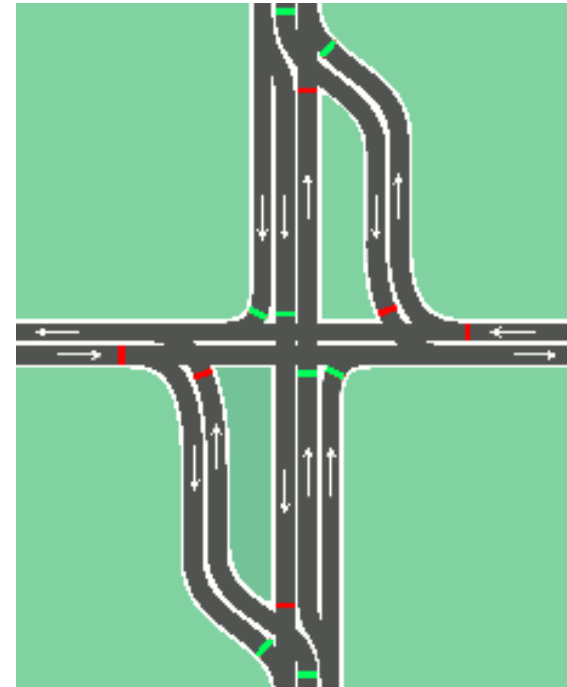
## ★ Continuous Flow:

⑩ Left turns pre-cross oncoming lanes

⑩ I grew up with one of these

⑩ <https://vimeo.com/57973241>

⑩ <https://vimeo.com/57973040>



# Traffic-Sim: Recent Applications

- ★ What should traffic lights look like for AVs?
  - ⑩ Are they needed at all?
  - ⑩ How do we optimize for mixed AV and non-AV traffic?
    - ⑩ <https://vimeo.com/37751380>
- ★ Great resources at <https://goo.gl/3YUY2o>



# Structure

- ★ Recap
- ★ Control
- ★ Traffic-Sim
- ★ **Prediction**



# Limitations in Planning

## ★ Most autonomous navigation algorithms

- ⑩ Defensive

- ⑩ Opaque

- ⑩ Do not consider “interactions” with other participants

- ⑩ Assume a very simple model for estimating movement of other cars

## ★ Drivers have a tendency to rear end self-driving cars on the road [ Consumer Affairs]

- ⑩ 19 such crashes out of 285 Waymo vehicles in CA in 2017



# Structure

- ✦ Interaction-based planning
  - ⑩ Formal framework for 2-way interactions
  - ⑩ Probabilistic reasoning for multi-vehicle interactions



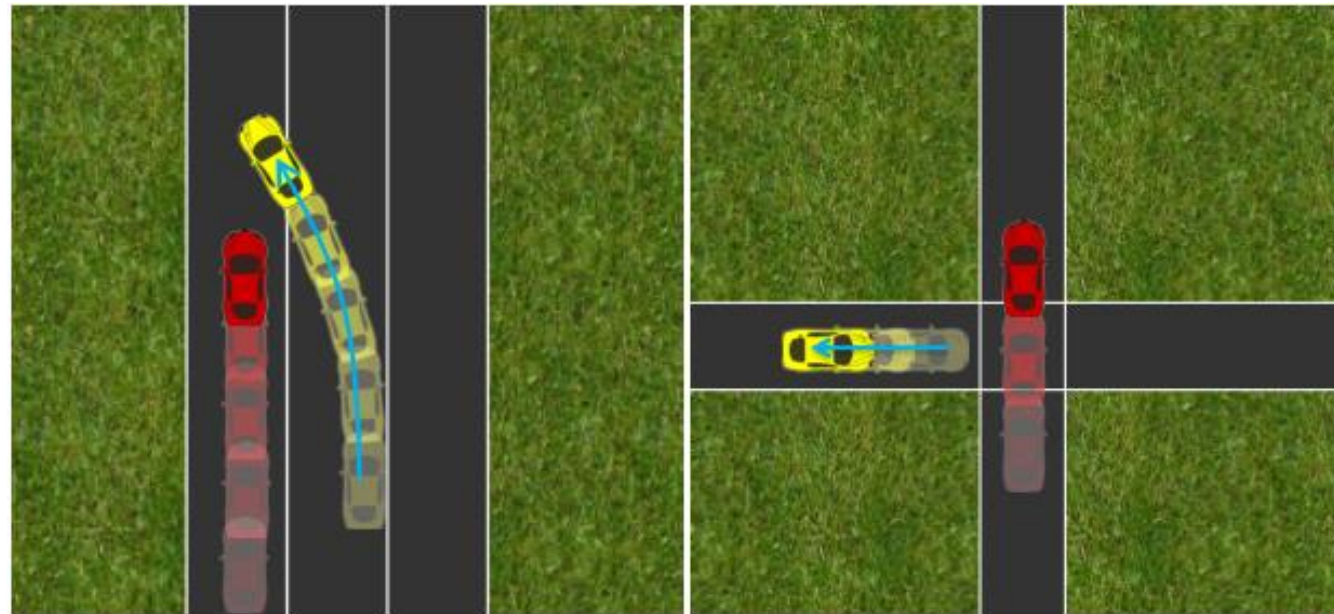
## Formal Framework for 2-way interactions

- ★ Dorsa Sadigh, Shankar Sastry, Sanjit A. Seshia, and Anca D. Dragan. **Planning for Autonomous Cars that Leverages Effects on Human Actions.** In Proceedings of the Robotics: Science and Systems Conference (RSS), June 2016.
- ★ Our key insight is that other drivers do not operate in isolation:
  - ⑩ an autonomous car's actions will actually have effects on what other drivers will do.
  - ⑩ Leveraging these effects during planning will generate behaviors for autonomous cars that are more efficient and communicative.



# Formal Framework for 2-way interactions

- ★ We model the interaction between an autonomous car and a human driver as a dynamical system, in which the robot's actions have immediate consequences on the state of the car, but also on human actions.



(a) Car merges *ahead* of human;  
anticipates human *braking*

(b) Car *backs up* at 4way stop;  
anticipates human *proceeding*



## Formal Framework for 2-way interactions

- ✦ Let  $x$  represent the state of the system, which includes positions and velocities of the human and autonomous robot.
- ✦ Effect of robot controls:  $x' = f_{\mathcal{R}}(x, u_{\mathcal{R}})$
- ✦ Effect of human actions:  $x'' = f_{\mathcal{H}}(x', u_{\mathcal{H}})$
- ✦ Overall dynamics of the system:  $x^{t+1} = f_{\mathcal{H}}(f_{\mathcal{R}}(x^t, u_{\mathcal{R}}^t), u_{\mathcal{H}}^t)$





## Formal Framework for 2-way interactions

- ★ Formulate choosing robot controls as a reward maximization problem
- ★ Reward function of robot

$$r_{\mathcal{R}}(x^t, u_{\mathcal{R}}^t, u_{\mathcal{H}}^t).$$

- ⑩ Reward function depends on  $u_{\mathcal{H}}$

- ★ MPC used at every iteration

- ⑩ Let  $x^0$  be the current state

- ⑩ Reward over MPC time horizon  $t$  is :

$$R_{\mathcal{R}}(x^0, \mathbf{u}_{\mathcal{R}}, \mathbf{u}_{\mathcal{H}}) = \sum_{t=1}^N r_{\mathcal{R}}(x^t, u_{\mathcal{R}}^t, u_{\mathcal{H}}^t)$$



## Formal Framework for 2-way interactions

★ At every iteration, the robot needs to find the  $\mathbf{u}_R$  that maximizes this reward:

$$\mathbf{u}_R^* = \arg \max_{\mathbf{u}_R} R_{\mathcal{R}}(x^0, \mathbf{u}_R, \mathbf{u}_{\mathcal{H}}^*(x^0, \mathbf{u}_R))$$

⑩  $\mathbf{u}_{\mathcal{H}}^*(x^0, \mathbf{u}_R)$  is what the human would do over the next  $N$  steps if the robot were to execute  $\mathbf{u}_R$ .

★ Typical solutions assume that the human will maintain current velocity

$$\mathbf{u}_{\mathcal{H}}^*(x^0, \mathbf{u}_R) = \mathbf{u}_{\mathcal{H}}^*(x^0)$$

⑩ Instead they assume that humans would maximize their own reward function.



# Formal Framework for 2-way interactions

## ★ Human driver reward

⑩ Use Inverse Reinforcement Learning (IRL) over driver demonstrations in simulation.

⑩ Assume a simple parameterization of human reward

## ★ Given a human reward function

⑩ Solve the optimization problem using quasi-Newton methods like L-BFGS

$$\mathbf{u}_{\mathcal{R}}^* = \arg \max_{\mathbf{u}_{\mathcal{R}}} R_{\mathcal{R}}(x^0, \mathbf{u}_{\mathcal{R}}, \mathbf{u}_{\mathcal{H}}^*(x^0, \mathbf{u}_{\mathcal{R}}))$$



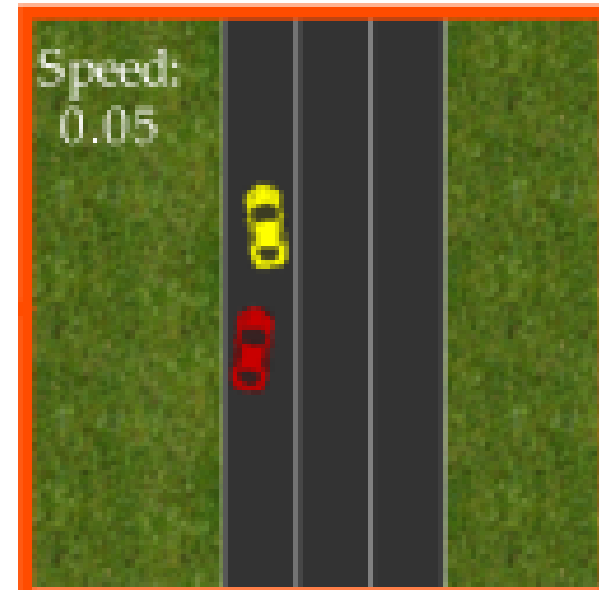
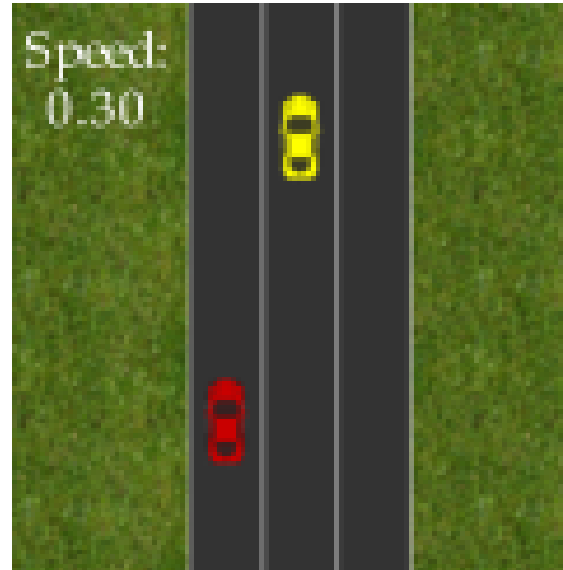
# Experiments

- ★ Assume a simple dynamics model of the car.
- ★ 3 Scenarios
  - ⑩ Make human slow down
  - ⑩ Make human change lanes
  - ⑩ Make human go first through intersection
- ★ In each case, hand engineer the robot reward function achieve the desired effect on human behavior



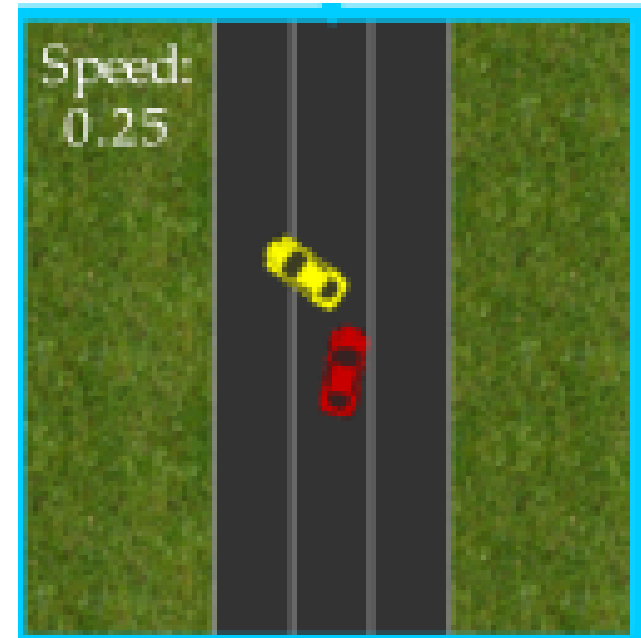
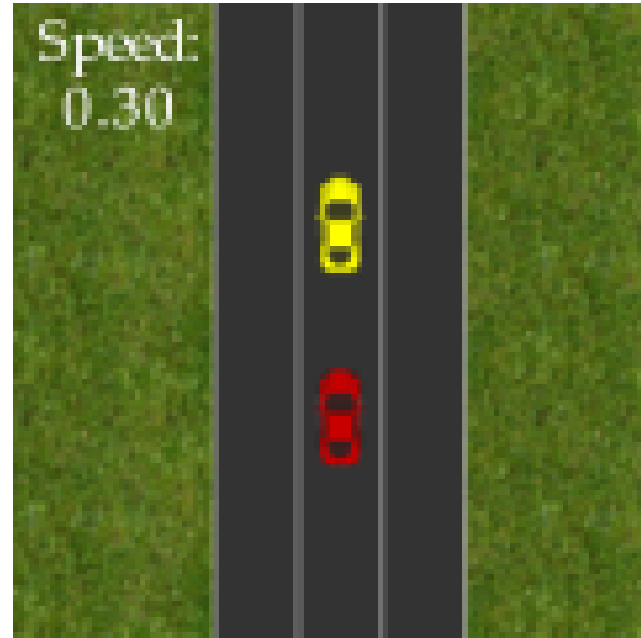
## Experiments: Make human slow down

- ✦ The robot plans to move in front of the person, expecting that this will make them slow down.
- ✦ Achieved by augmenting the robot's reward with the negative of the square of the human velocity.



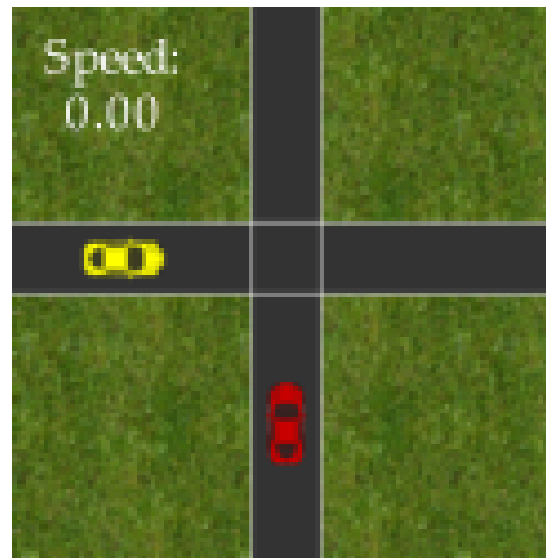
## Experiments: Make human change lanes

- ✦ The robot plans to purposefully occupy two lanes, expecting this will make the human move around it by using the unoccupied lane.
- ✦ Achieved by augmenting the robot's reward with the lateral position of the human



## Experiments: Make human cross intersection first

- ★ The robot plans to purposefully back up slightly, expecting this will make the human cross first.
- ★ Achieved by augmenting the robot's reward with a feature based on the position of the human car relative to the middle of the intersection.
  - ⑩ Communication behavior emerges naturally out of reward optimization.



# Structure

## ★ Interaction-based planning

⑩ Formal framework for 2-way interactions

⑩ Probabilistic reasoning for multi-vehicle interactions





# Behavior Prediction

- ★ Galceran, E., Cunningham, A. G., Eustice, R. M., & Olson, E. (2017). **Multipolicy decision-making for autonomous driving via changepoint-based behavior prediction: Theory and experiment.** *Autonomous Robots*, 1-16.
- ★ Choose ego-vehicle actions that maximize a reward function over time within a dynamic, uncertain environment with tightly coupled inter-actions between multiple agents.



# Behavior Prediction

- ★ Assume a set of a priori known policies
  - ⑩ Go straight, change lanes, merge left, merge right etc
- ★ Leverage Bayesian change-point detection to estimate the policy that a given vehicle was executing at each point in its history of actions.
  - ⑩ Given current policy, infer the likelihood of actions or intentions.
- ★ Statistical test for detecting anomalous behaviors.



# Behavior Prediction

- ✦ Bayesian change-point detection over 30 s windows

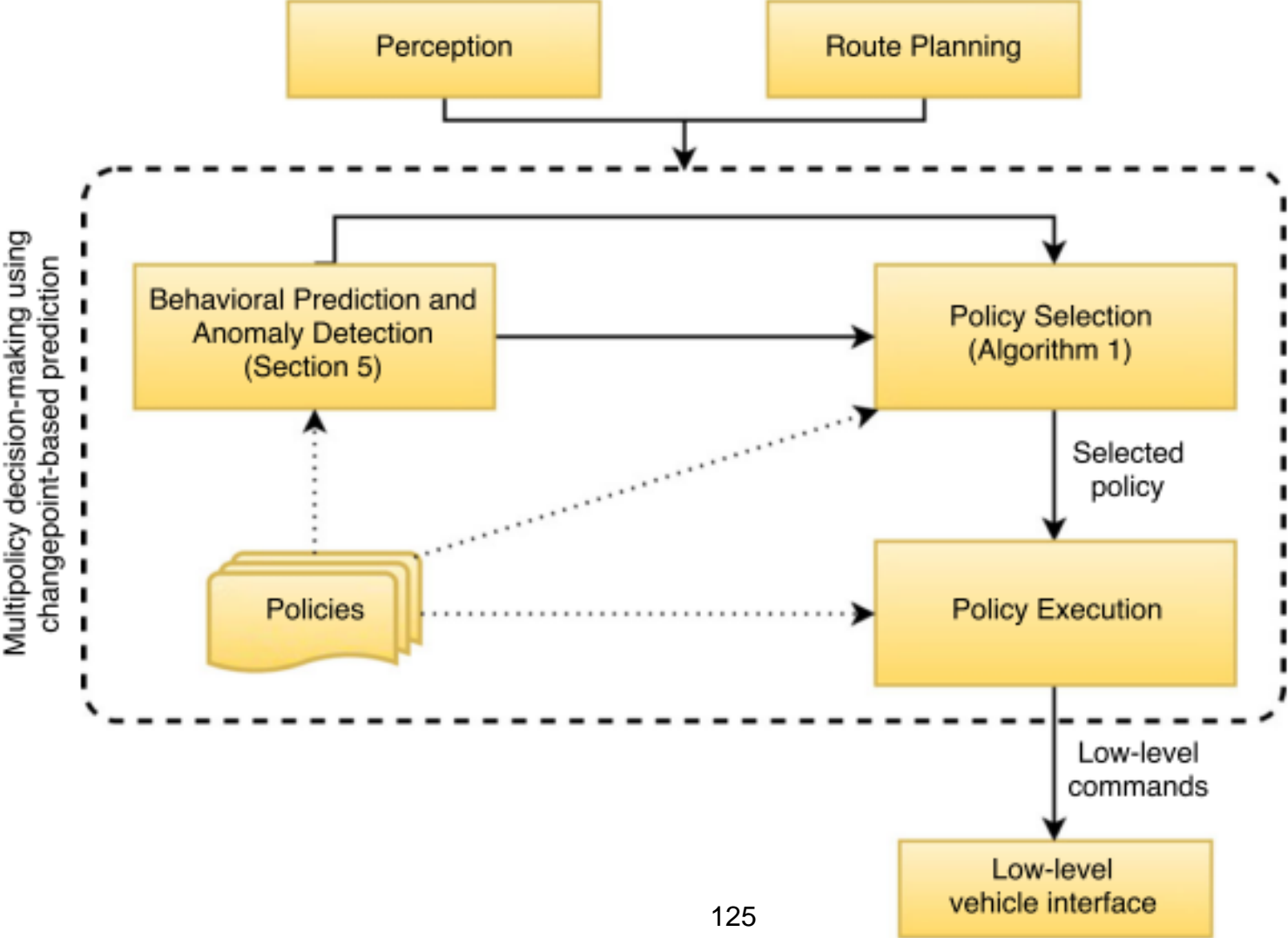


# Multi-policy decision making

- ★ Draw set of sample policies over distribution for neighbor vehicles
  - ⑩ For each sample set
    - ★ Simulate other vehicles forward
    - ★ Choose a policy for ego vehicle that maximizes reward in this instance
    - ★ Track best reward
- ★ Choose policy for ego vehicle with the best reward



# Approach



# Conclusion

- ★ Proof of concept tests in real world and simulation
  - ⑩ Good real world results in “offline” behavior prediction
- ★ Limitations
  - ⑩ No guarantees in decision making
  - ⑩ A very coarse approximation of POMDP
  - ⑩ Decision making is slow
    - ★ 2-4 neighbors with small set of policy samples
    - ★ Anomalous detection does not influence decision making



# Questions?



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